



Please take some time to  
**PLAY!** Engage with a  
question and the materials.



# Acknowledgement



Before going any further, it is important that we recognize that we are here today to learn on the unceded, shared territories of the Coast Salish people on which our schools are located. We recognize that the Katzie and Semiahmoo First Nations who have signed the Surrey Schools Aboriginal Education Enhancement Agreement.



# Playful Mathematical Inquiry in Grades 3 to 5: Multiplication



February 16th, 2017 ~ STA Focus Day  
North Surrey Secondary School  
Presented by Jen Barker  
Twitter: @barkerJBarker

# Acknowledgements

- Thanks to Cynthia Walker, Gurpreet Koonar, Diane Brebeck, Hyekyung Lee for letting me try out some lessons in their classes!
- These ideas have been collected and/or inspired from a number of sources. Please see hand out for specifics!





# Learning Intentions

- I have an emerging definition of PLAY!
- I understand there are different types of inquiry and what these look like.
- I understand my role as the teacher during playful mathematical inquiry, including designing the learning opportunities, asking nudging questions, and providing formative and summative assessment.
- I have a few ideas about how to design and incorporate playful Mathematical inquiry in my math class with regard to multiplication.

# Where can you find PPT, learning intentions, and more ideas?

[www.meaningfulmathmoments.com](http://www.meaningfulmathmoments.com)

HOME MUSINGS RESOURCES IDEAS CR4YL PRESENTATIONS/PUBLICATIONS



Click the  
Presentations tab  
and look for STA  
Focus Day

## Meaningful Moments in MATHEMATICS



Welcome! Thanks for stopping by my site. I was inspired to write down my Mathematical musings by several other Math educators who have generously shared their stories with me either through workshops, blogs, Twitter, or through publications and have inspired my love of Mathematics and shaped my practice.

I have taught Kindergarten through Grade Five in both Richmond and now the Surrey School District. This year I have two roles. As an Early Numeracy Teacher, I work in an inner-city school with four amazing primary teachers supporting their students in Mathematics. My other position is as the Changing Results for Young Learners Numeracy Advocate. In this role I work with 31 teachers who are participating in a inquiry-based initiative.

### Tweets by @Barkerjbarker

Jennifer Barker Retweeted



ASCD @ASCD

The goal of a class should be for students to walk away with the love of learning  
[bit.ly/2eLtWAR](https://bit.ly/2eLtWAR)





What grade do you teach? Why  
did you sign up for this session?



# PLAY

Diminished consciousness of self

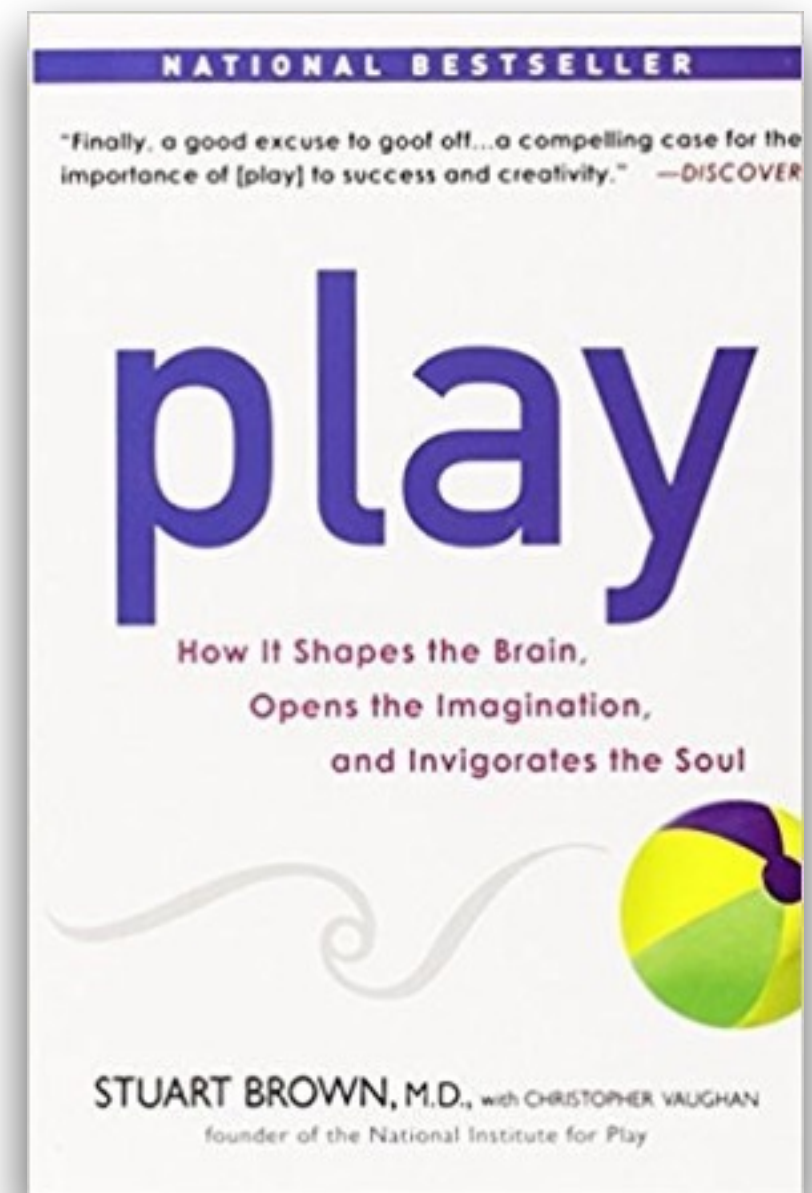
- no good or bad
- willingness to take risks

Improvisational Potential

- its openness
- co-constructing understanding

Continuation Desire

- it hooks! Focused attention
- self motivated





# What is Inquiry-based learning?

Inquiry-based Learning is a dynamic and emergent process that builds on students' natural curiosity about the world in which they live.

As its name suggests, Inquiry places students' questions and ideas, rather than solely those of the teacher, at the centre of the learning experience. Students' questions drive the learning process forward.

Teachers using an inquiry-based approach encourage students to ask and genuinely investigate their own questions about the world.

Teachers further facilitate students' learning by providing a variety of tools, resources, and experiences that enable learners to investigate, reflect, and rigorously discuss potential solutions to their own questions about a topic the class is studying.



# Shifting Pedagogical Paradigms

Traditional learning	Inquiry learning
Have to learn	<b>Want to learn</b>
What to know	<b>How to know</b>
Tell and memorize	<b>Ask and inquire</b>
Only one right answer	<b>Many conclusions</b>
Teacher-directed	<b>Learner-centred</b>
One-size-fits-all	<b>Personalized</b>
Passive learning	<b>Active learning</b>
Assess for marks	<b>Assess for learning</b>



# Types of Inquiry



## Structured Inquiry:

- The teacher determines the big idea and what the students will come to understand by the end.
- The teacher starts with the guiding question.
- The students help create the plan and guide the inquiry with their questions, interests, ideas, analysis, reflections and understandings.

## Guided Inquiry:

- The teacher comes up with the big idea or topic and or the teacher come up with the questions.
- The students are responsible for designing and following their own procedures to test the question and then communicate their results and findings.

### Open Inquiry:

- The students determine the purpose and formulate the questions.
- The students design procedures, gather the materials and communicate their findings.
- The teacher facilitates, supports, asks questions and redirects the investigation.



From Michelle Hikida, Richmond Teacher



# What might this look like in my classroom?

## Whole class structured inquiry

- everyone has the same question & the same materials



## Whole class guided inquiry

- everyone has same question and chooses from the different materials at each table

## Small groups guided inquiry

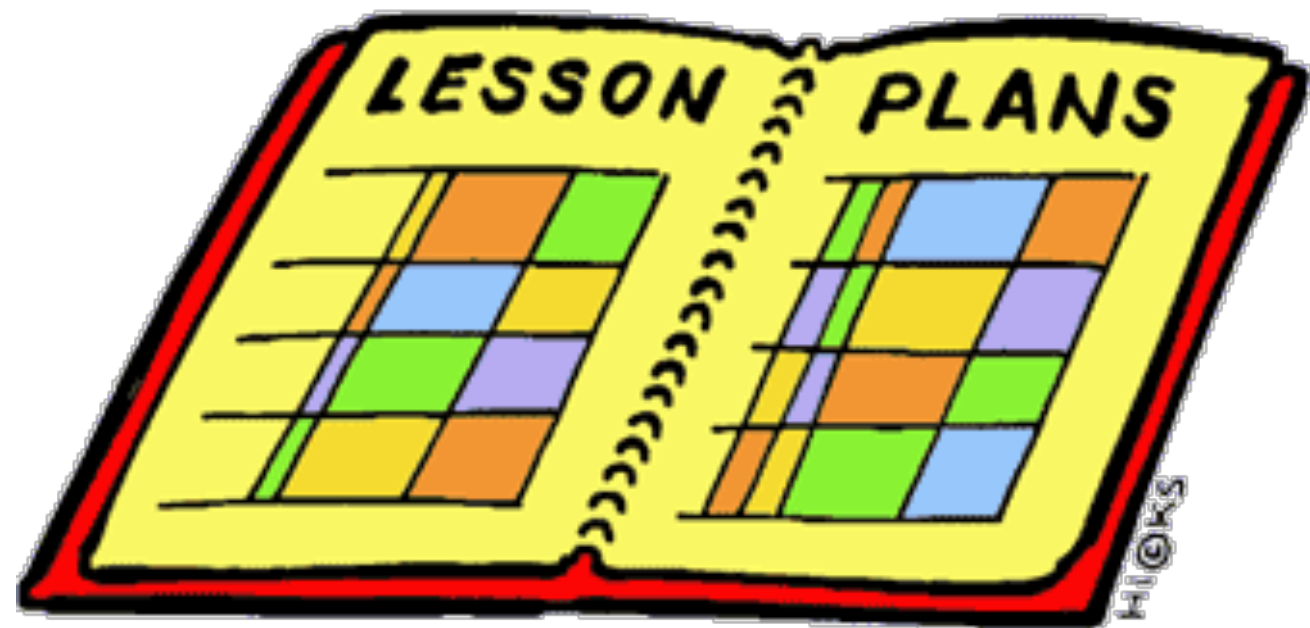
- Different questions and different materials at each table
- could have 2, 3, or 4 questions around the class

## Individual or Partner Open Inquiry

- Lots of different questions
- Many different materials dependent on what students choose

# Structure of a Whole Class Lesson

1. Introduce the problem - use a book, image, artifact
2. Exploration Time - what materials will you need?
3. Sharing - what strategies did you try?





# Developmental progression of Multiplication

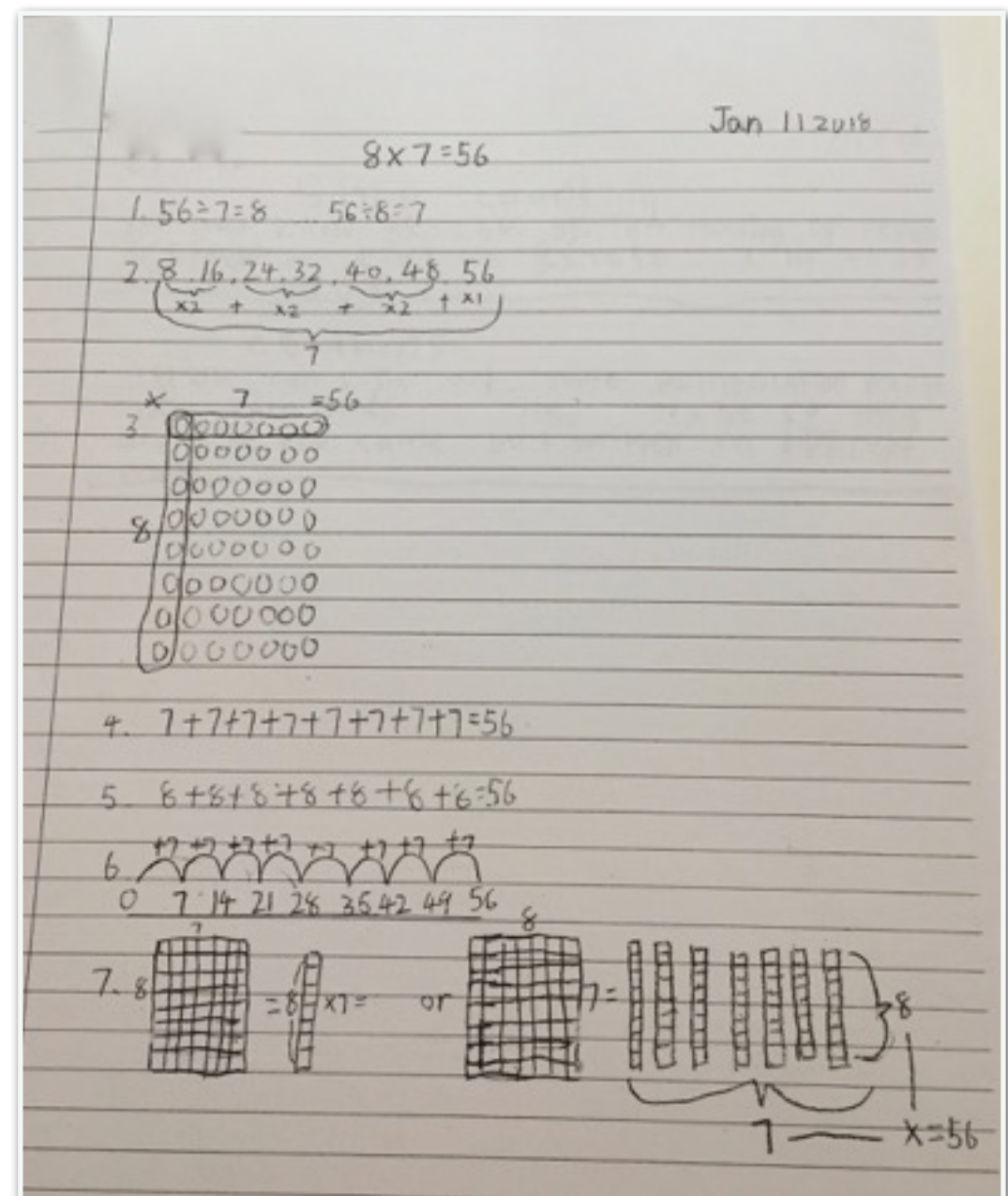
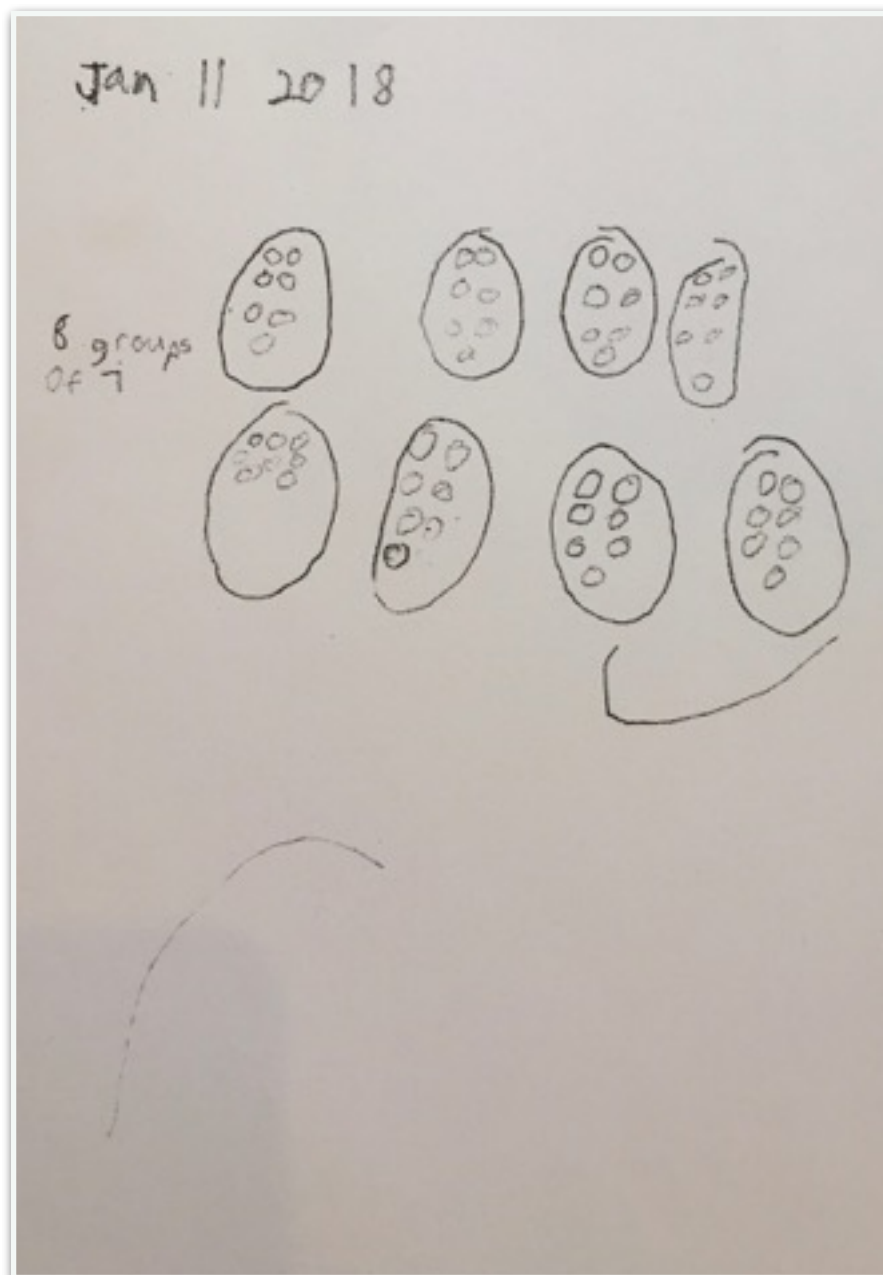
- Recognizing Equal Groups
- Multiplying Equal Groups - skip counting & repeated addition & groups of
- Multiplying Using Rectangular Arrays
- Using Multiplicative Thinking to Solve Single & Multi-digit questions including language such as times, twice as many, etc.
  - Using known facts and compensating
  - Doubling and Halving
  - Using the commutative property
  - Using the distributive property
  - Using the associative property



# Finding Out What Students Know

# Activating Prior Knowledge

What are all the ways you can show  $8 \times 7 =$

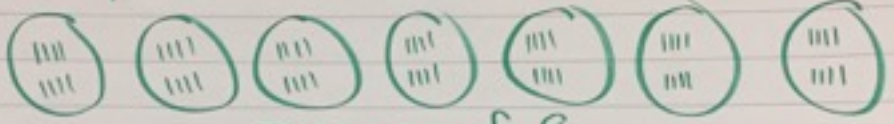




AFTER: Students share aloud the strategies they know!

Strategies for Multiplication

Groups of Model or Picture



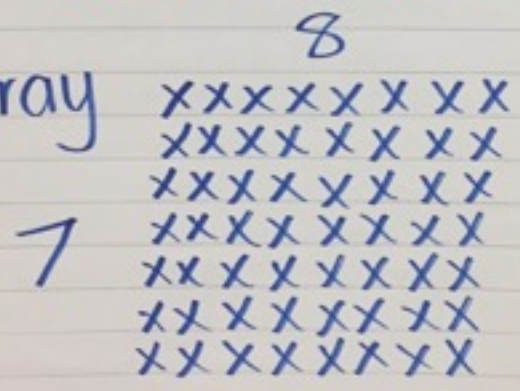
7 groups of 8

Skip Counting  
8, 16, 24, 32, 40, 48, 56

Array

8

7



Related Facts

$$56 \div 7 = 8$$
$$56 \div 8 = 7$$

Using Facts I know / Friendly Facts

$$8 \times 7 = 56$$
$$8 \times 8 = 64$$
$$64 - 8 = 56$$

half of 8 is  $\rightarrow 4 \times 7 = 28$  and  $28 + 28 = 56$

half of 8 is 4 half of 4 is 2 so  $8 = 2 \times 2 \times 2$

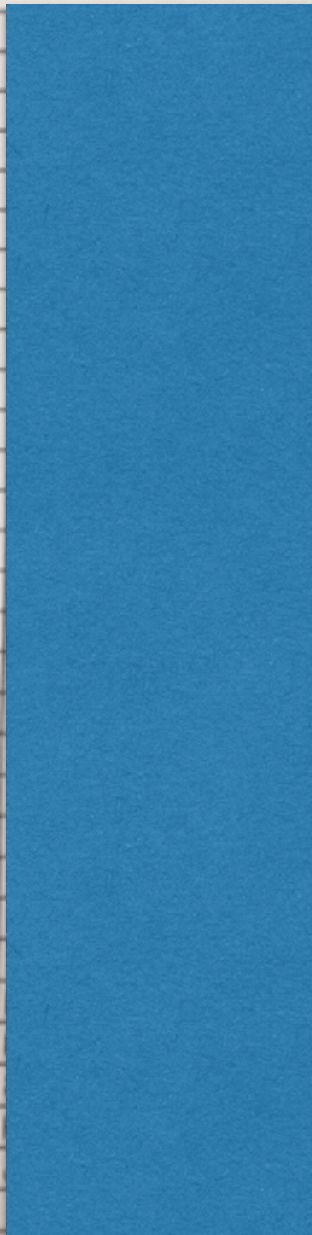
$$56 \div 2 = 28$$
$$28 \div 2 = 14$$
$$14 \div 2 = 7$$

Commutative Principle

$$8 \times 7 = 56$$
$$7 \times 8 = 56$$

↑ ↑  
Factors can be rearranged and the product is the same.



[illegible]

Lucas: "I know what times means but I can't explain it. I'm not good at math."

Me: Can you think of it as groups of?

Lucas: Maybe

Me: Would drawing a picture help?

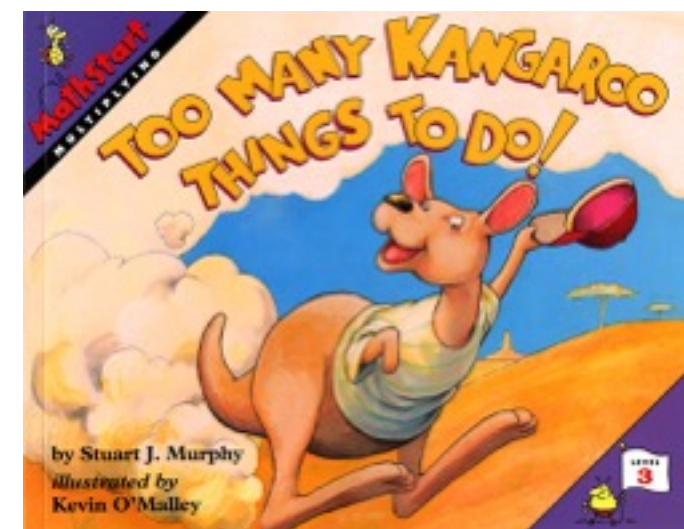
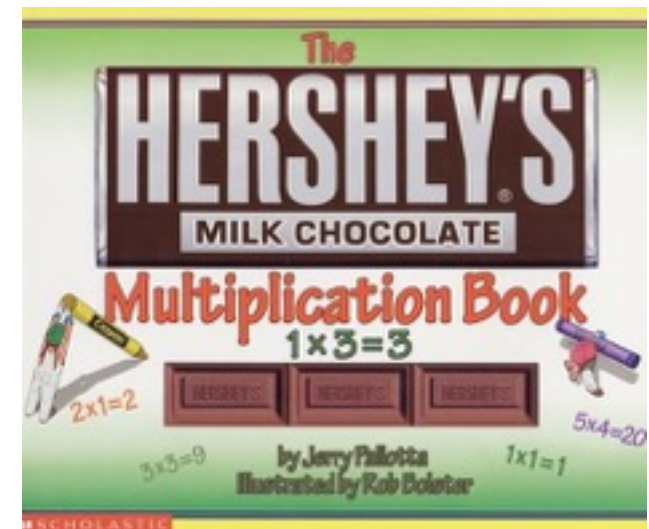
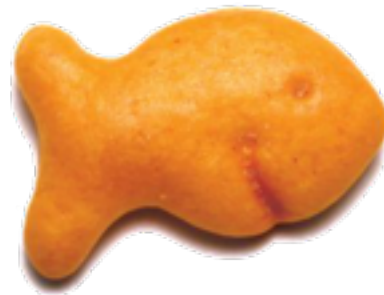
# How might you plan your Multiplication unit?





# Designing learning opportunities that are PLAYFUL & ENGAGING?

- Exciting literature
- Inviting Materials
- Connected to students' interests
- Multi-modal - hands on, kinesthetic, visual, auditory
- Opportunities for Collaboration
- Organized





Lessons that provided an entry point  
for all and allow each student  
to work to their potential

Learning Intentions for:

ALL

SOME

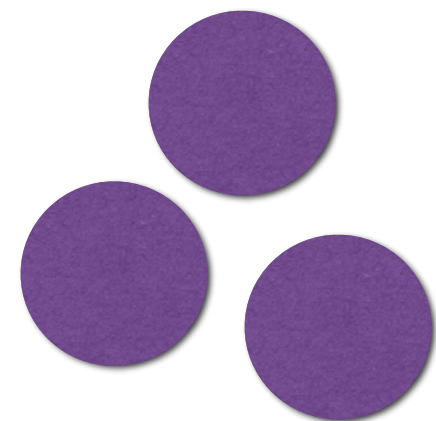
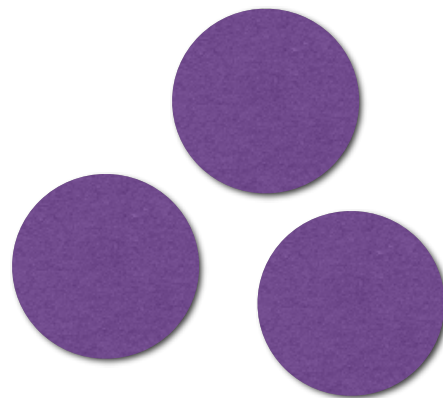
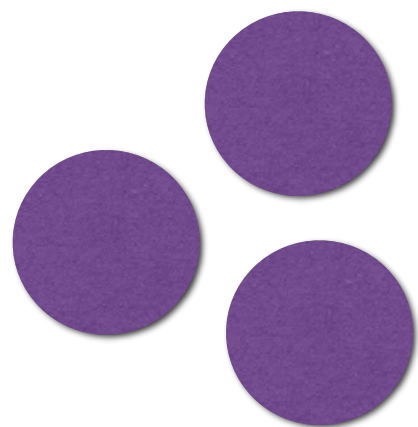
FEW



Thanks to Shelley Moore for her work in this area.

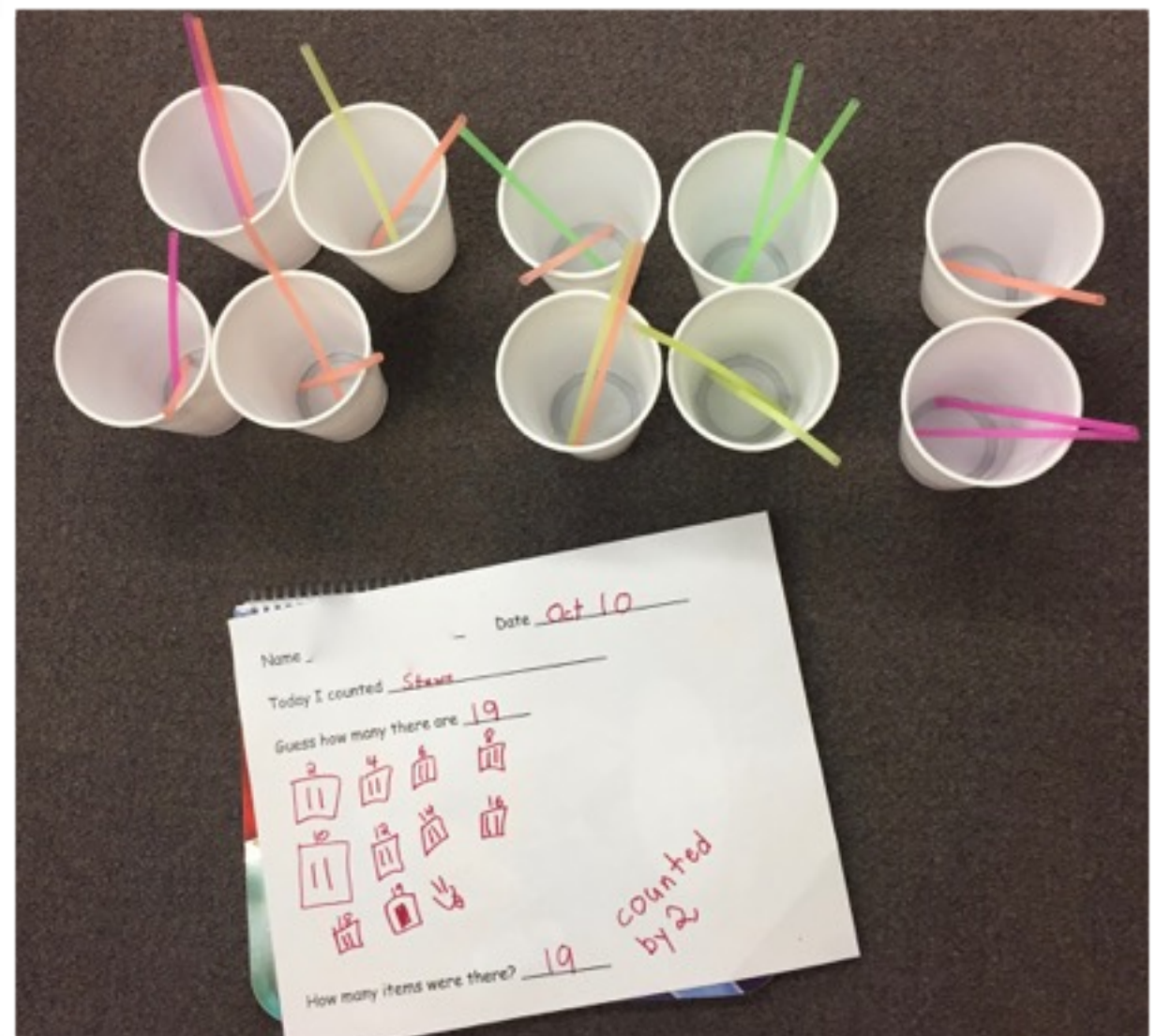
# How do we assist students in seeing equal groups?

- Counts by equal groups (e.g., 2's, 5's, 10's, and so forth)
- Knows the quantity stays the same when counted by different sized groups (conservation of number)
- Identifies and extends the number pattern that emerge when counting by equal groups





# What are the different ways you could count your collection?





# What comes in equal groups?

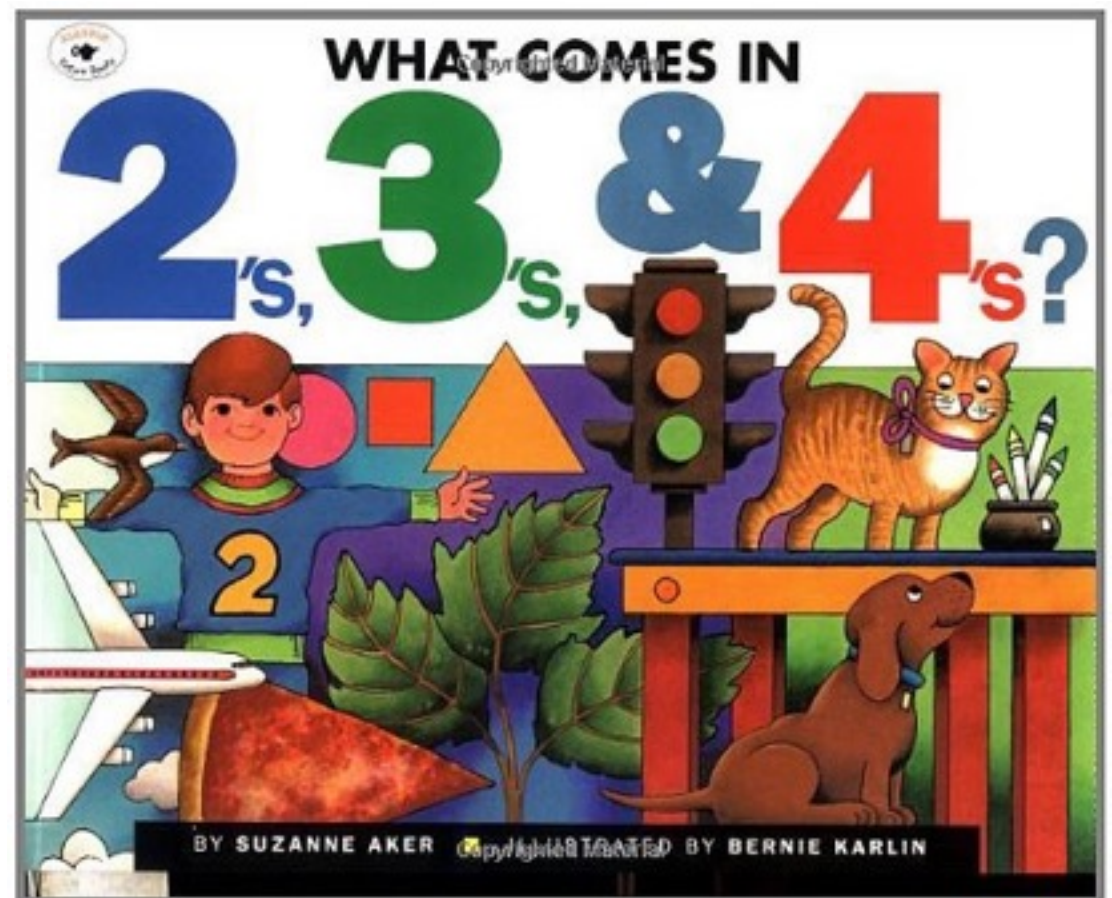
2

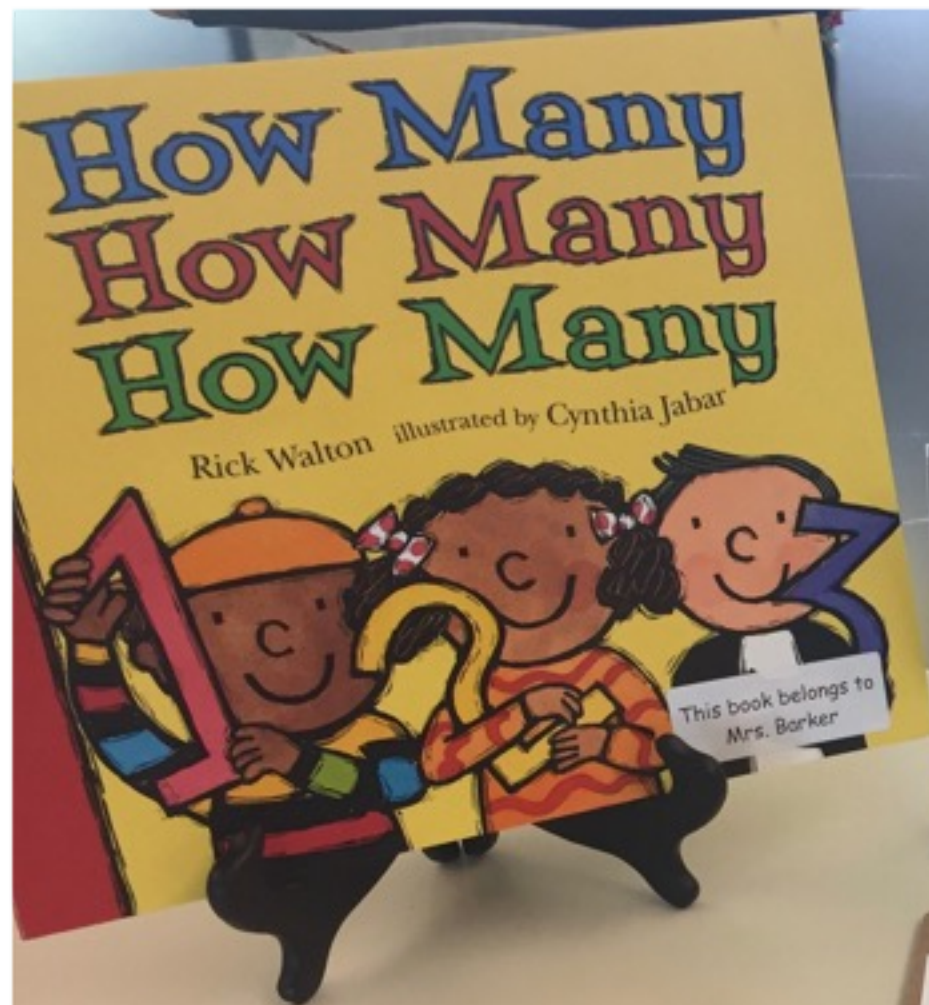


eyes  
ears  
hands  
feet  
shoes

4

Dog legs





**Multiplication:**  
What items come in "groups of"? Can you think of items for numbers 1 – 12?





## Multiplication:

How can hundreds charts help you think about your question?

$$9 \times 7 =$$

$$9 \times 6 =$$

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

6, 12, 18, 24, 30, 36

42, 48, 54

I can skip count.

9 jumps of 6 is 54

$$9 \times 6 = 54$$

Sharpie



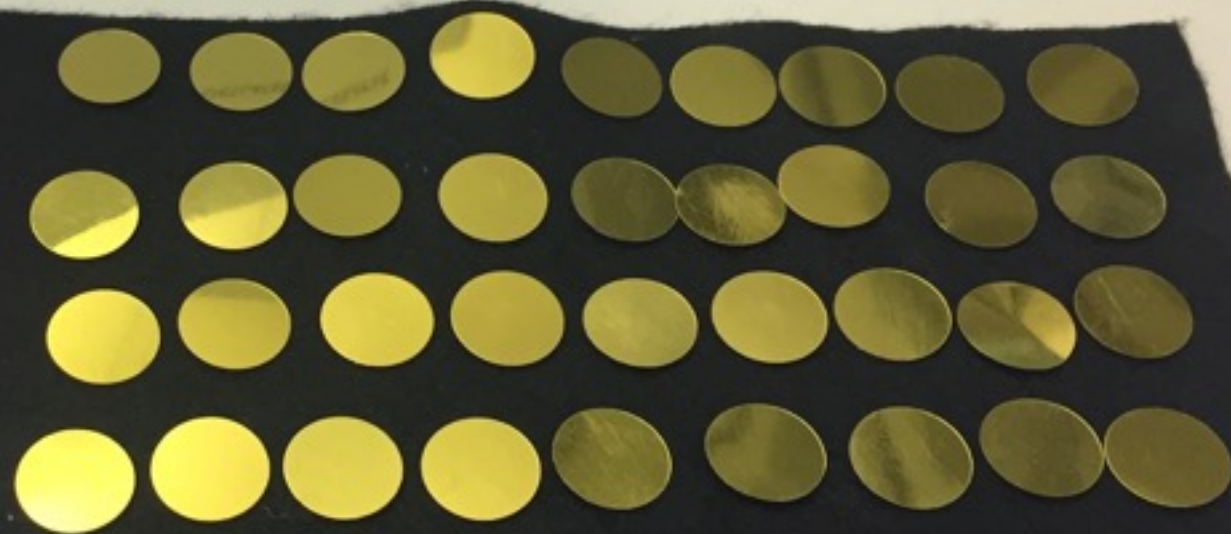


## Multiplication:

How do T charts help us to count groups of items?

$$4 \times 9 =$$

n	q
1	9
2	18
3	27
4	36



## Two of Everything

Jilly Toy Hong



## Multiplication:

How are repeated addition and multiplication connected?



$$4 + 4 + 4 + 4 + 4 = 20$$

4 + 4 = 8

4 + 4 = 8

4 + 4 = 8



# How do we help our students develop understanding of multiplying equal groups?

- Counts groups as single entities (unitizes)
- Distinguishes between number of groups and number of objects in a group
- Show with models “a number of groups of a certain size” when the language of “groups of” is presented with various terms (e.g., “piles of,” “stacks of,” “rows of,” “cups of,”)
- Interprets word problems using models and drawings showing the number of groups and the number in each group
- Records number of groups in each step of a skip counting pattern, relating it to multiplication (Repeated addition and skip counting)



How many? How many in  
each? How many altogether



$$4 \text{ groups of } 2 = 8$$
$$4 \times 2 = 8$$



## Multiplication:

What multiplication game(s) can you create?

Bayer  
Bayer

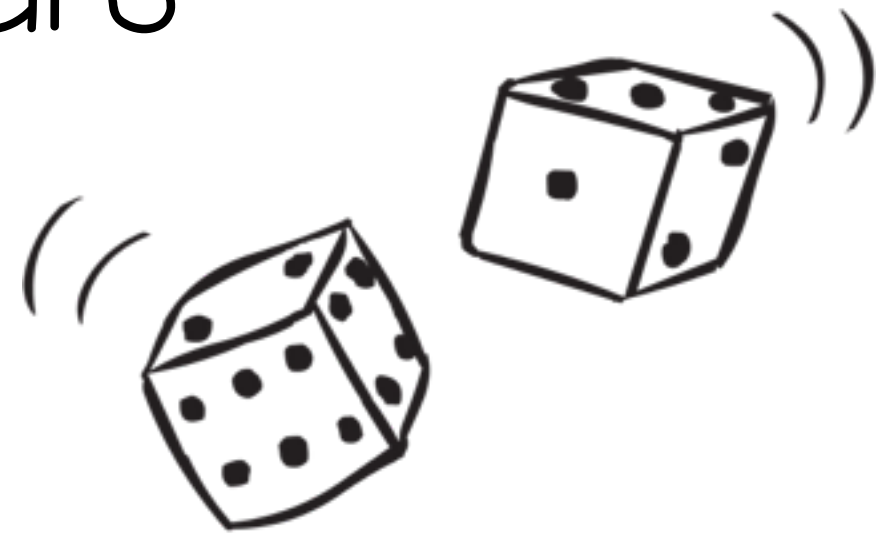
Bayer

Jen	Julie
$3 \times 3 = 9$	$6 \times 5 = 30$
$4 \times 4 = 16$	
<u>25</u>	



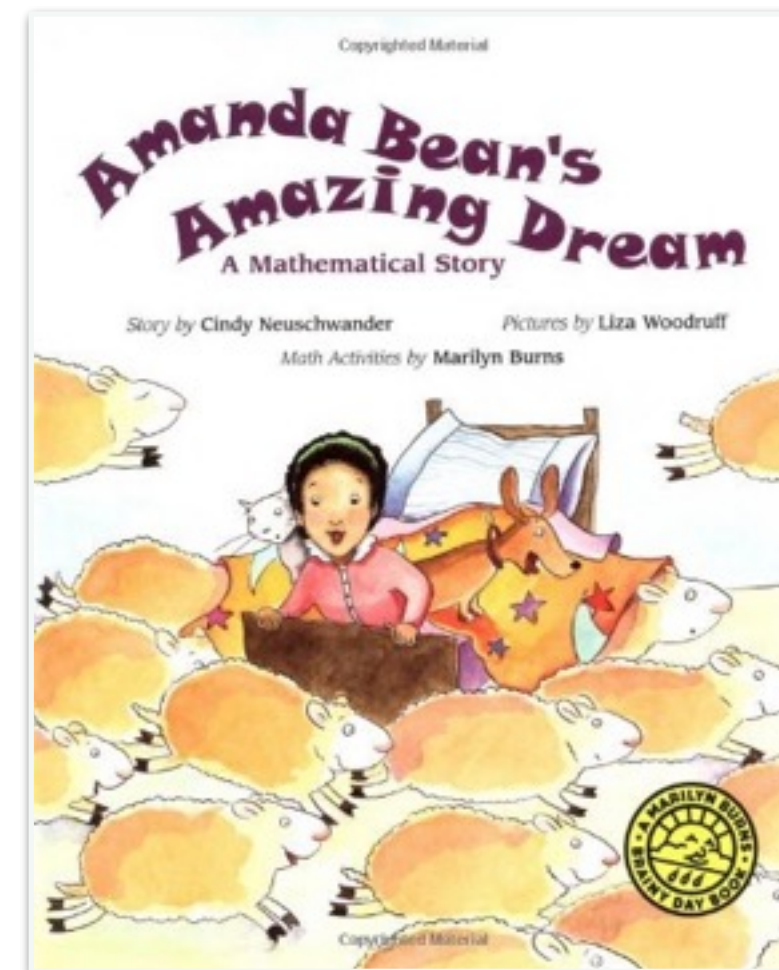
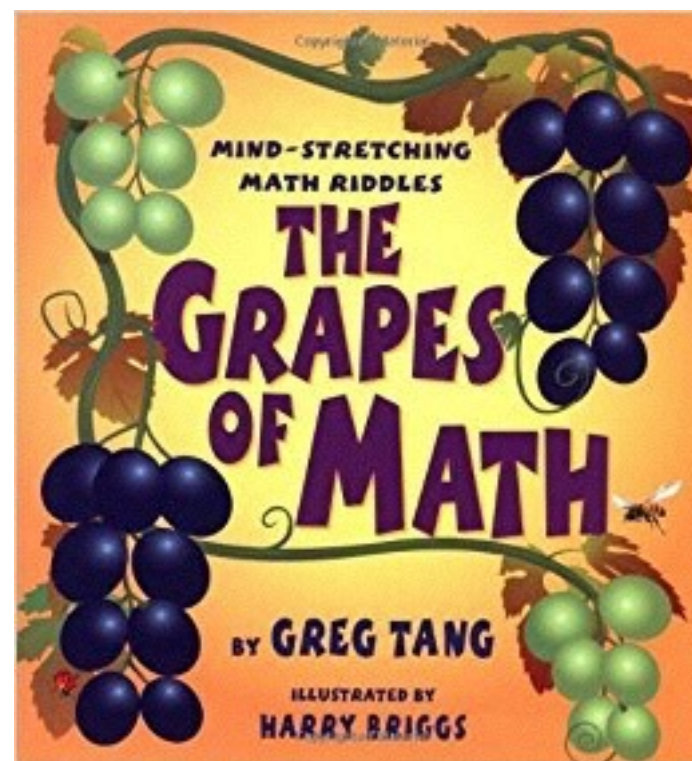
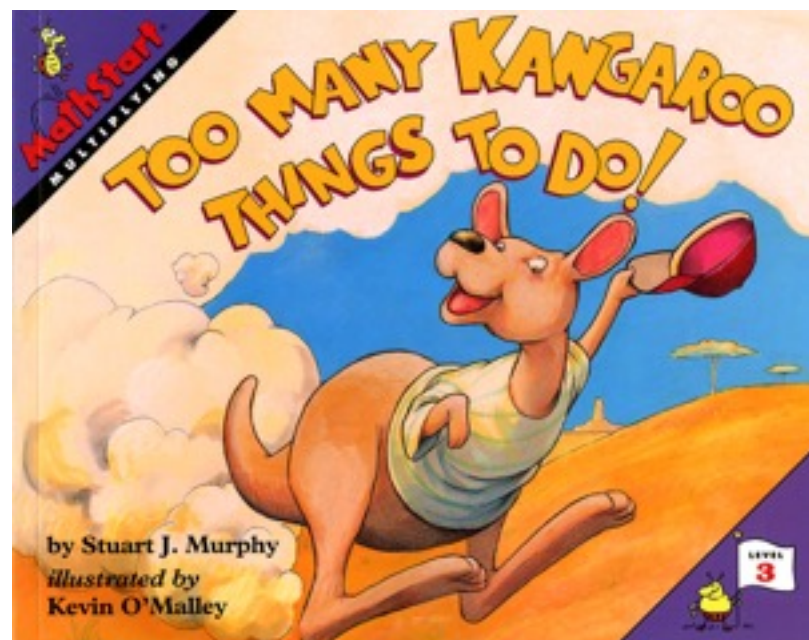
# Circle and Stars

A Marilyn Burns classic! Play with a partner.  
Each game has eight rounds.



$$2 \times 3 = 6$$

[https://www.kyrene.org/cms/lib/AZ01001083/Centricity/Domain/1309/Circles  
%20and%20Stars%20Directions.pdf](https://www.kyrene.org/cms/lib/AZ01001083/Centricity/Domain/1309/Circles%20and%20Stars%20Directions.pdf)



Look at a page from the story.  
What question could you ask the  
multiplication could help you solve?  
Try it out!



Then I notice something. It looks like eight bicycles with sheep on them.

"How many wheels is that?" I wonder. I start counting, but the sheep whiz by so fast, I cannot count all the bicycle wheels.

"Wait!" I yell. "I am Amanda Bean and I count anything and everything!"



What question might your students ask?



## Multiplication:

Create a scene. What multiplication stories can you tell?



$$5 \times 2 = 10 \text{ frogs}$$

$$1 \times 3 = 3 \text{ elephants}$$

13 animals



## Multiplication:

I see \_\_\_\_ groups of \_\_\_\_.

What could I be looking at?

I see 4 groups of 12 roses.  
I could be looking at flowers  
in a store

I see 3 groups of 2 strawberries.  
I could be looking at 6  
berries on my plate.



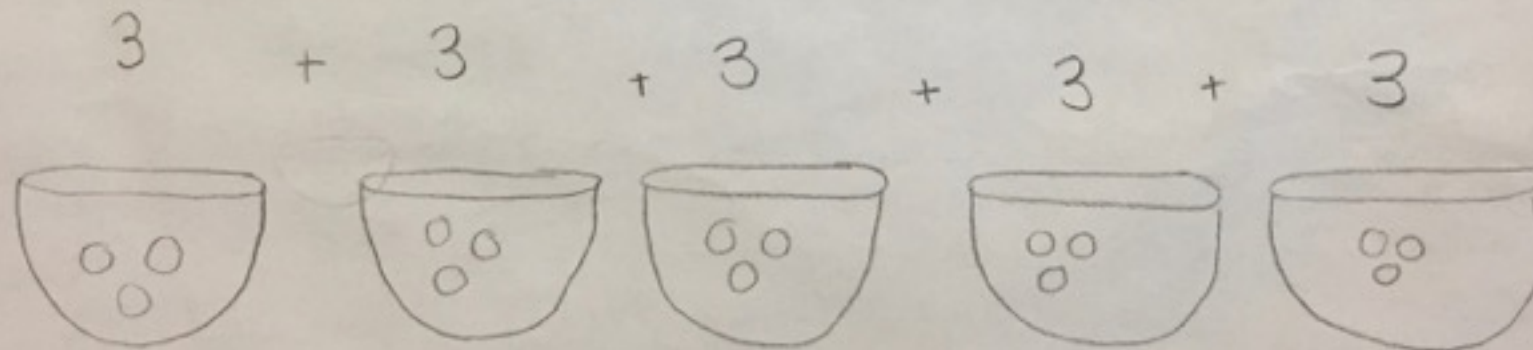
## Dim Sum for Everyone!

Your family decides to order Dim Sum for dinner. The dishes of dim sum are served on plates with 3 treats each. How many treats would come to your table?



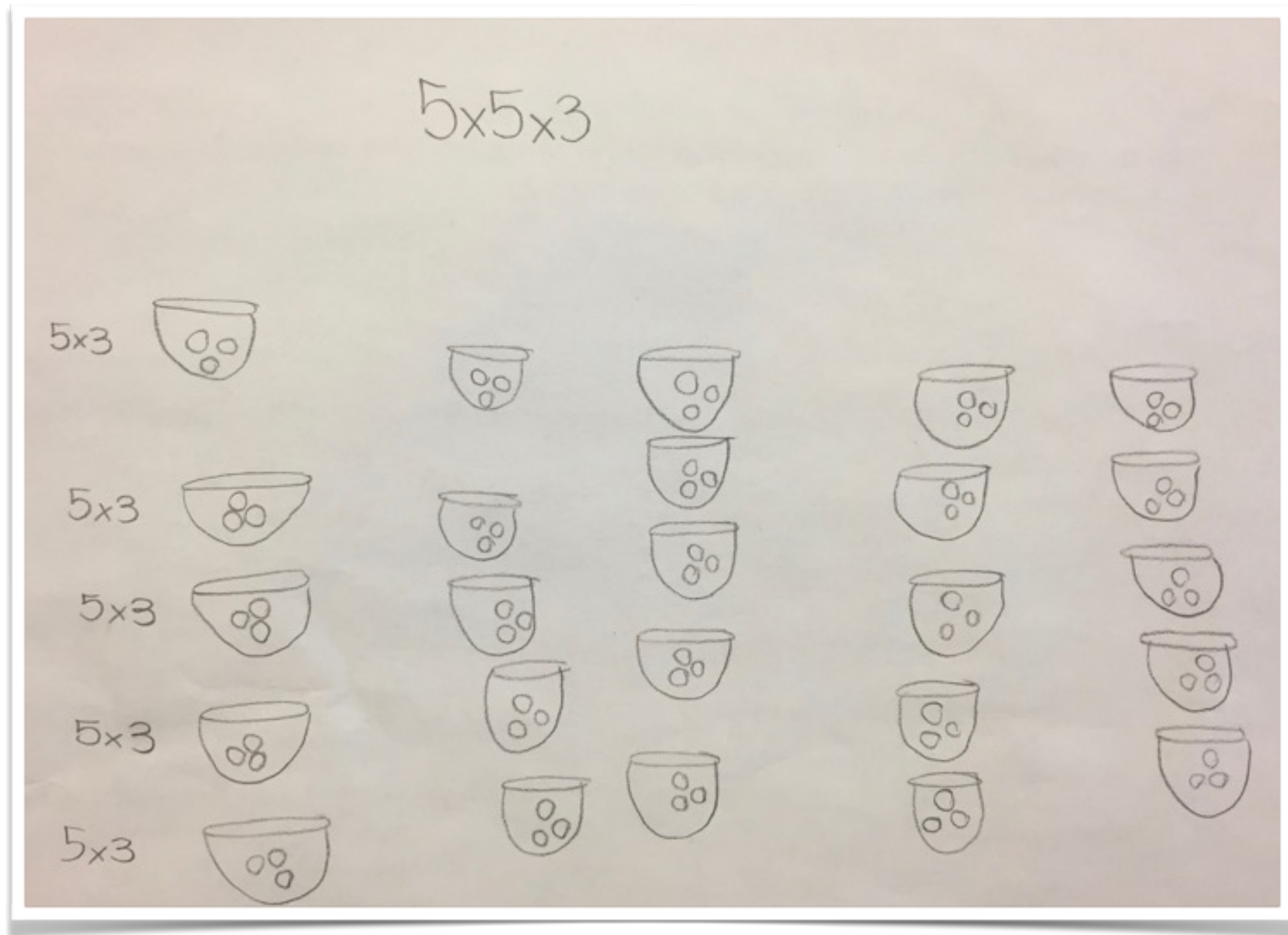
15 treats would come to our table.

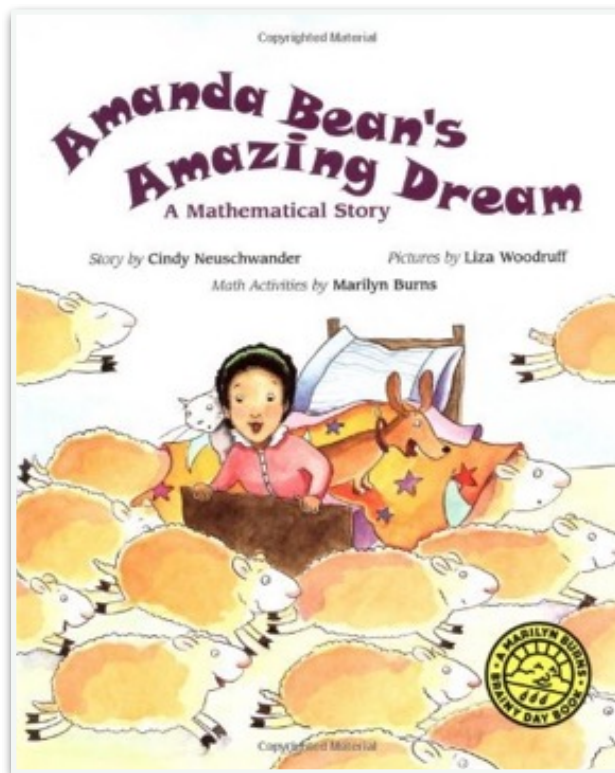
5 groups of 3 = 15





What if your family received five different servings of Dim Sum?





Name: \_\_\_\_\_



## Amanda Bean's Amazing Dream

# Which Has More?

*For each question, explain your thinking using numbers, pictures, and/or words.*

Which has more cookies,

- a tray with \_\_\_\_ rows and \_\_\_\_ cookies in each row, or
- a tray with \_\_\_\_ rows and \_\_\_\_ cookies in each row?



Which has more wheels, \_\_\_\_ tricycles or \_\_\_\_ bicycles?



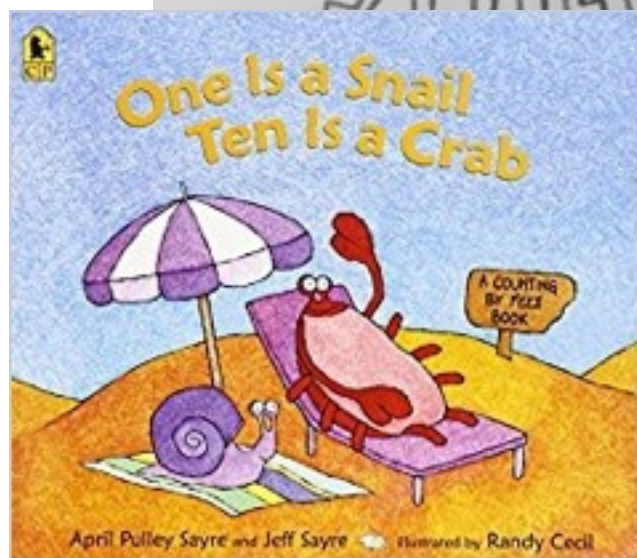
Thanks to Marc  
Garneau for sharing  
these!

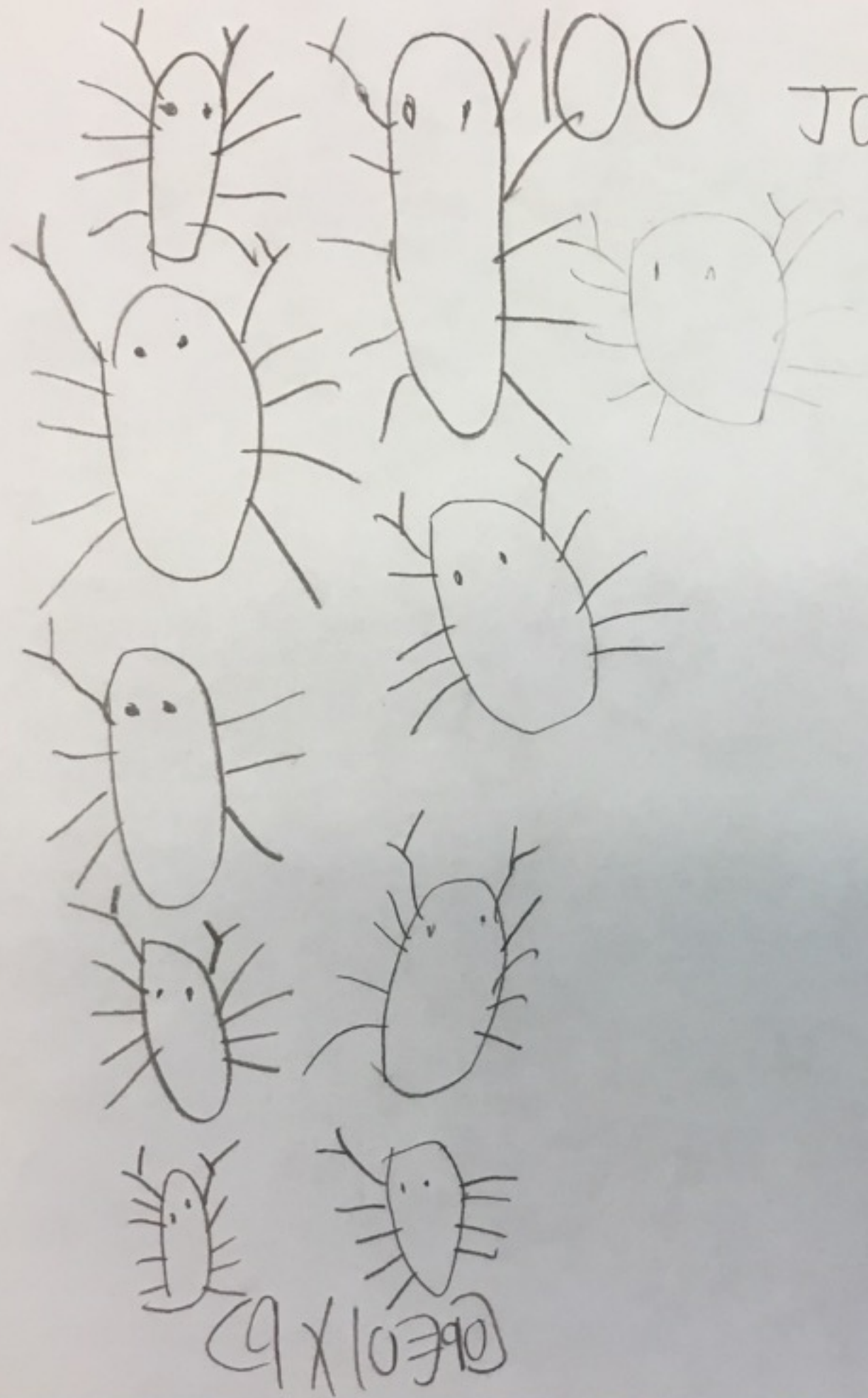


40 legs

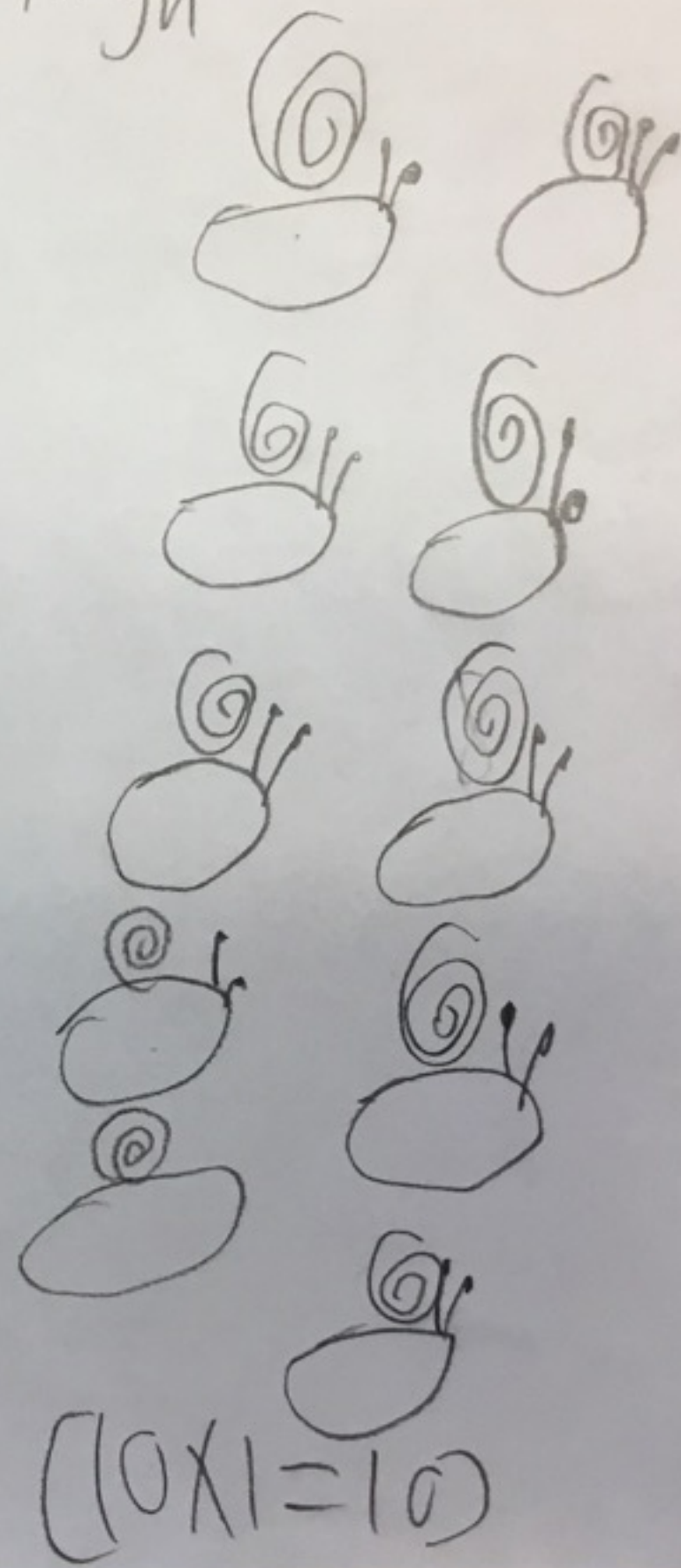


$$(2 \times 10) + (10 \times 2) \\ 20 = 40 = 20$$





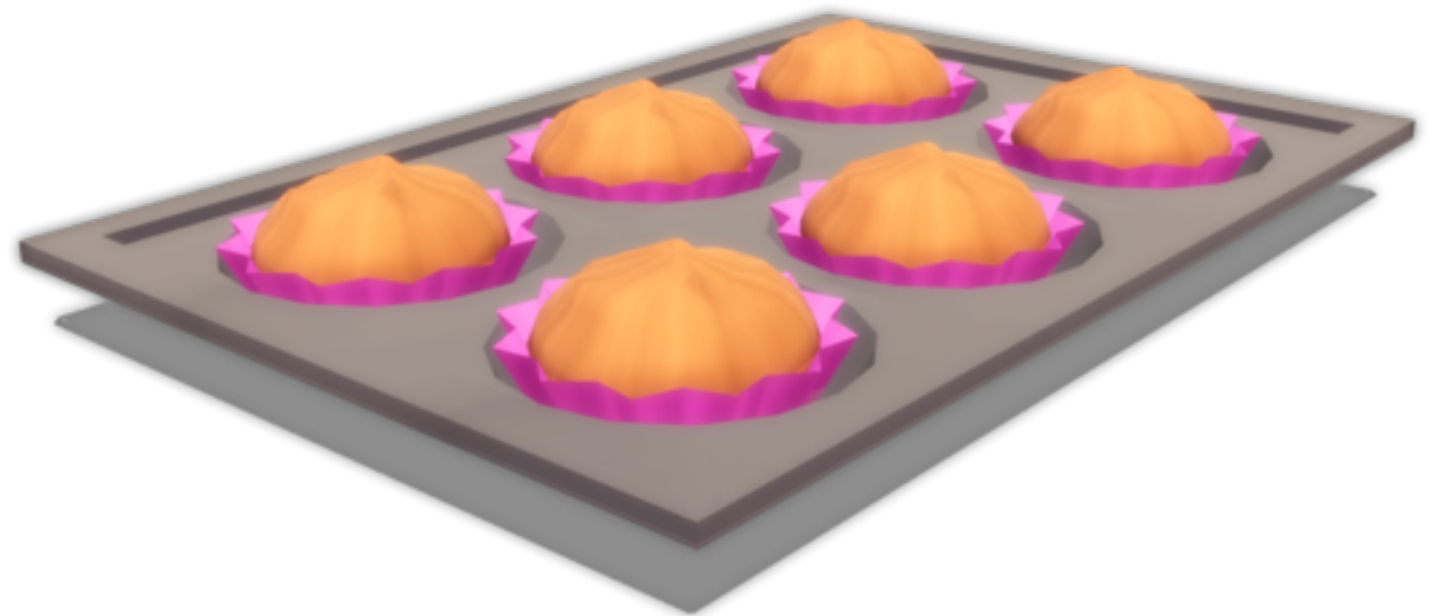
Jair Singh 10

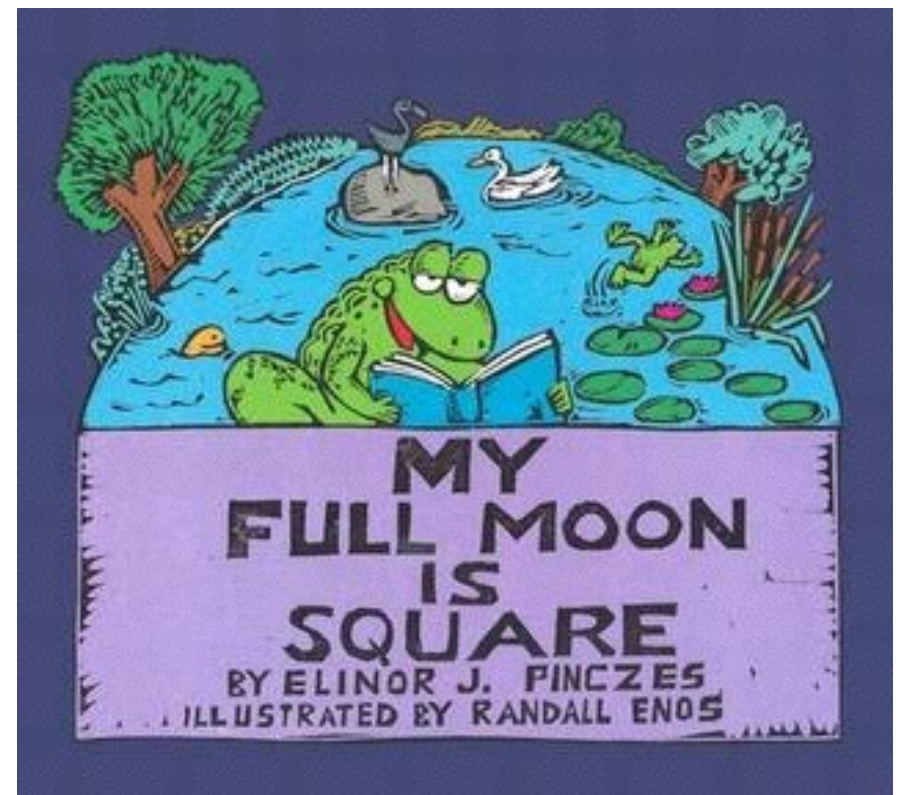




# How do we assist students in multiplying using rectangular arrays?

- Builds rectangular arrays using “rows of”
- Describes arrays in terms of equal groups (usually by rows)
- Partitions arrays into smaller arrays
- Describes arrays in terms of equal groups when the array is only partially visible





Can you represent the arrangement of \_\_\_\_ flies?  
How might you describe it?



## Multiplication:

Using square tiles represent a multiplication question that has the same factors (e.g.,  $7 \times 7$ ) in an array.

What do you notice? What do you wonder?

Boysen  
Bunker



# How many different ways can you arrange the chocolates?

Name of Elementary  
6505 123A Street  
Surrey, BC  
Canada, V3W 5Y5



February 17<sup>th</sup>, 2017

Hershey's Canada  
5750 Explorer Drive  
Mississauga, Ontario  
Canada, L4W 0B1

Dear students,

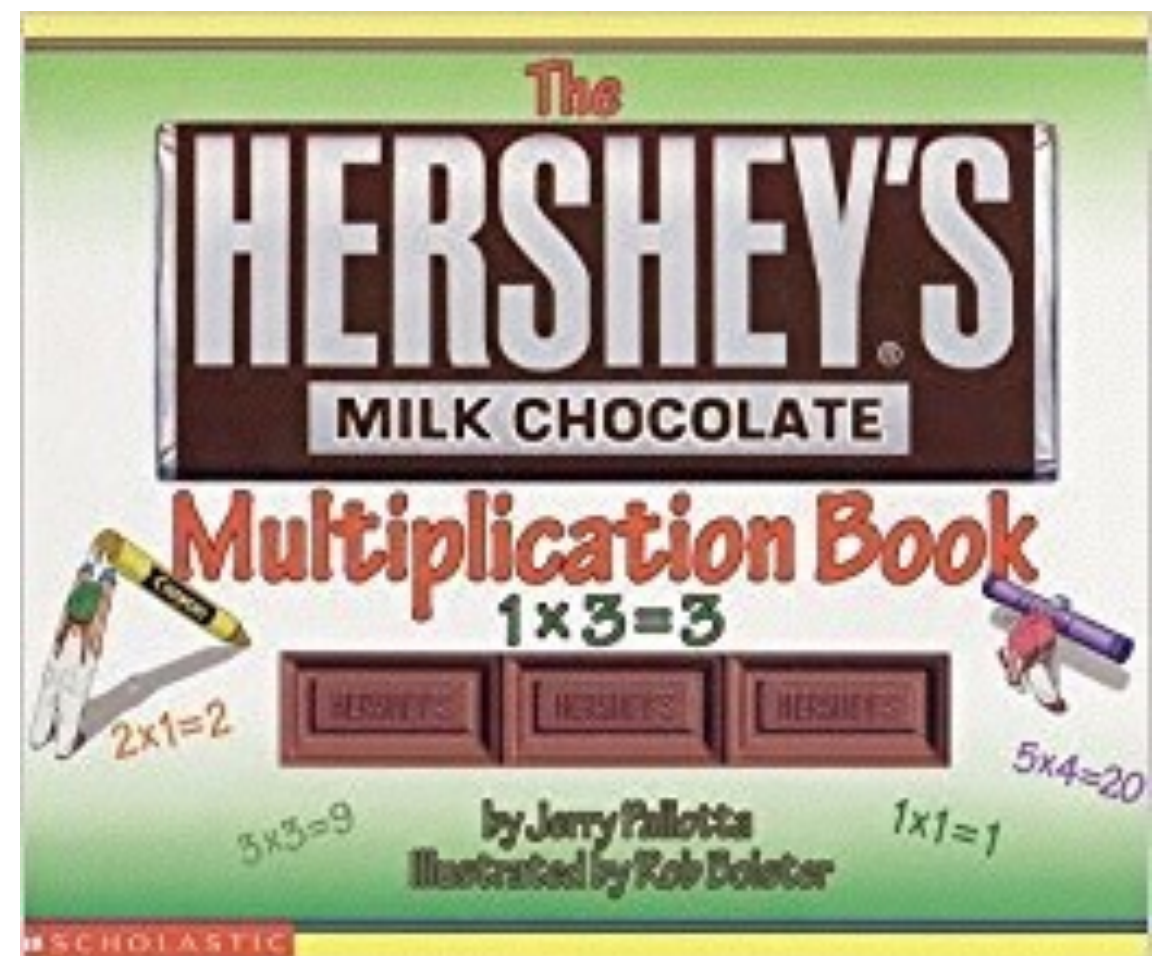
My name is John Bilbrey. I am the President of Hershey's Canada. This spring Hershey's will be making some new chocolate bars. We have 5 different bars coming out. Below is the amount of chocolate squares in each bar.

6 squares  
12 squares  
18 squares  
24 squares  
36 squares

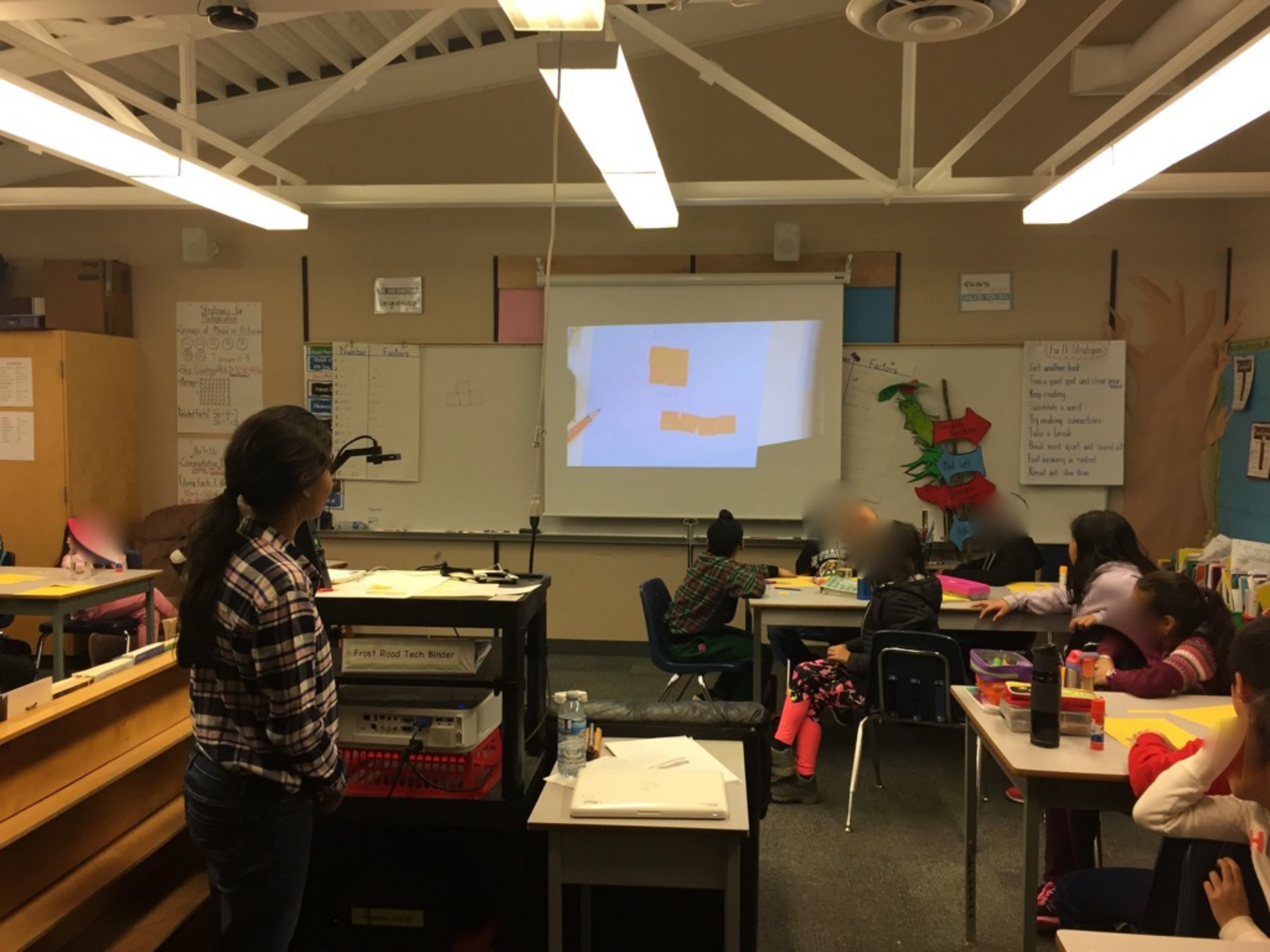
Since we know that children love chocolate bars, can you help us to determine how we should package these new bars?

I look forward to see your pictures and hearing your thinking.  
Regards,

John Bilbrey  
CEO Hershey's Canada

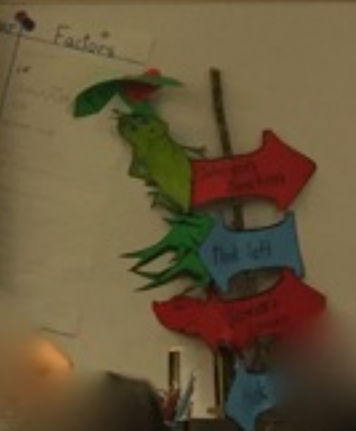
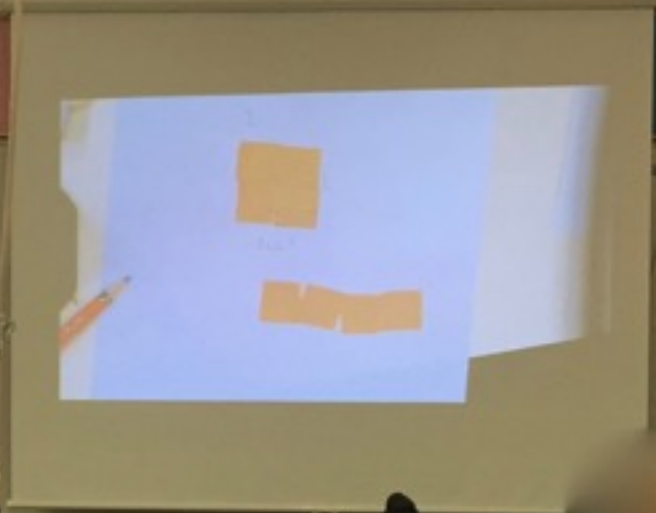






Strategies for  
Multiplication  
Groups of Model in Picture  
7 groups of 8  
8 groups of 7  
8 groups of 8  
8 groups of 9  
8 groups of 10  
8 groups of 11  
8 groups of 12  
8 groups of 13  
8 groups of 14  
8 groups of 15  
8 groups of 16  
8 groups of 17  
8 groups of 18  
8 groups of 19  
8 groups of 20

Number	Factors
2	1, 2
3	1, 3
4	1, 2, 4
5	1, 5
6	1, 2, 3, 6
7	1, 7
8	1, 2, 4, 8
9	1, 3, 9
10	1, 2, 5, 10
11	1, 11
12	1, 2, 3, 4, 6, 12
13	1, 13
14	1, 2, 7, 14
15	1, 3, 5, 15
16	1, 2, 4, 8, 16
17	1, 17
18	1, 2, 3, 6, 9, 18
19	1, 19
20	1, 2, 4, 5, 10, 20



Fix It Strategies  
Get another book  
Find a good spot and clear your space  
Keep reading  
Substitute a word  
Try making connections  
Take a break  
Break word apart and sound it out  
Find meaning in context  
Read and slow down

Frost Road Tech Binder

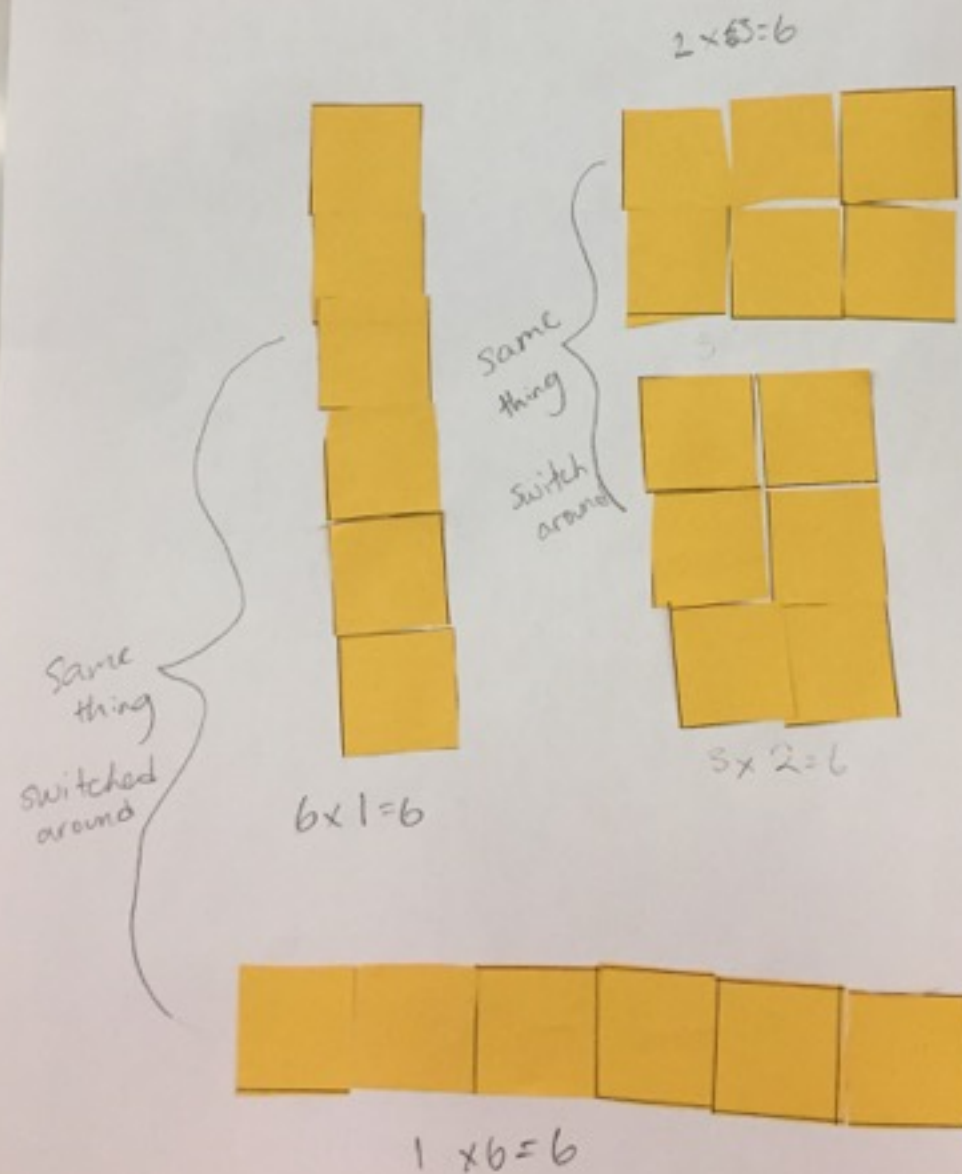


MEMO: 6 squares

Dear Hershey's President,

We found 4 ways but 2 of the ways are switched around which would be the same thing. I would prefer the 3x2 Hershey's bar because it's easier to eat.

Sincerely, Bernice & Amisha



MEMO: 1

Dear Hershey's

We have  
chocolate  
can they

Sincerely,



# COMMUTATIVE PROPERTY

The order of the factors does not matter -  
the product is still the same!

$$6 \times 4 = 4 \times 6$$

$$24 = 24$$



Diminish consciousness of self

Improvisational potential

Continuation Desire



MEMO: 17 squares

Dear Hershey's President,

We found 1 way to wrap a  
17 square chocolate bar. We  
prefer the only way which is  
17 by 1.

Sincerely,





### Multiplication:

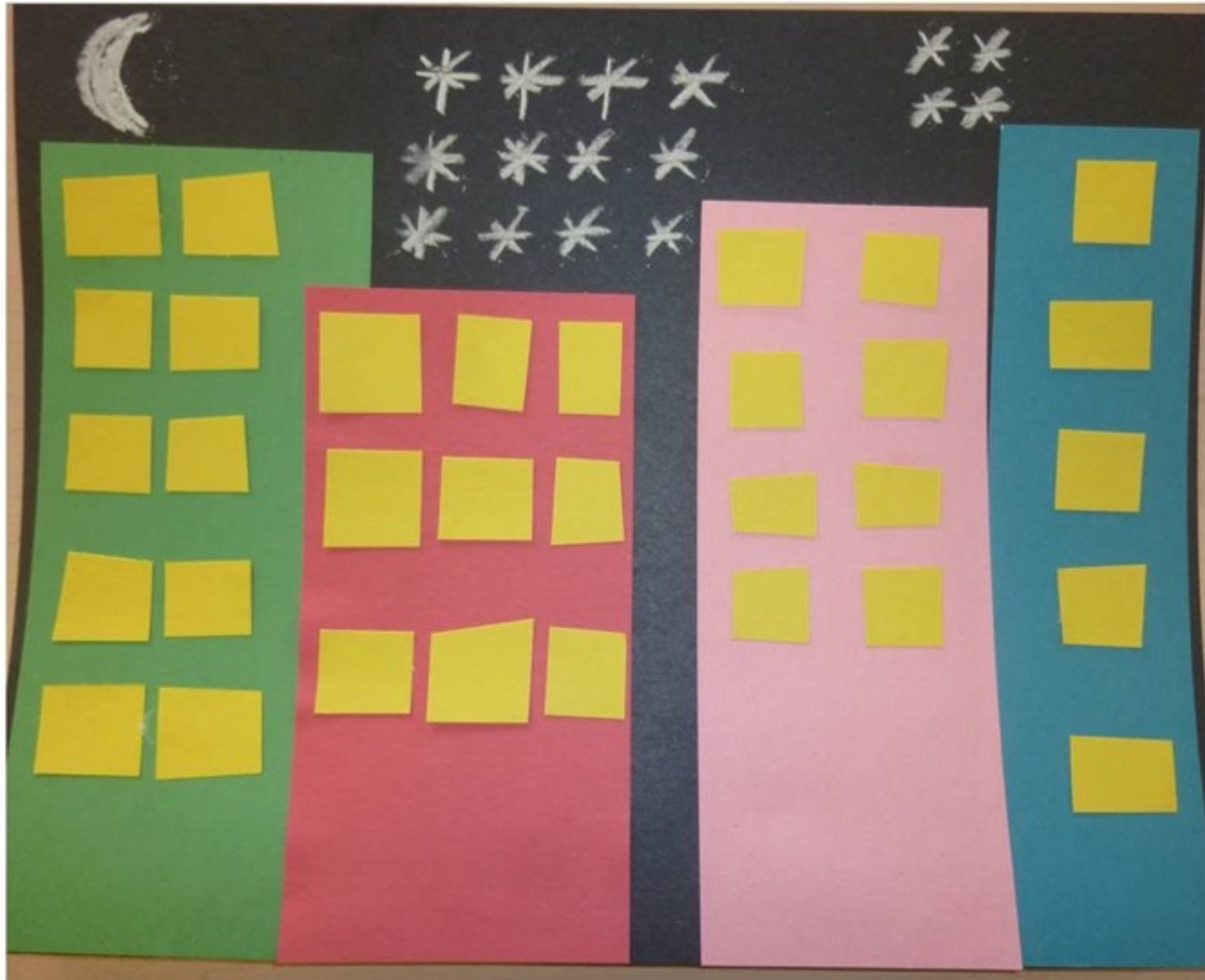
How do squares and rectangles help you to think about your question?



$$5 \times 7 =$$



Can you create some of the arrays you might see at night in the city?





### Multiplication:

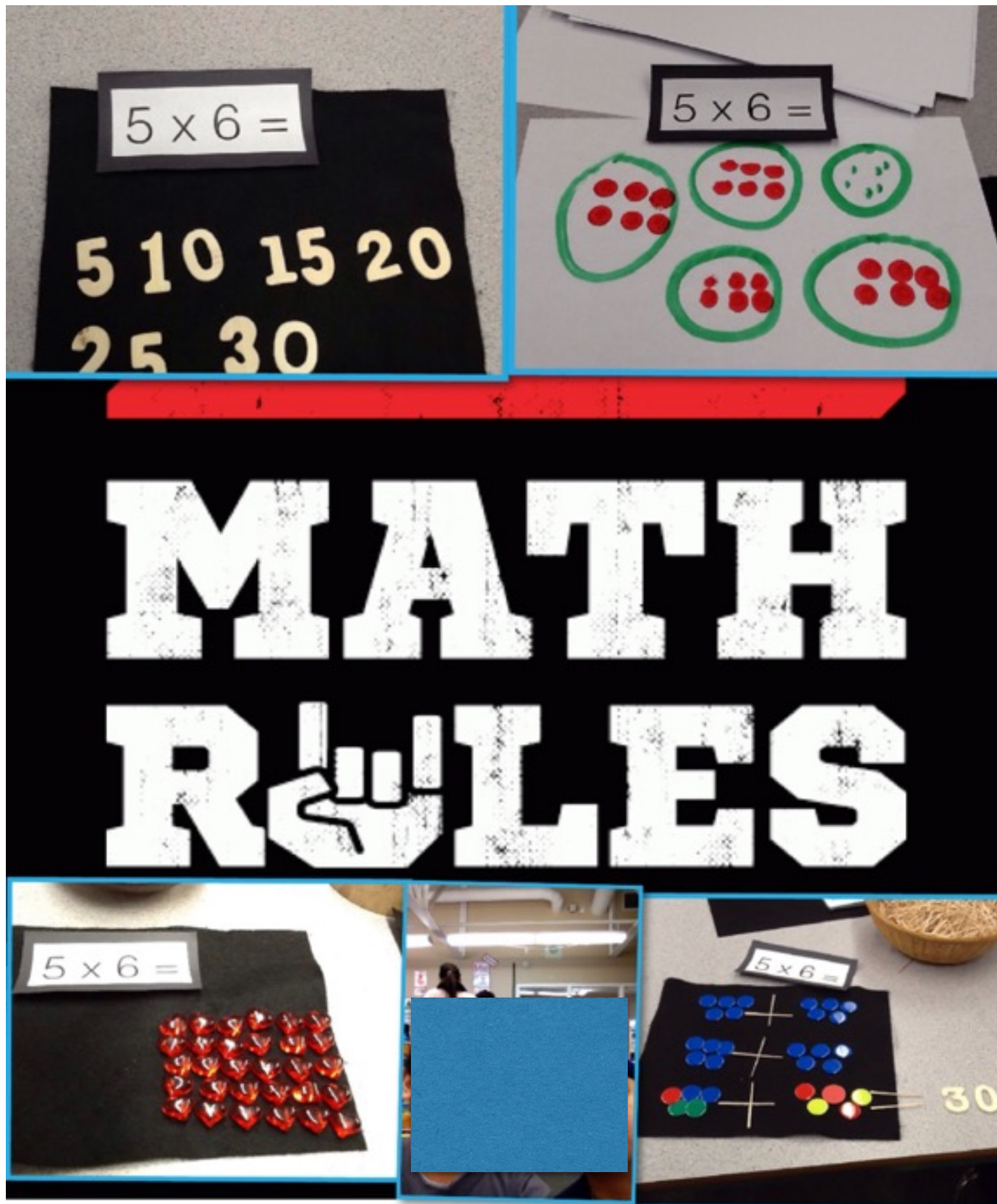
Fish like to swim in schools (groups)  
Pick a number of fish. How many  
different equal groups can be made  
from your fish?

$$10 \div 2$$
$$5 \div 4$$



$$10 \div 2$$

20  
10 x 2  
2 x 10  
4 x 5  
5 x 4



How many  
different ways  
can you  
represent your  
question?



Using a fact they know  
and compensating.

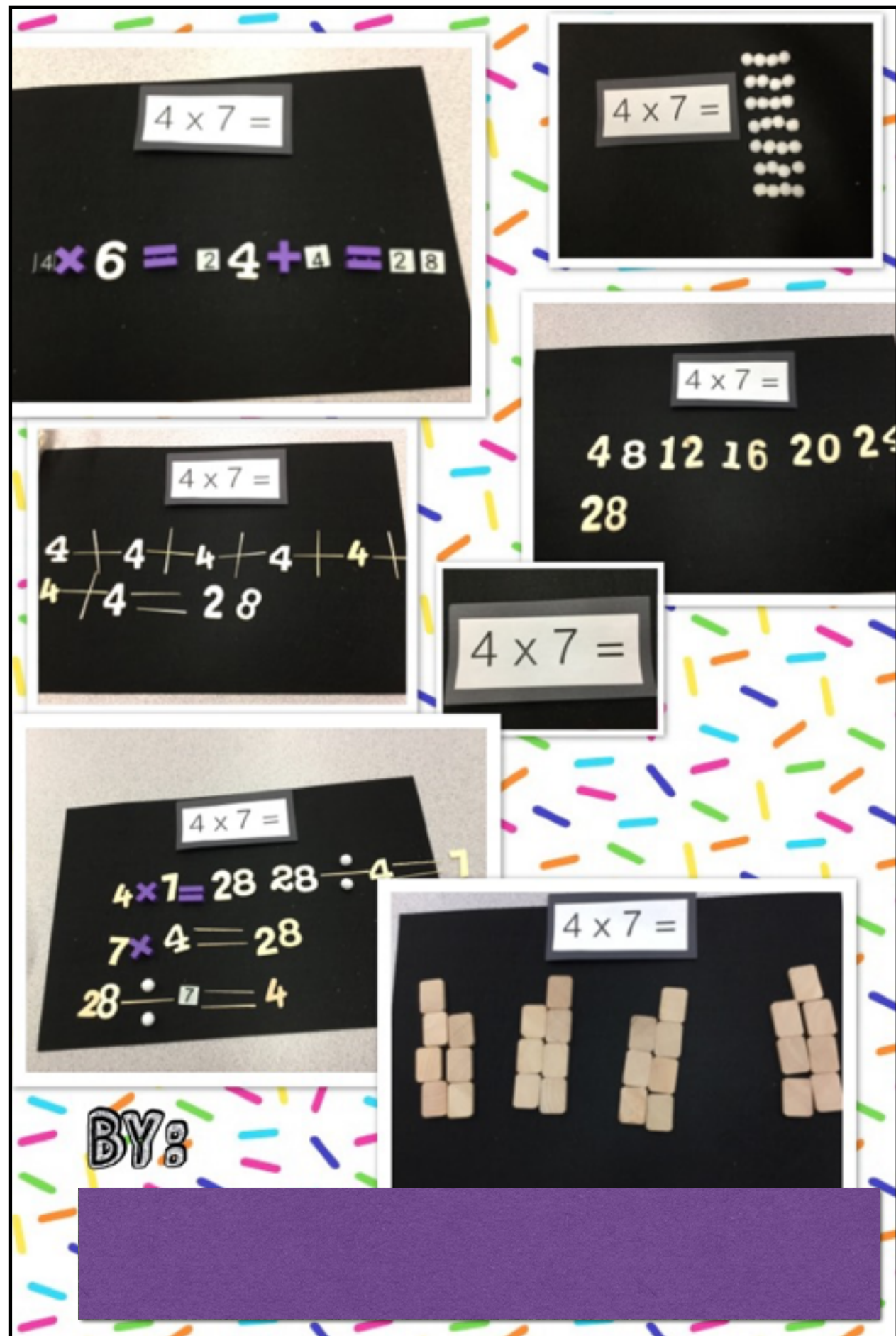
## Representing with arrays

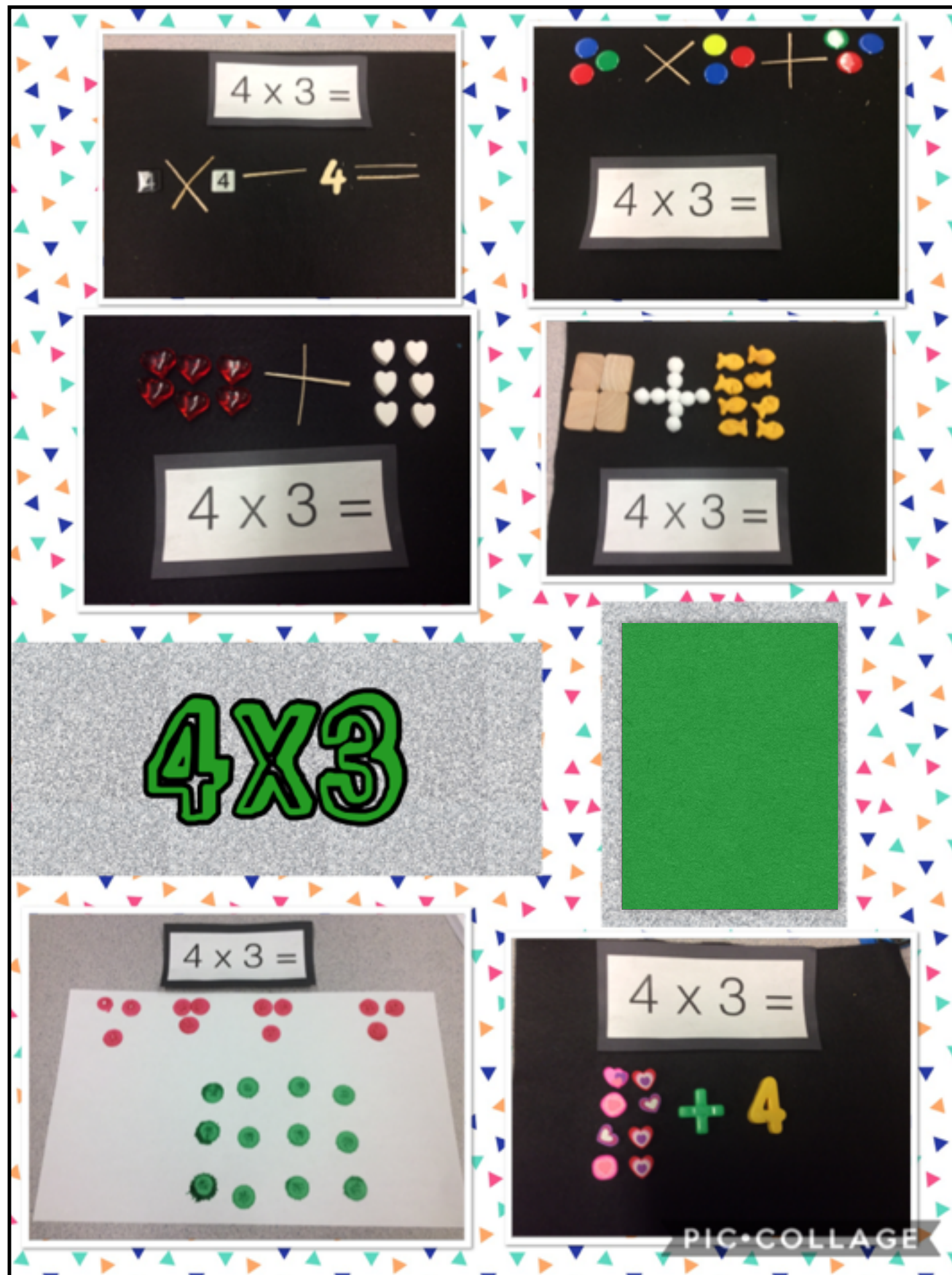
## Connection to repeated addition

## Applying skip counting

# Representing groups of

# Connection to division and related facts





Take a close look at their work. Are they representing their question or showing different ways to make 12? What questions might you ask these students?



What happens when you multiply  
an even # x even #  
or and odd # x odd #  
or an even # x odd #?

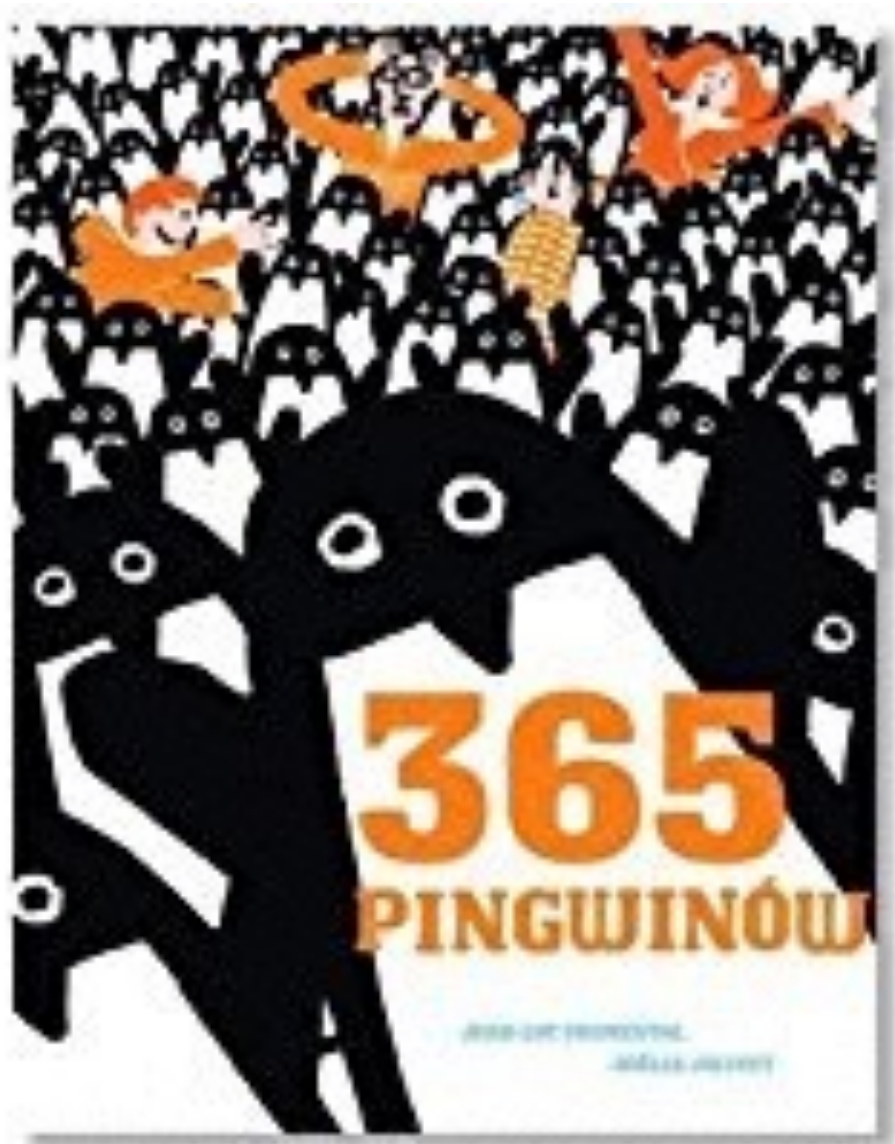
Ex.

①  $4 \times 4 = 16$

②

$$4 + 4 + 4 + 4$$

Can you arrange \_\_\_\_ penguins into equal groups?  
Can you describe the ways using multiplication?  
How is this related to division?



What materials might  
you provide?



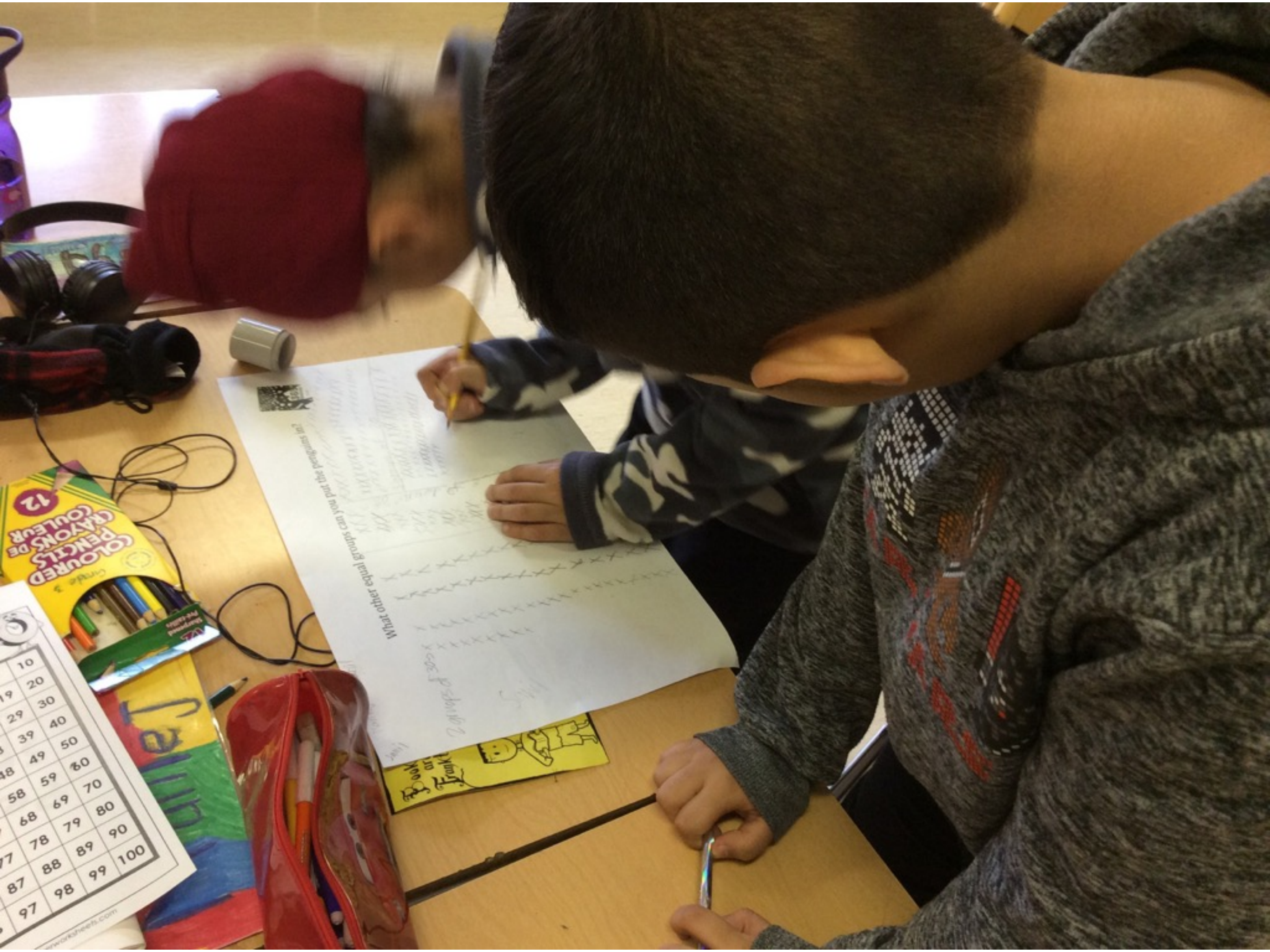
What other equal groups can you put the penguins in?



of ten.







10		
19	20	
29	30	
39	40	
48	49	50
58	59	60
68	69	70
77	78	79
87	88	89
97	98	99
		100



What other equal groups can you put the penguins in?



20  
XXXXXX  
XXXXXX  
XXXXXX

20  
XXXXXX  
XXXXXX  
XXXXXX



+



=



=



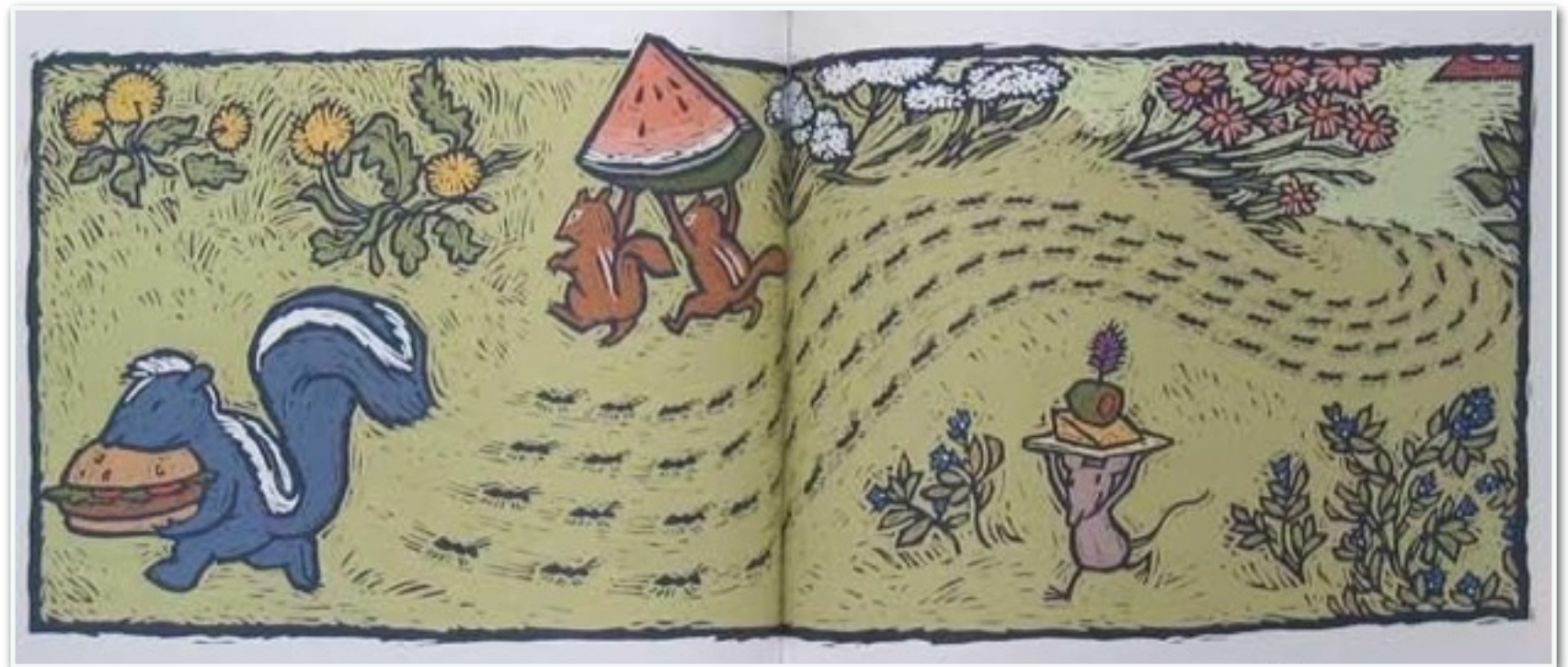
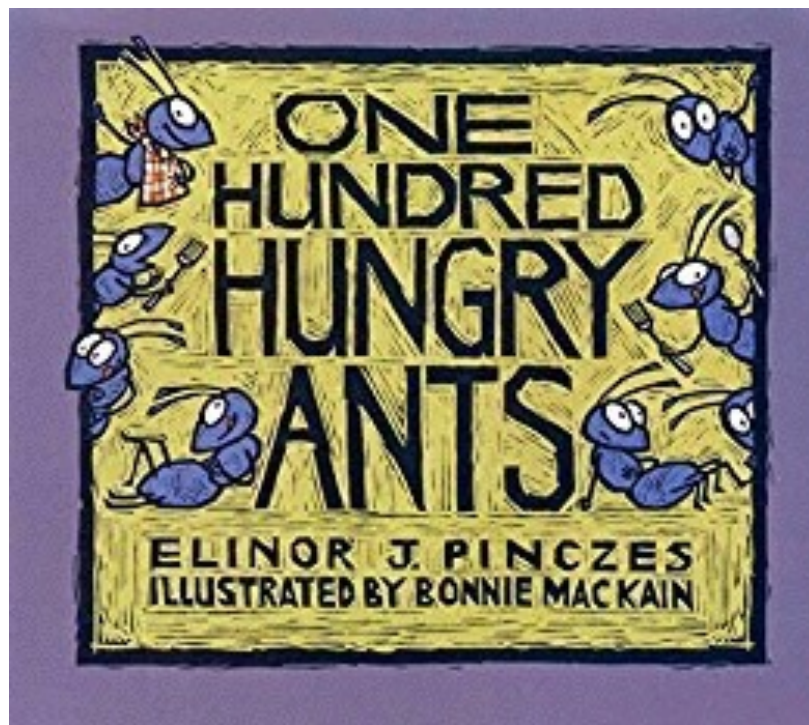




**Hundreds Chart**

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100





“Mathematizing a read-aloud provides students with opportunities to learn mathematical concepts in meaningful contexts. Using literature to connect concepts with students’ experiences helps foster understanding and motivates students to learn.”

~ Hintz and Smith (2013) Mathematizing Read-Alouds

1 line	$1 \times 100 = 100$	$100 \times 1$
2 lines	$2 \times 50 = 100$	
<del>3 lines</del>	$33 \mid 33 \mid 33$	remainder 1
4 lines	$4 \times 25 = 100$	$25 \times 4$
5 lines	$5 \times 20 = 100$	$20 \times 5$
10 lines	$10 \times 10 = 100$	$4 \div 1 = 4$



What are all the possible ways that 99 ants can line up equally?

22, 33, 44, 55, 66, 77, 88, 99

$99 \div 3 = 33$

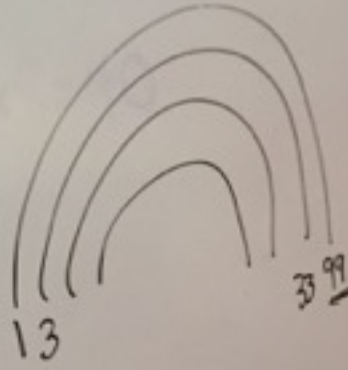
$33 + 33 + 33 = 99$   
Repeated Addition

$3 \times 33 = 33 + 33 + 33$

$33 \times 3$

Identity Element

$1 \times 99 = 99$   
 $99 \times 1 = 99$  } Commutative Property



$$1 \times 99$$

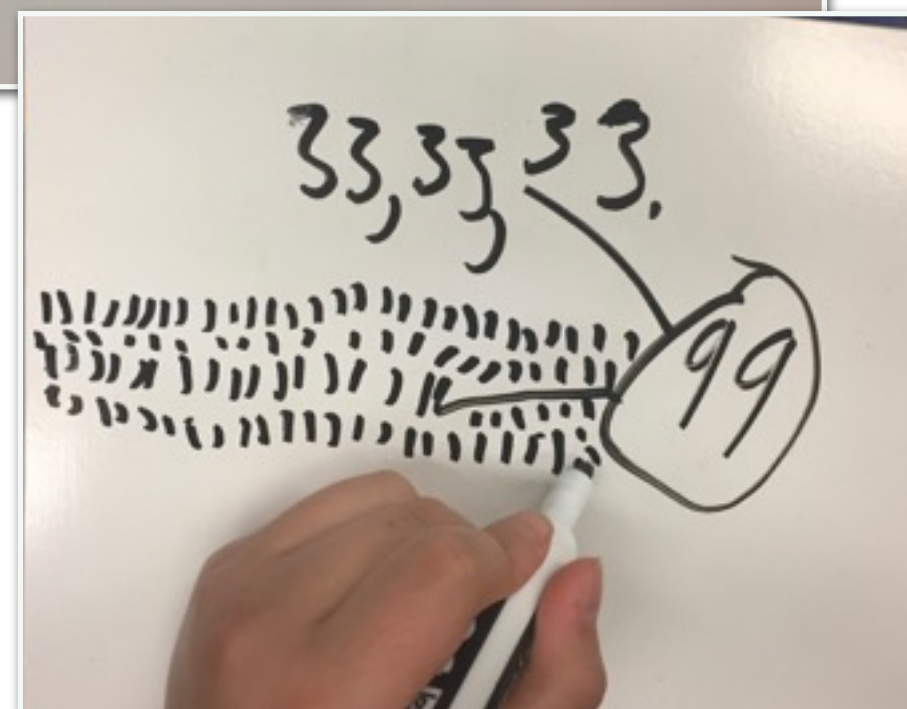
$$9 \times 11$$

$$3 \times 33$$

$$33 \times 3$$

$$11 \times 9$$

$$99 \times 1$$





Number	Factors
30	1, 2, 3, 5, 6, 10, 15, 30
31	1, 31
32	1, 2, 4, 8, 16, 32
33	1, 3, 11, 33
34	1, 2, 17, 34
35	1, 5, 7, 35
36	1, 2, 3, 4, 6, 9, 12, 18, 36
37	1, 37
38	1, 2, 19, 38
39	1, 3, 13, 39
40	1, 2, 4, 5, 8, 10, 20, 40
41	1, 41
42	1, 2, 3, 6, 7, 14, 21, 42
43	1, 43
44	1, 2, 4, 11, 22, 44

What do you notice about the information?

What do you notice about the even numbers? The odd numbers?

Why do numbers have different factors?

What about the numbers that only have 2 factors. Why might that be?

# How do we assist students in using multiplicative thinking to solve single and multi-digit multiplication questions.

- Using known facts and compensating
- Doubling and Halving
- Making landmark or friendly numbers
- Using the commutative property
- Using the distributive property
- Using the associative property



# How does halving and doubling help you solve a question you don't know?

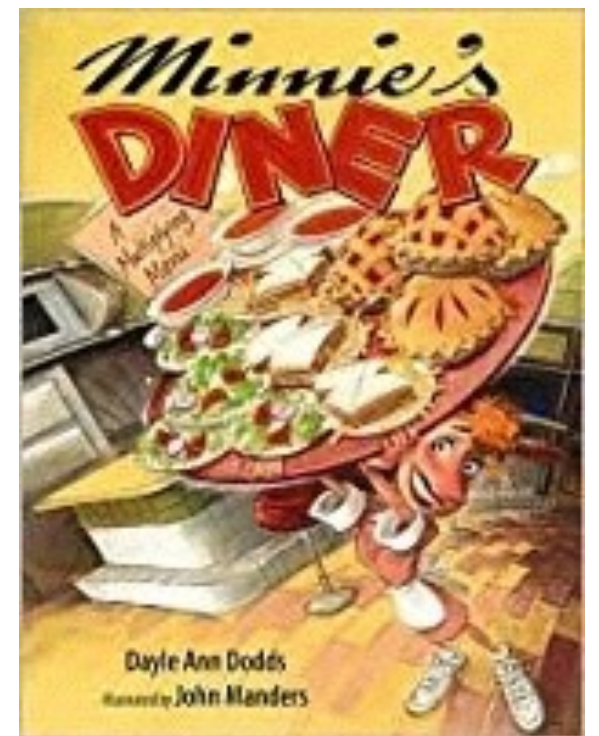
What do you notice is happening?

Let's record what each brother ordered?

How could we describe this using multiplication?

How many dishes did Minnie use for \_\_\_\_\_'s meal?

How many dishes did Minnie use to feed all the brothers?



# Multiplication:

How can you use Cuisenaire rods to represent your question?

$$6 \times 17 =$$

$$3 \times 6 =$$

$$6 \times 18 =$$

1 way

$$6 \times 18$$
$$6 \times (10 + 8)$$
$$(6 \times 10) + (6 \times 8) = 108$$

2 way OR

$$6 \times 18$$
$$6 \times (9 \times 2)$$
$$(6 \times 9) + (6 \times 9) = 108$$



$$6 \times 18 =$$



1 way

$$6 \times 18 =$$

$$6 \times (10 + 8)$$

$$\underset{60}{(6 \times 10)} + \underset{48}{(6 \times 8)} = 108$$

2 ways

OR

$$6 \times 18$$

$$6 \times (9 + 9)$$

$$\underset{54}{(6 \times 9)} + \underset{54}{(6 \times 9)} = 108$$

# DISTRIBUTIVE PROPERTY

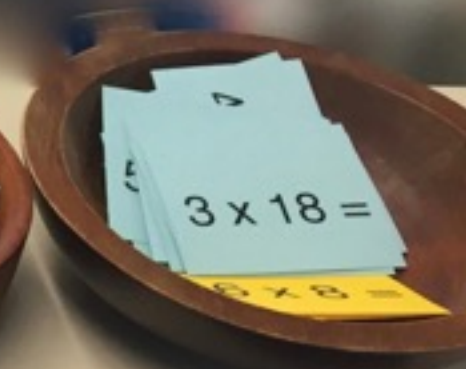
You can break a factor up and distribute the multiplication across both factors!

$$\begin{aligned} 2 \times 33 &= 2 \times (30 + 3) \\ &= (2 \times 30) + (2 \times 3) \\ &= 60 + 6 = 66 \end{aligned}$$



## Multiplication:

How can you represent your question using ten frames?

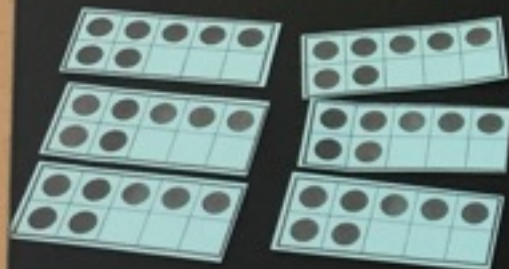


$$6 \times 7 = 42$$
$$(6 \times 5) + (6 \times 2) = 42$$

30      12

$$7 \times 7 = 49$$
$$7 \times 6 = 42$$
$$7 \times 5 = 35$$
$$7 \times 4 = 28$$
$$7 \times 3 = 21$$
$$7 \times 2 = 14$$
$$7 \times 1 = 7$$
$$30 + 12 = 42$$

$$6 \times 7 =$$



$$2 \times 18 =$$



# Multiplication:

How can you represent your question using base 10 blocks?

$$3 \times 12 =$$

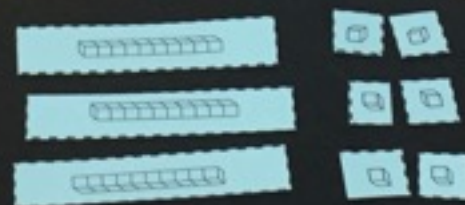
$$\begin{array}{r} 12 \\ \text{Break Factor into two} \\ 10 \quad 2 \\ 3 \quad 30 \quad 6 \end{array}$$

$$\frac{3}{(3 \times 10)} \times (\frac{10}{+} \frac{2}{}) =$$

$$(3 \times 10) + (3 \times 2) = 36$$

$$4 \times 12 =$$

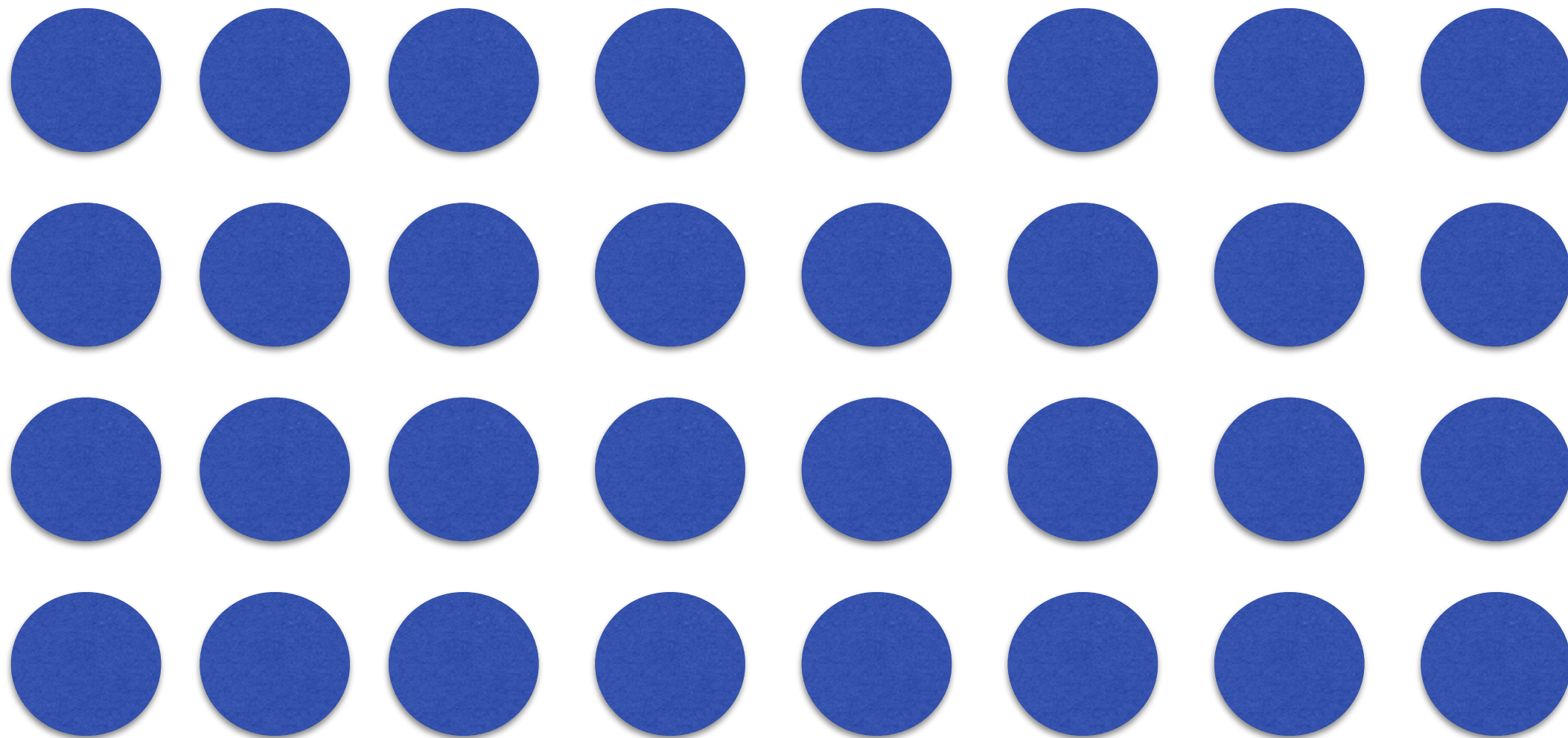
$$\begin{array}{l} \_\_\_ \times (\_\_\_ + \_\_\_) = \\ (\_\_\_ \times \_\_\_) + (\_\_\_ \times \_\_\_) = \end{array}$$





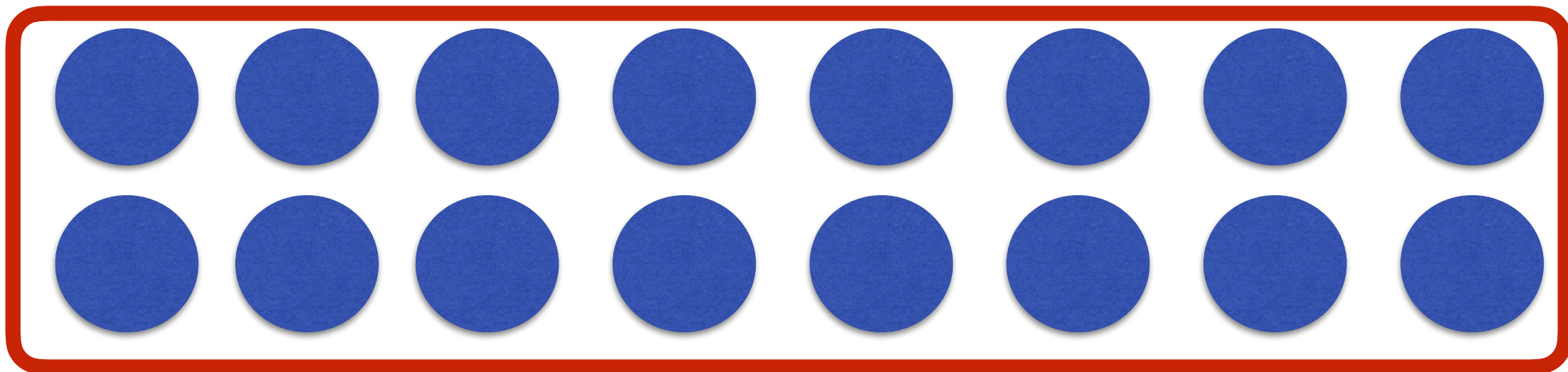
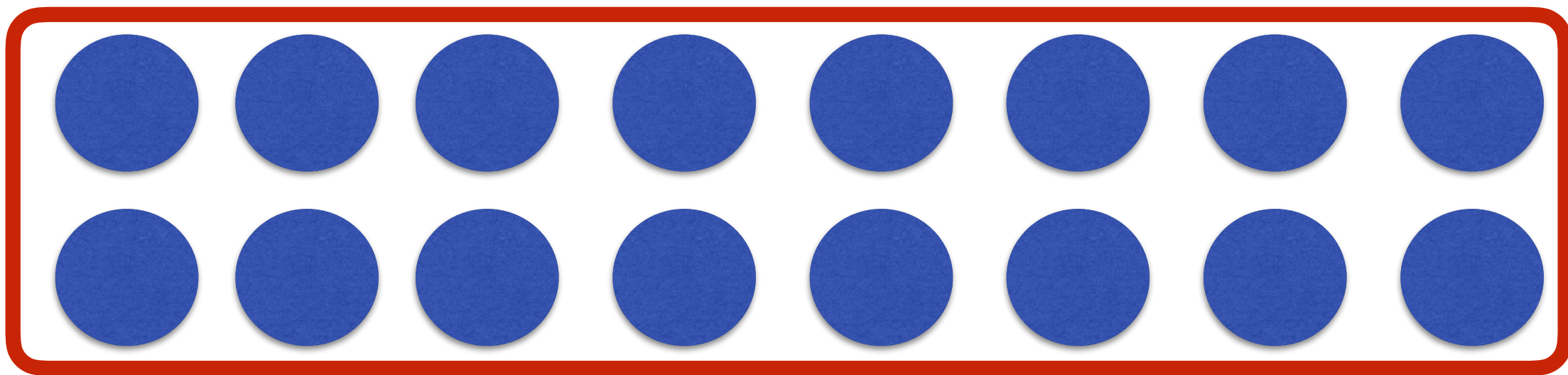
How does halving and doubling help you solve a question you don't know?

$$4 \times 8 =$$



How does halving and doubling help you solve a question you don't know?

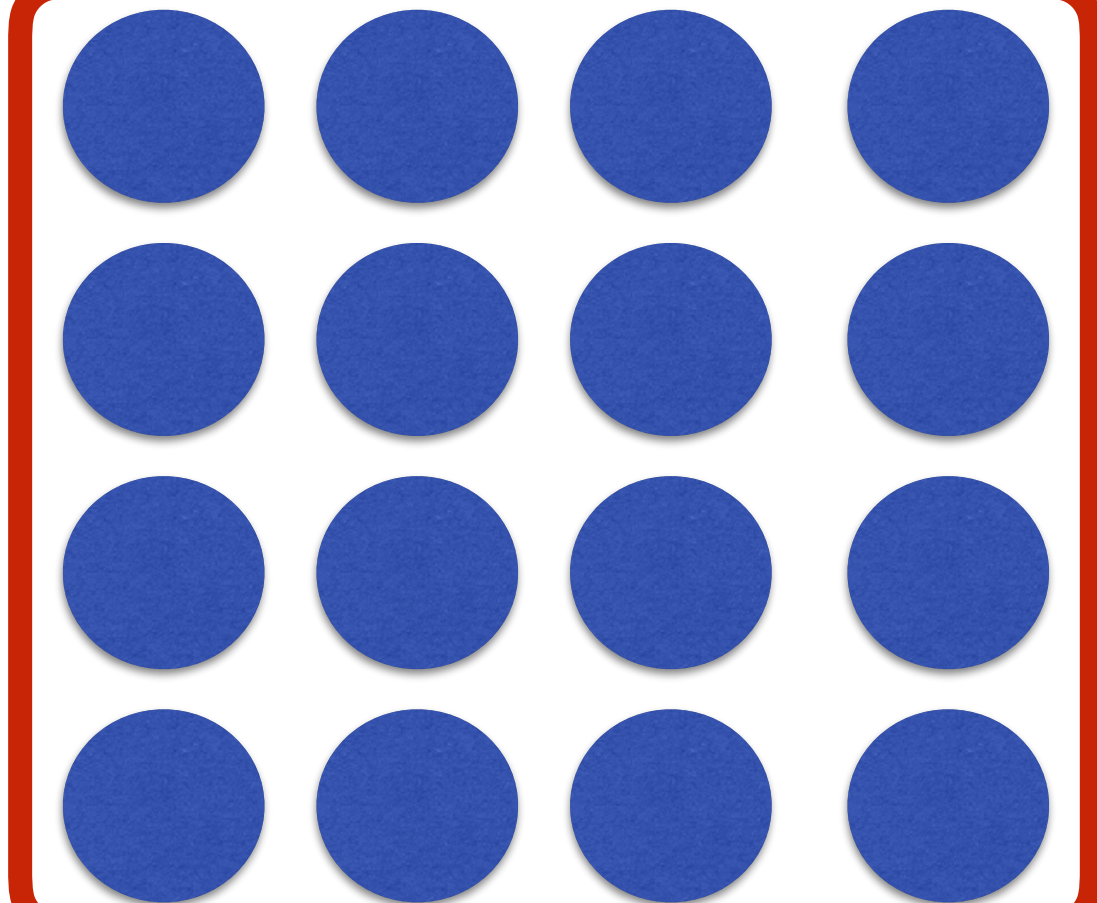
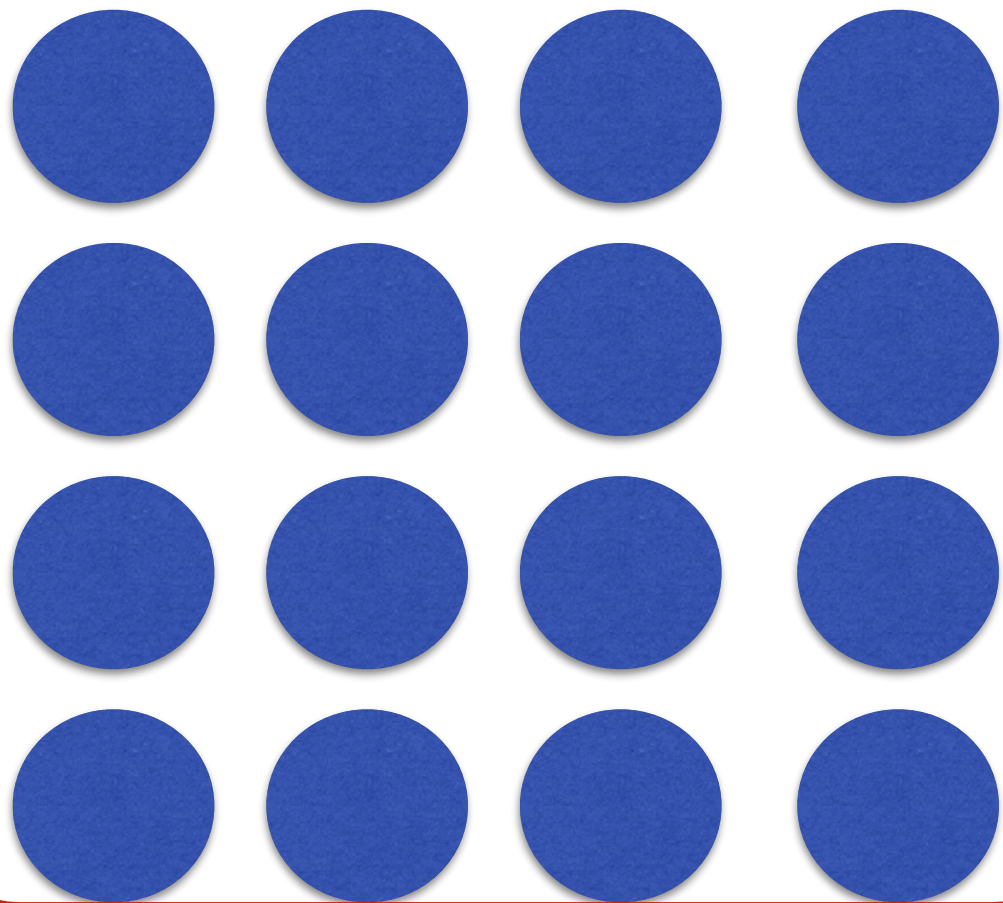
$$4 \times 8 = 2 \times (2 \times 8)$$





How does halving and doubling help you solve a question you don't know?

$$4 \times 8 = 2 (4 \times 4)$$



# ASSOCIATIVE PROPERTY

How you group the factors does not matter - the product is still the same!

$$(6 \times 4) \times 2 = 6 \times (4 \times 2)$$

$$24 \times 2 = 6 \times 8$$



$$48 = 48$$



# How can you use facts you know to help you solve a question you don't know?

<https://www.mathlearningcenter.org/resources/apps>

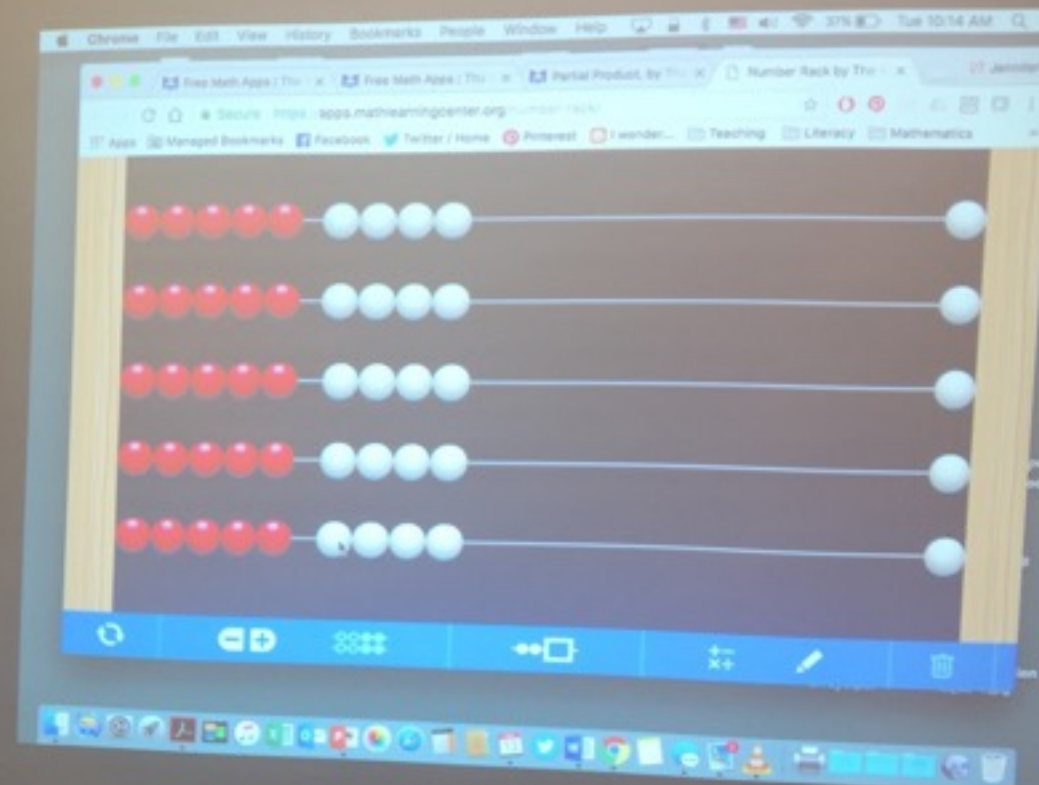
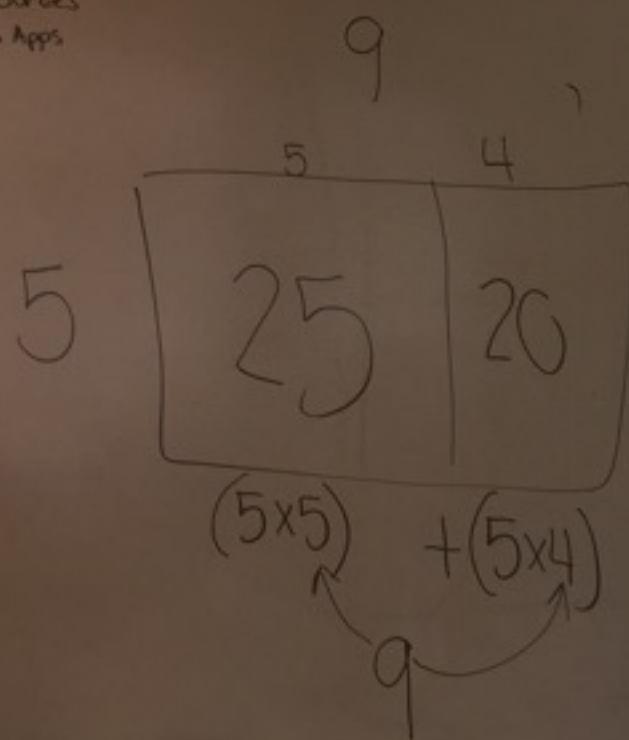


Open Web App  
[Apple App Store](#)   
[Chrome Store](#) 

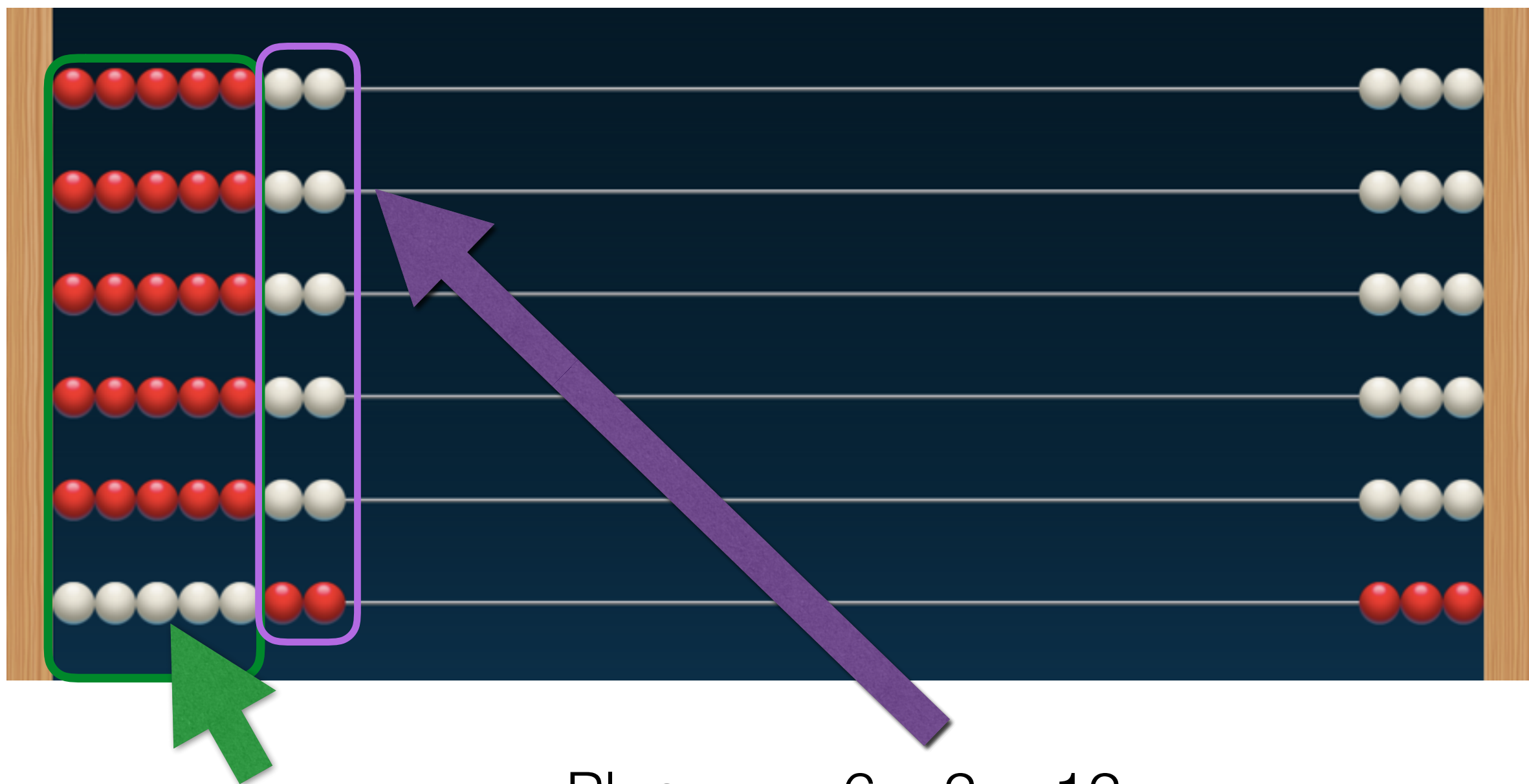
## Number Rack

Number Rack facilitates the natural development of children's number sense. Rows of movable, colored beads encourage learners to think in groups of fives and tens, helping them to explore and discover a variety of addition and subtraction strategies. Free activities and free book available.

Resources  
Math Apps







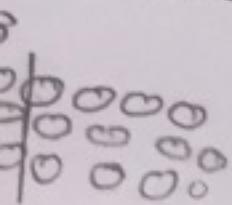
$$6 \times 5 = 30$$

Plus

$$6 \times 2 = 12$$

$$30 + 12 = 42$$

How can you use facts you know to help you solve questions you don't know?



$$(3 \times 5) + (3 \times 3) =$$

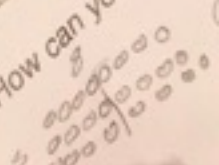
30

$$8 \times 3 =$$

$$(4 \times 3) + (4 \times 3) = 8 \times 3$$



How can you use facts you know to help you solve questions you don't know?

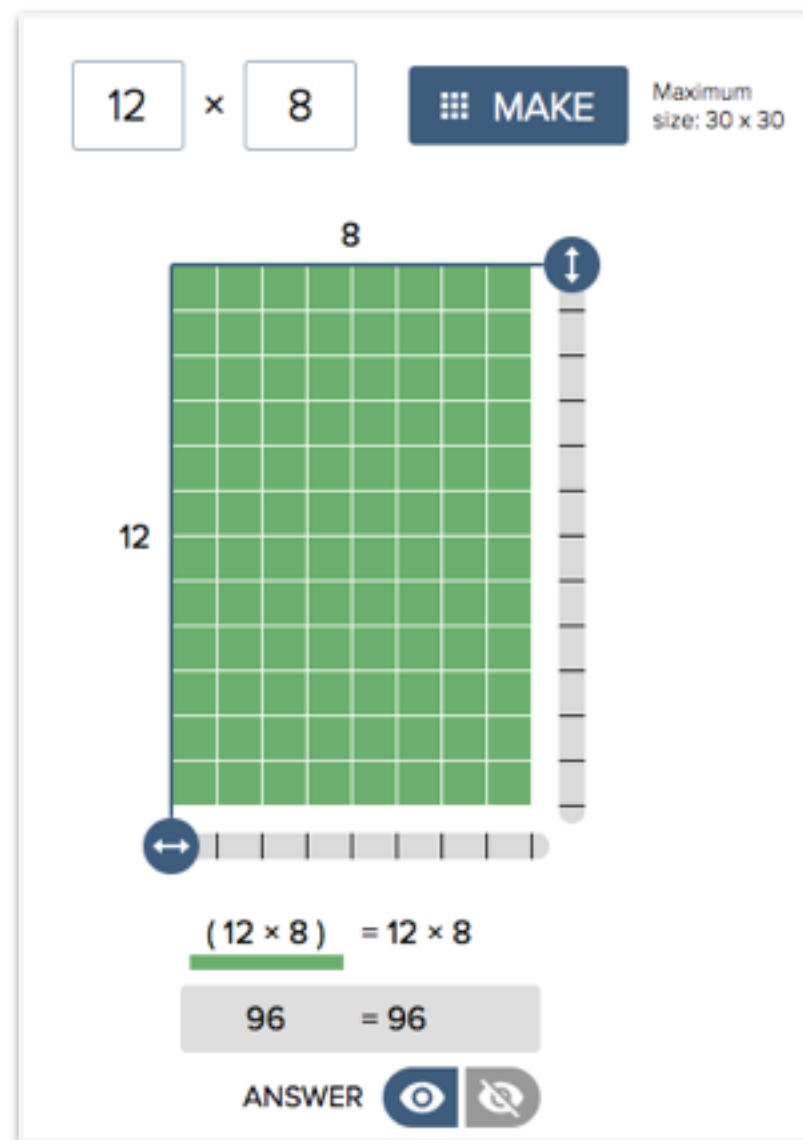




Children have real understanding only of that which they invent themselves, and each time that we try to teach them too quickly we keep them from reinventing it themselves.

- Piaget

How can you use facts you know to help you solve a question you don't know?



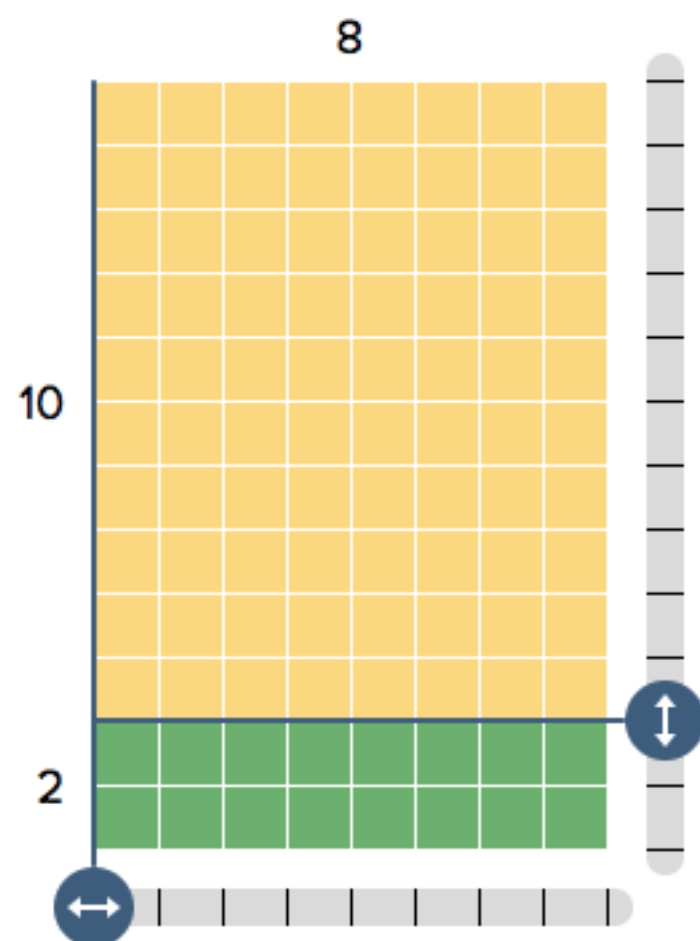
<https://www.mathlearningcenter.org/resources/apps>



12

×

8

 MAKEMaximum  
size: 30 x 30

$$(10 \times 8) + (2 \times 8) = 12 \times 8$$

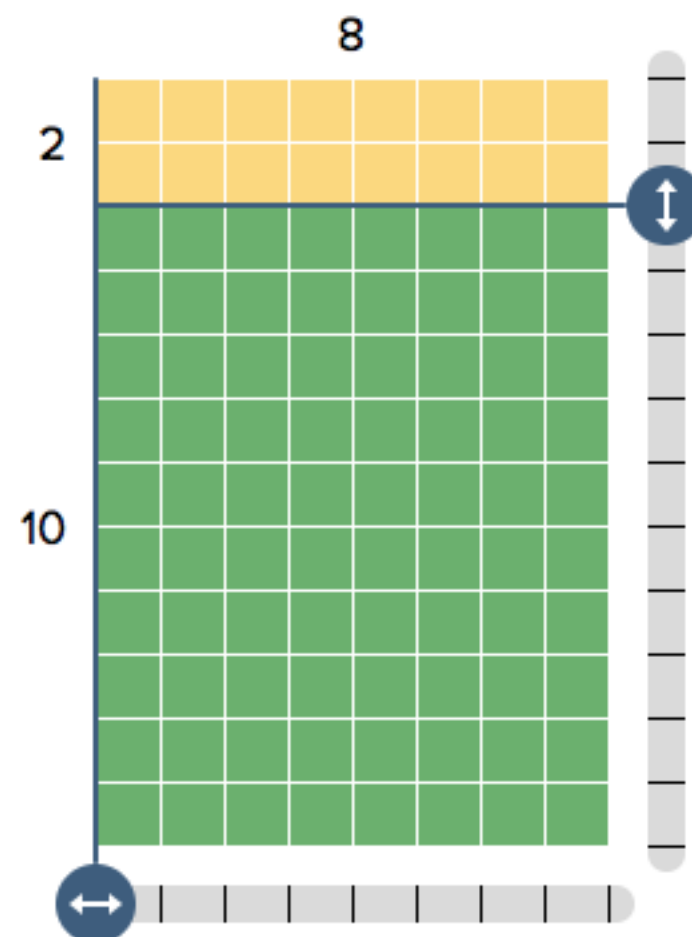
ANSWER



12

×

8

 MAKEMaximum  
size: 30 x 30

$$(2 \times 8) + (10 \times 8) = 12 \times 8$$

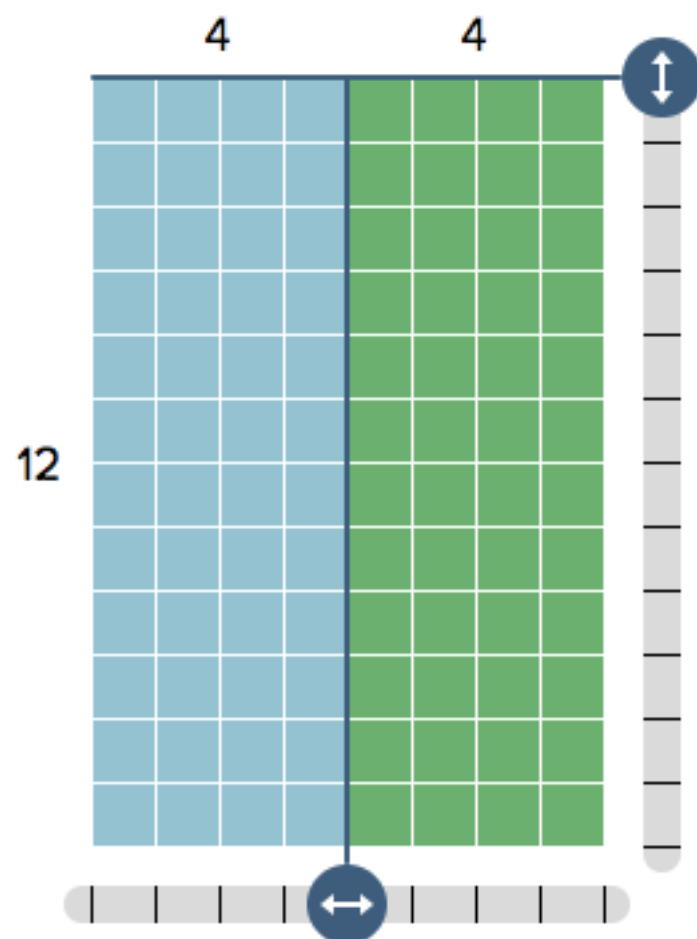
ANSWER



$$12 \times 8$$

 **MAKE**

Maximum  
size: 30 x 30



$$(12 \times 4) + (12 \times 4) = 12 \times 8$$

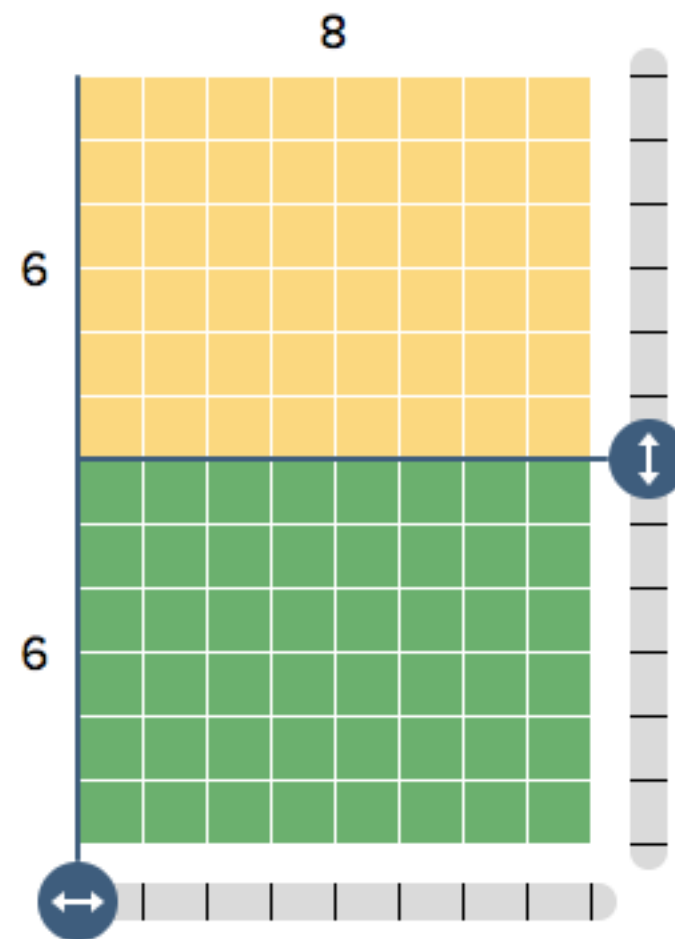
ANSWER



$$12 \times 8$$

 **MAKE**

Maximum  
size: 30 x 30

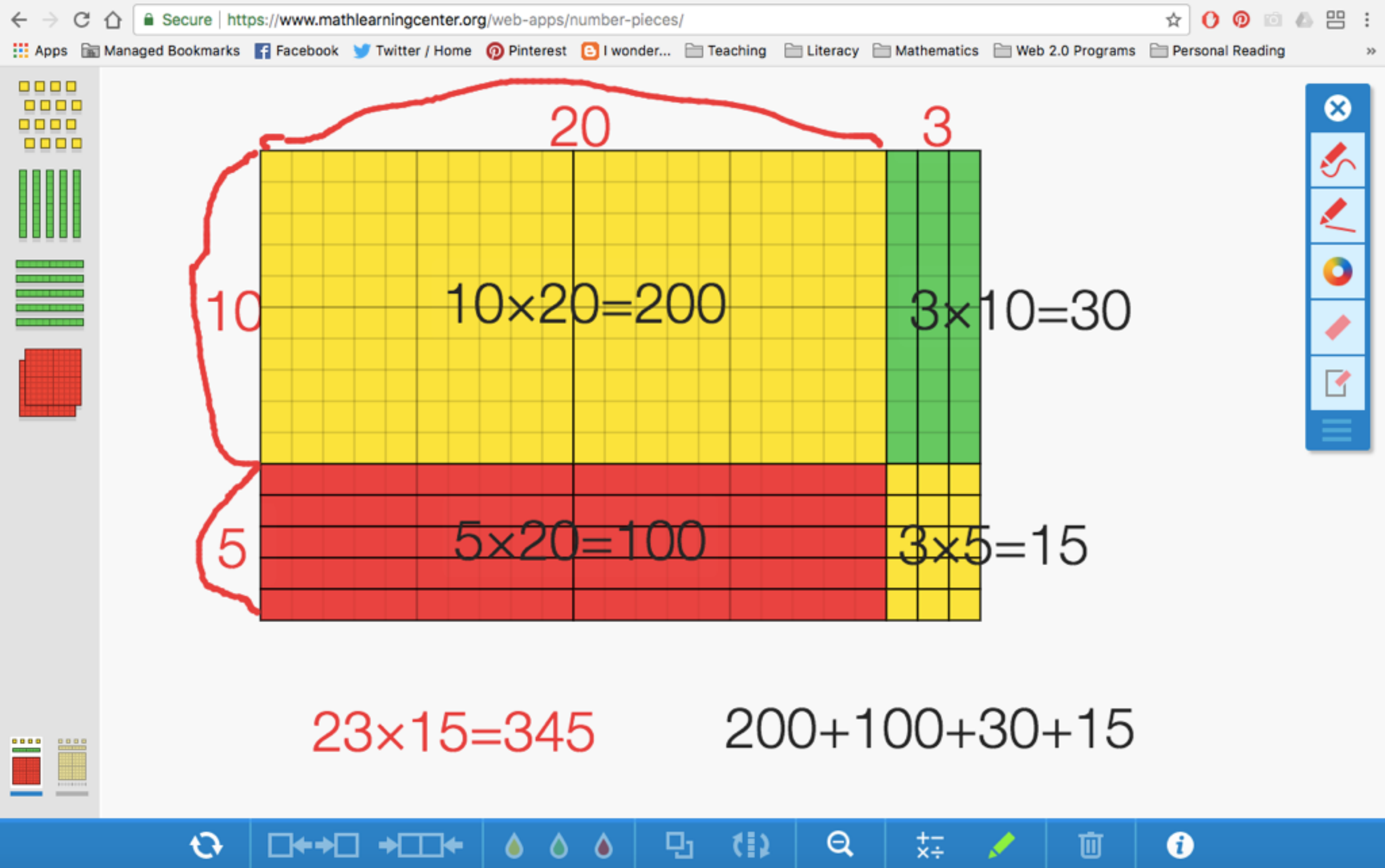


$$(6 \times 8) + (6 \times 8) = 12 \times 8$$

ANSWER







Same site - this is called Number Pieces

# Three Act Tasks

1) The Question, 2) Gathering Information, and 3) The Reveal.

The entire activity typically takes a full math period or the acts can be split up and worked on across multiple days. The goal of the activity is to engage children in asking mathematical questions, identifying information that will allow them to answer the question, developing a mathematical model of the situation, and revising their models to more closely reflect the real world.





# Act One





# Act Two



**There are 58 packages of skittles in the jar.**





# Act Three



“Play is often talked about as if it were a relief from serious learning. But for children play is serious learning. Play is really the work of childhood.”

Fred Rogers



# What is our role in playful inquiry?

- talk less and listen more
- be open to the children's questions
- ask open questions - design inviting, playful learning opportunities
- notice and name the curricular competencies
- ask questions to nudge learning
- use mathematical vocabulary
- build in time to reflect and connect
- know and honour student's interests
- establish a culture that supports wondering and playfulness



# Formative Assessment



We circulate and observe. Based on what we see, we ask questions to clarify our understanding and nudge learning forward.

We document the learning we see using anecdotal notes, photos, videos, checklists, collection of student work samples.



# Performance Based Assessment

Oct. 11/17

Patterns

Grade 3 / Div. 12

2017-18

	Increasing Patterns	Decreasing Patterns	Repeating			
A.	✓					
ad A.	pic X					
t B.						
B.	✓	✓	✓			
B.	✓ can't explain					
y B.	✓ can't explain		✓			
D.	X	X	✓			
D.	✓	✓	✓			
D.	# + colour →	✓				
I.			✓			
h K.	1/2					
a K.			✓			
K.			✓ colour			
A.	✓ ✓		✓ colour			
N.	✓ inc by 1	✓ colour				
R.	✓ ✓					
S. ab.						
S.	✓	✓	↗ ↘			
S.	✓ inc. ✓	✓	✓			
S.						
Y.			✓ colour			

# Journal Prompts

- Multiplication can be represented using
- I created...
- I'm proud of...
- I know...
- I'm thinking now...
- This reminds me of...
- Today I learned...
- A connection I have...
- I noticed...





# Multiplication: How do we revisit this topic throughout the year?

## 2017/18 School Calendar

**Calendar***pedia*  
Your source for calendars

August 2017						
Su	Mo	Tu	We	Th	Fr	Sa
		1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31		

September 2017						
Su	Mo	Tu	We	Th	Fr	Sa
					1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30

October 2017						
Su	Mo	Tu	We	Th	Fr	Sa
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				

November 2017						
Su	Mo	Tu	We	Th	Fr	Sa
			1	2	3	4
5	6	7	8	9	10	11
12	13	14	15	16	17	18
19	20	21	22	23	24	25
26	27	28	29	30		

December 2017						
Su	Mo	Tu	We	Th	Fr	Sa
					1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30
31						

January 2018						
Su	Mo	Tu	We	Th	Fr	Sa
	1	2	3	4	5	6
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30	31			

February 2018						
Su	Mo	Tu	We	Th	Fr	Sa
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28			

March 2018						
Su	Mo	Tu	We	Th	Fr	Sa
				1	2	3
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

April 2018						
Su	Mo	Tu	We	Th	Fr	Sa
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30					

May 2018						
Su	Mo	Tu	We	Th	Fr	Sa
		1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31		

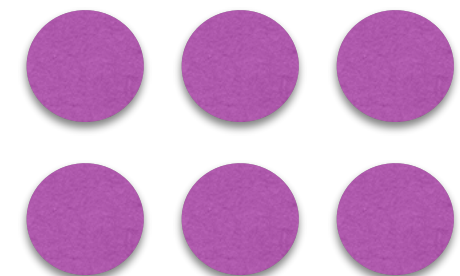
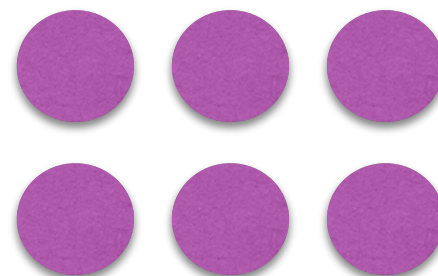
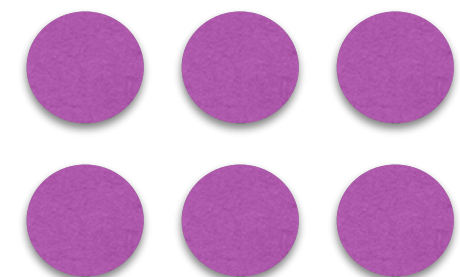
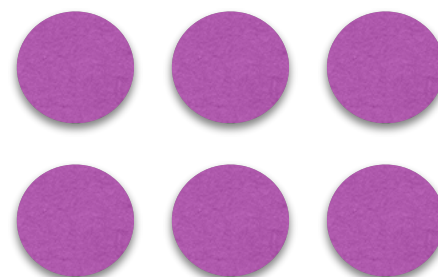
June 2018						
Su	Mo	Tu	We	Th	Fr	Sa
					1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30

July 2018						
Su	Mo	Tu	We	Th	Fr	Sa
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				

# Number Talks Using Quick Images

Learning Intentions:

- develop multiple strategies for Decomposing (Mental Math)
- developing flexibility through use of multiple strategies
- Computational Fluency
- Place Value







How many?

How did you see them?

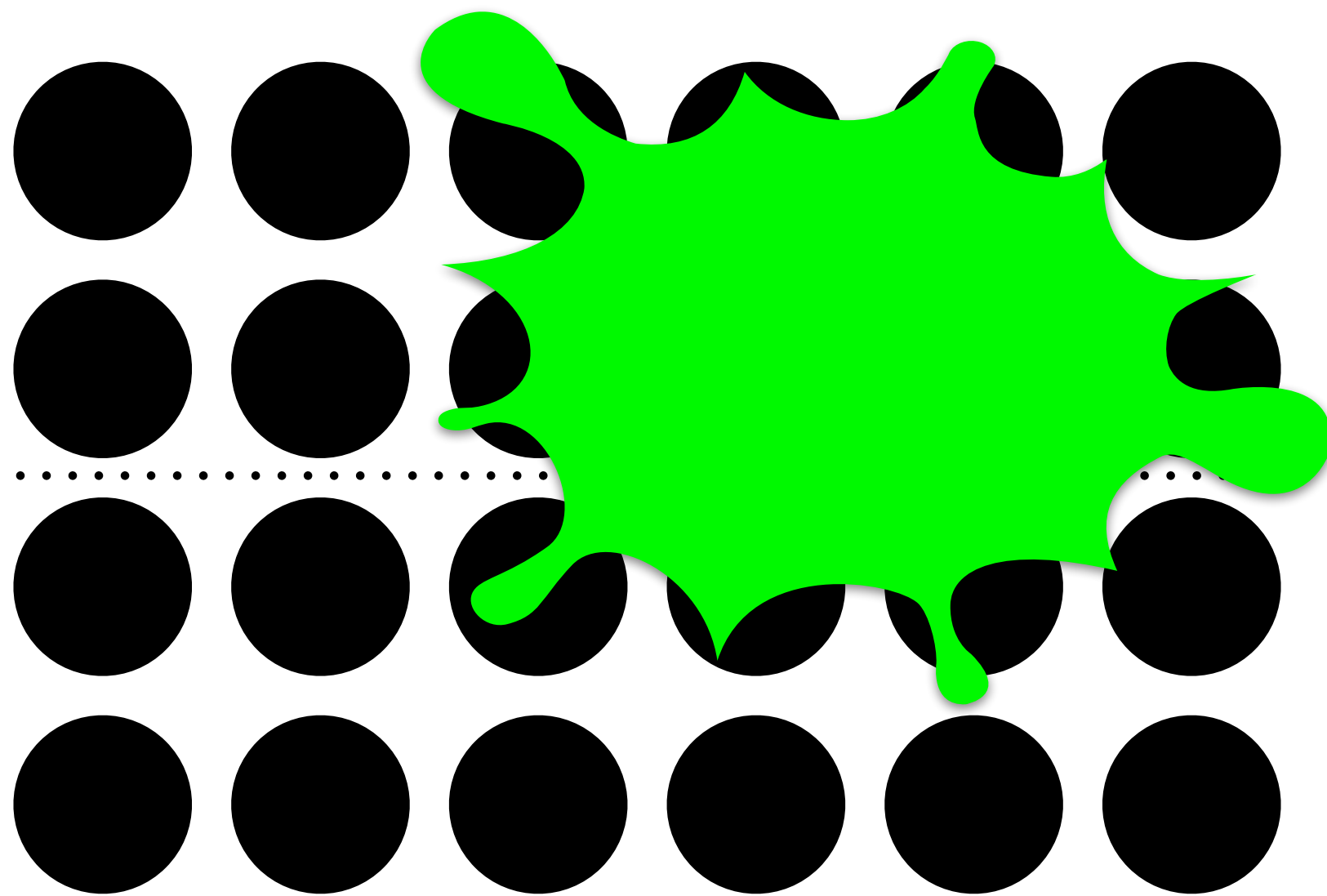


How could we describe this page using multiplication?

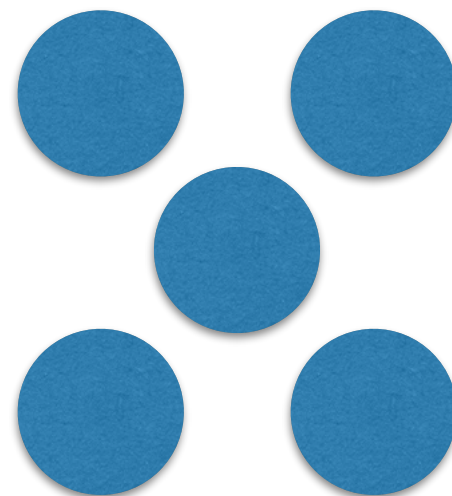
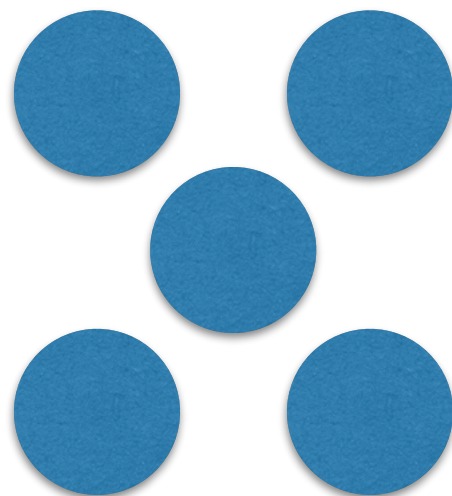
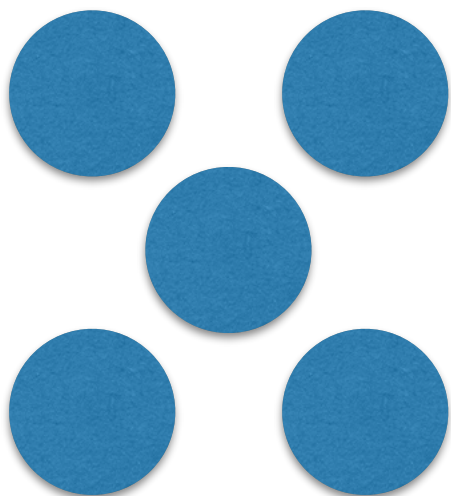
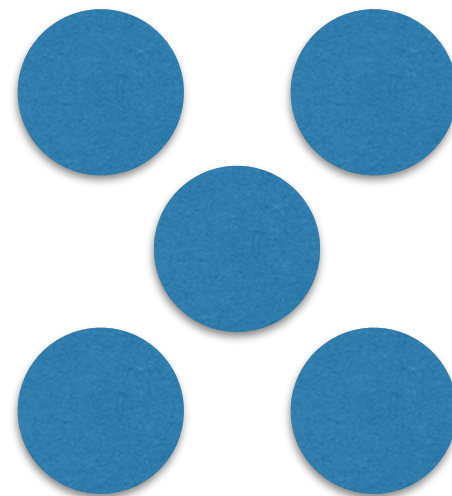
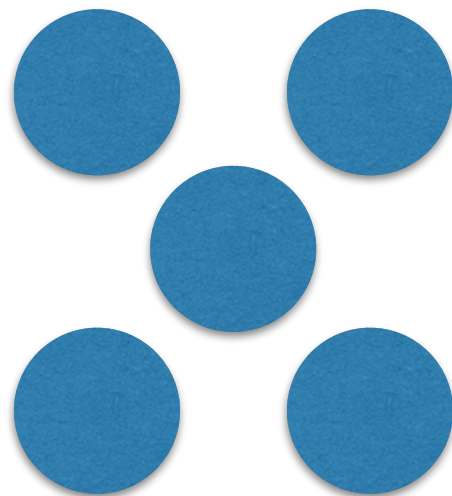
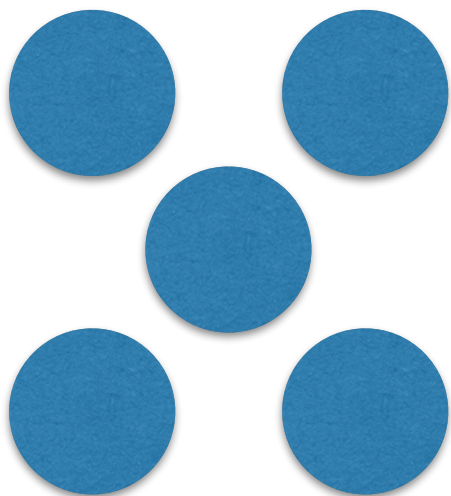
How many legs are there altogether?

How many horns?





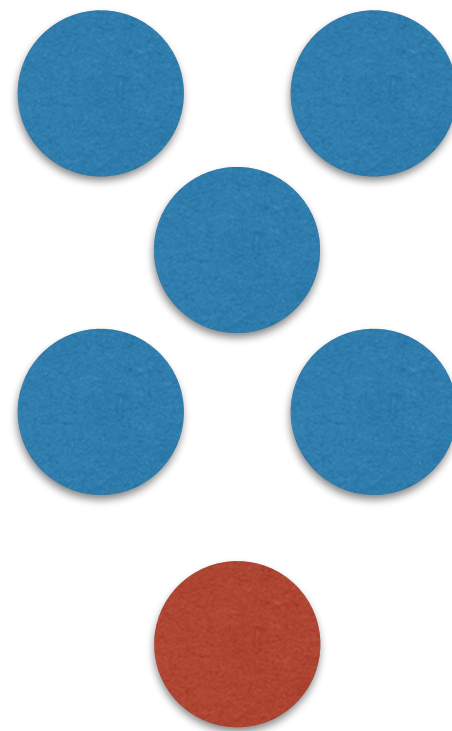
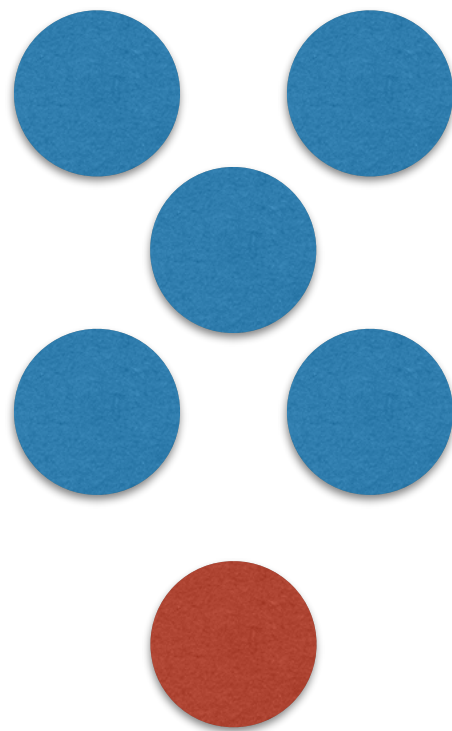
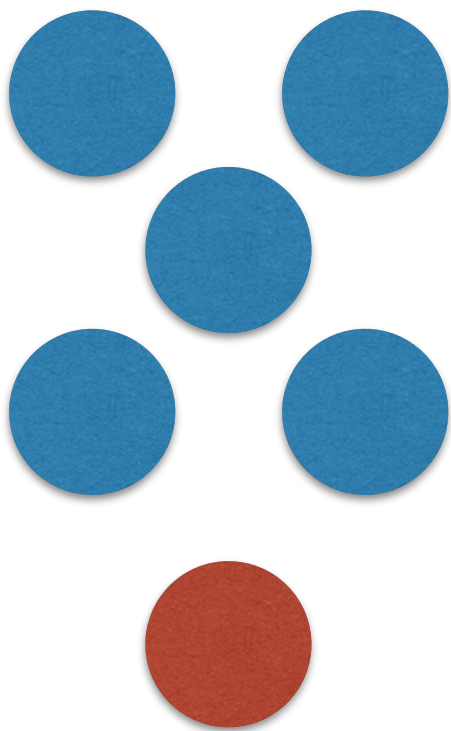
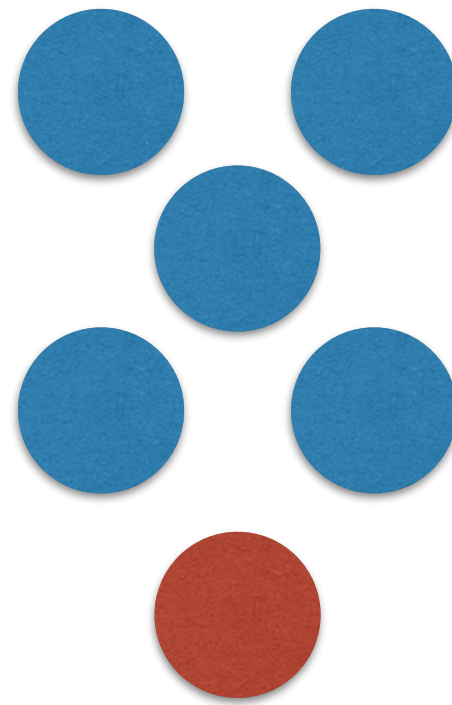
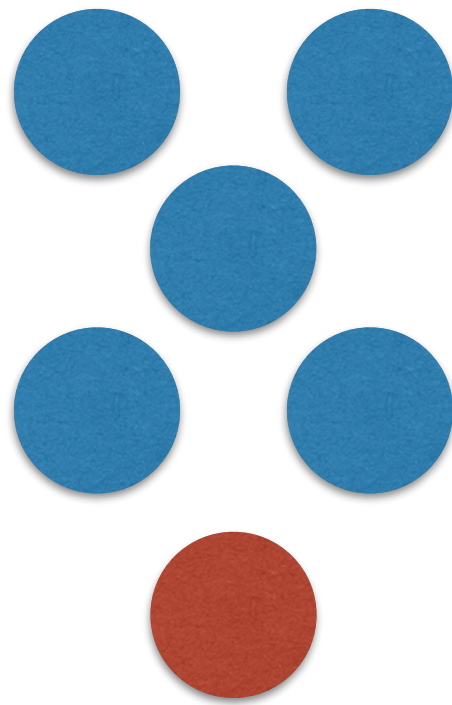
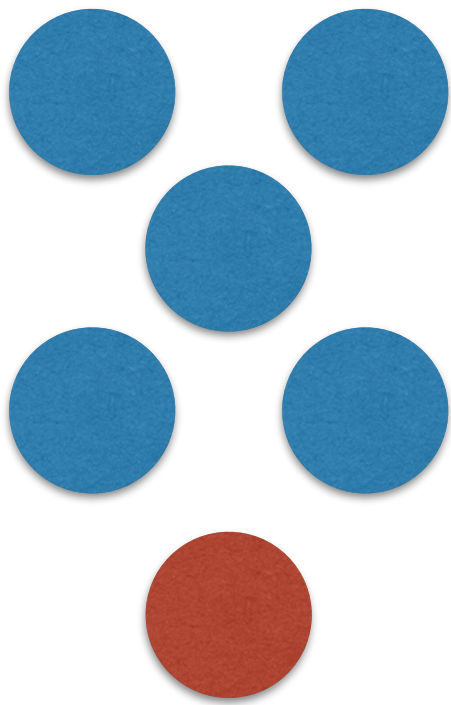




How many?

How did you see them?

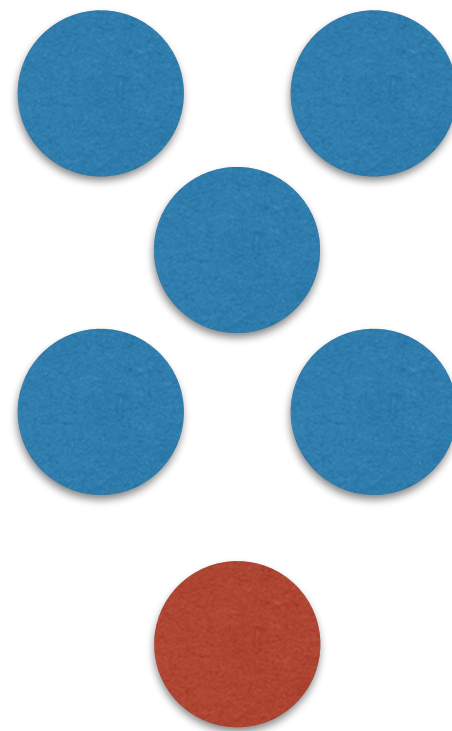
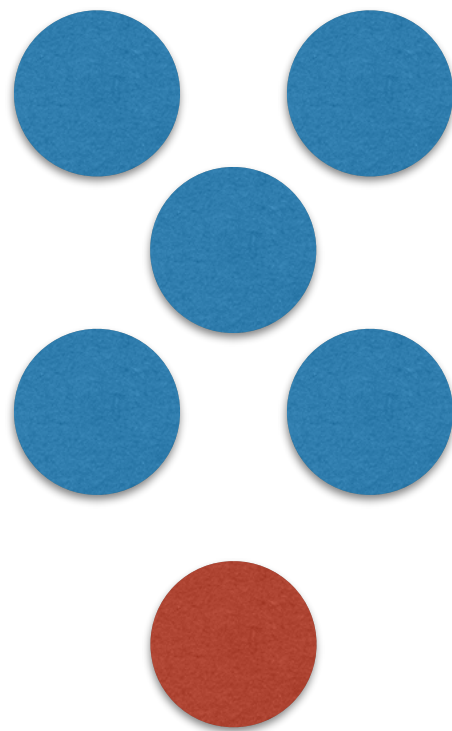
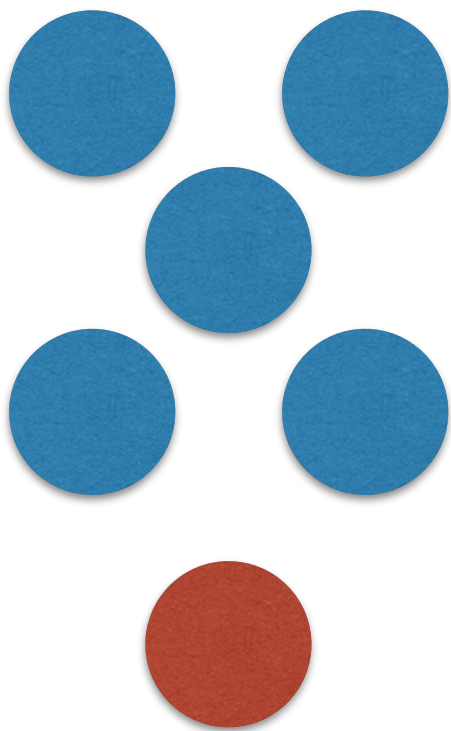
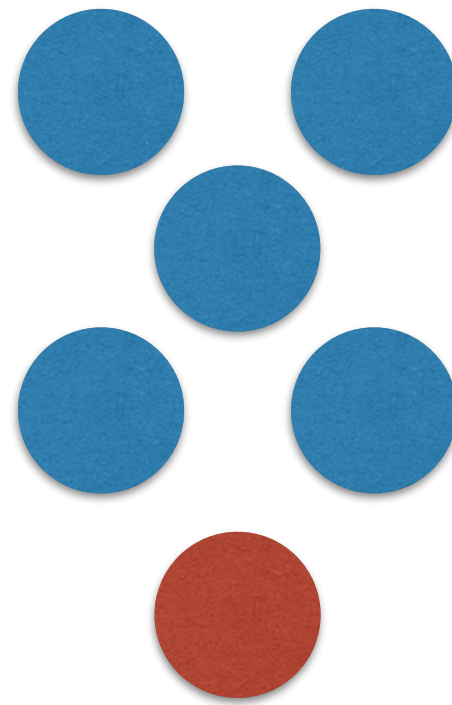
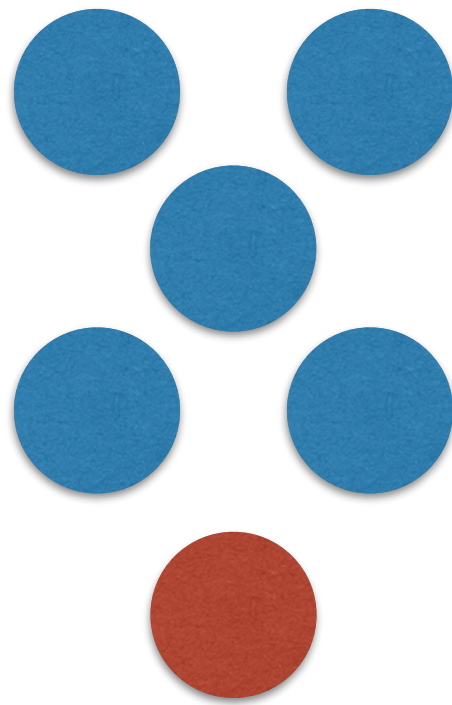
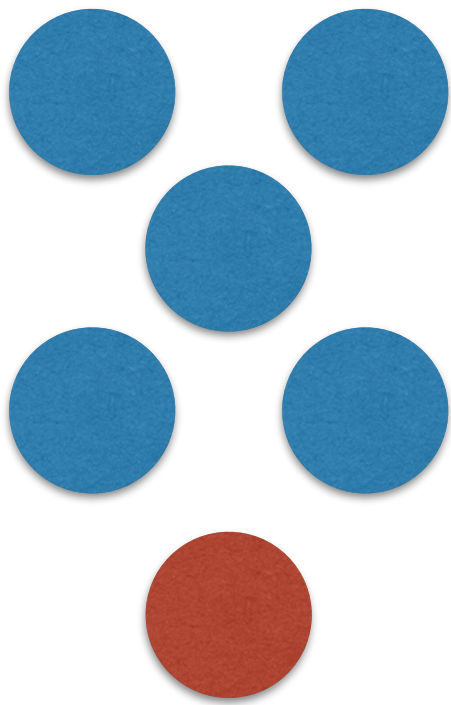


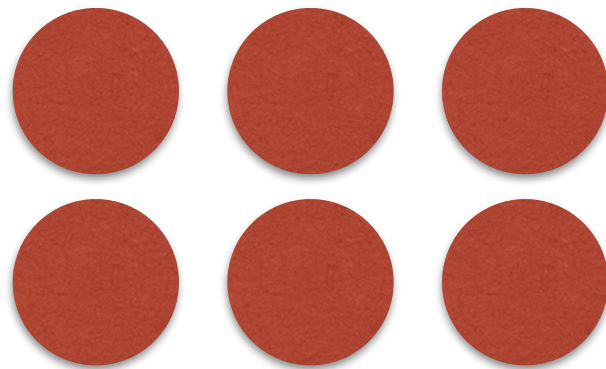
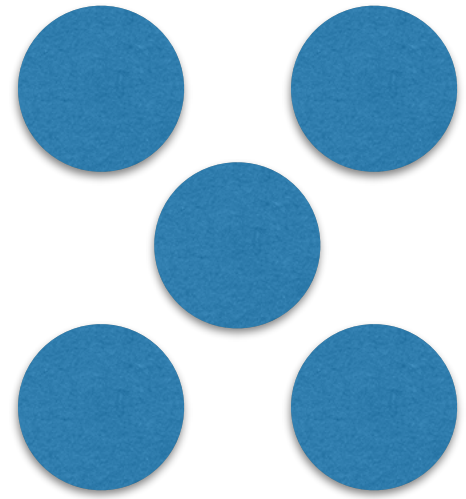
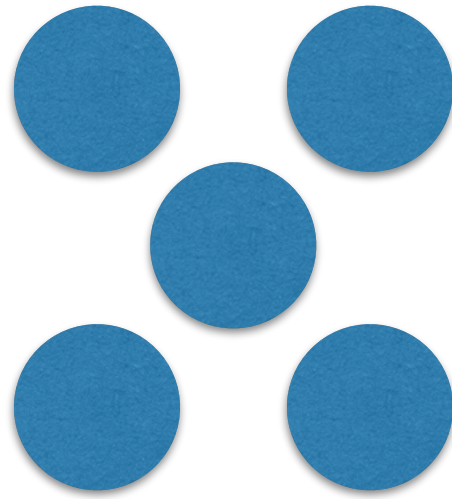
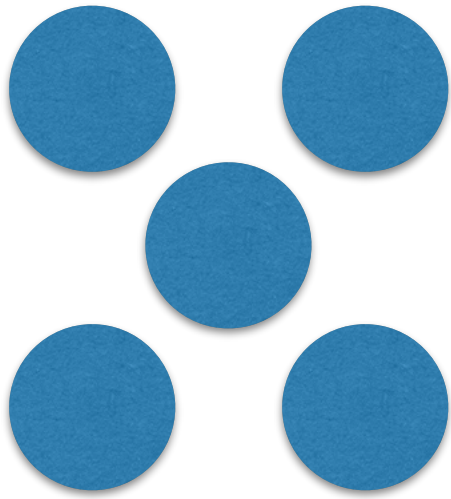
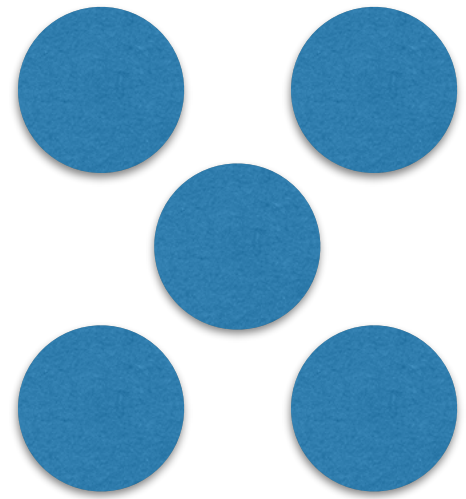
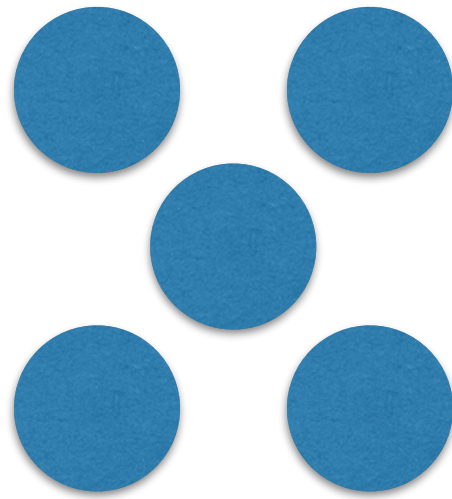
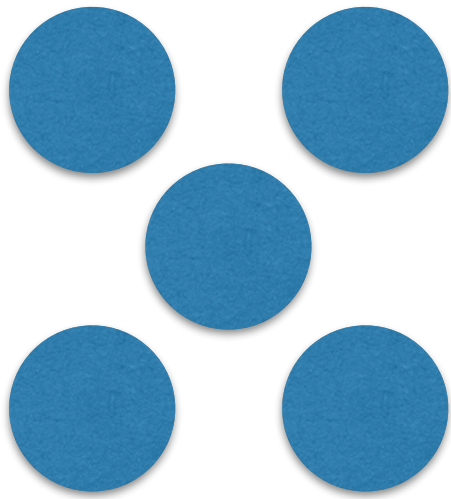


How many?

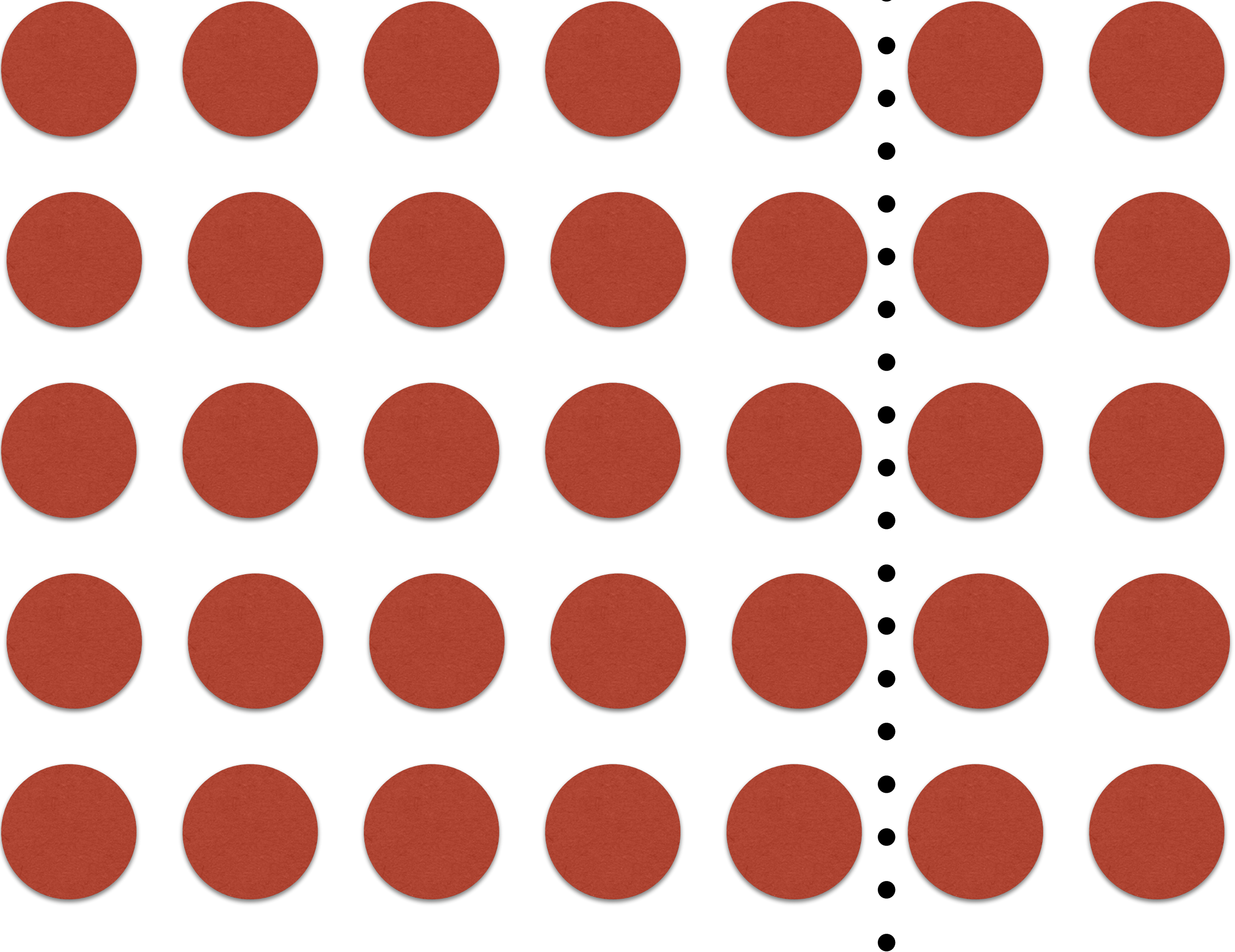
How did you see them?







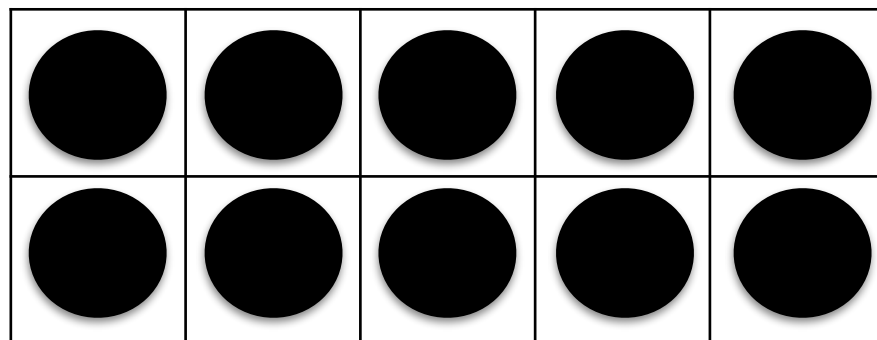
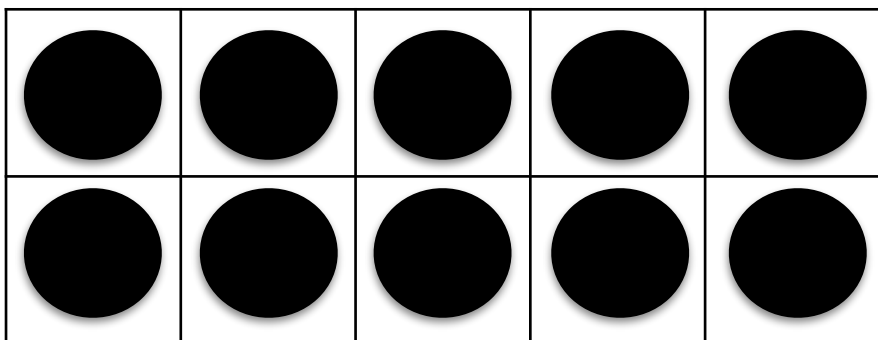
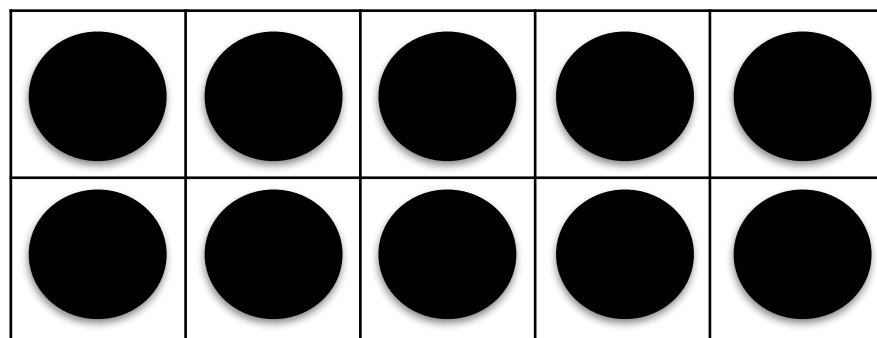
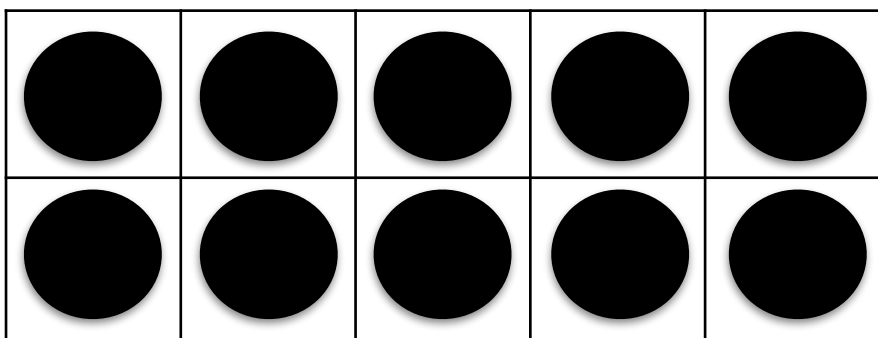
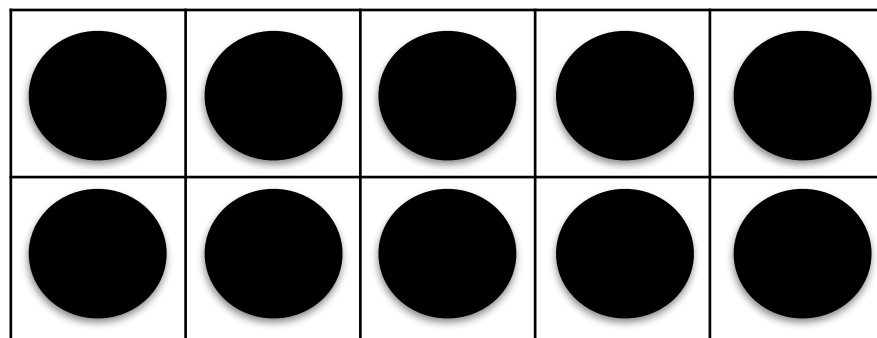
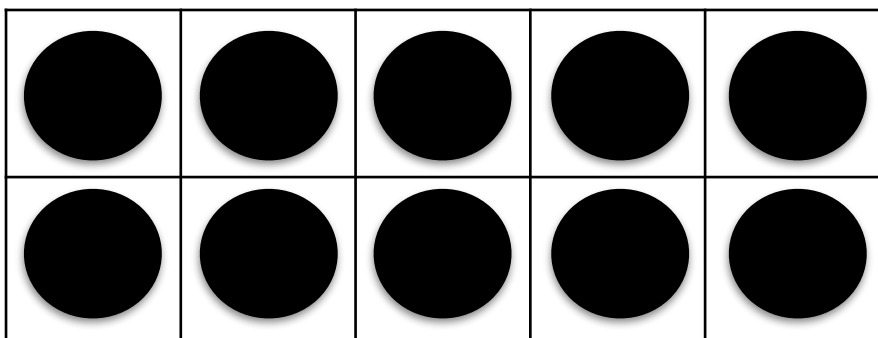
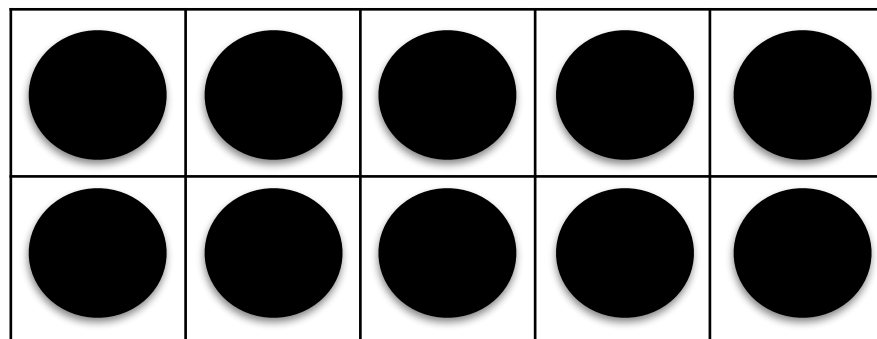
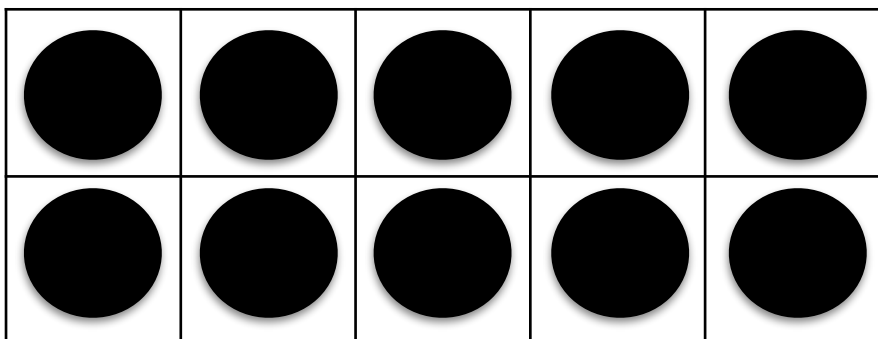
$$\begin{array}{c} 6 \\ \swarrow \quad \searrow \\ (6 \times 5) + (6 \times 1) \end{array}$$





How many?

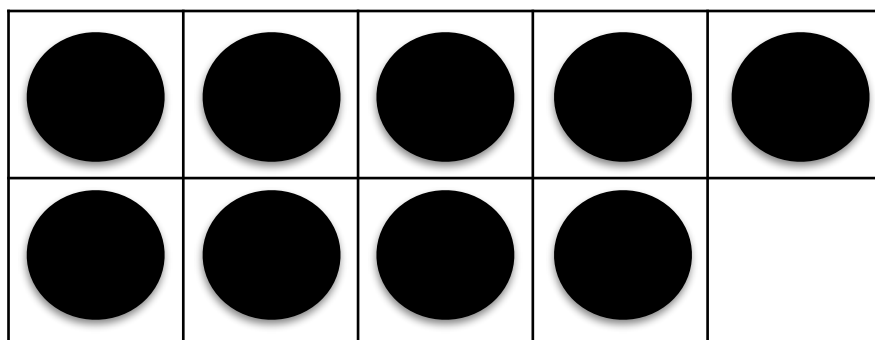
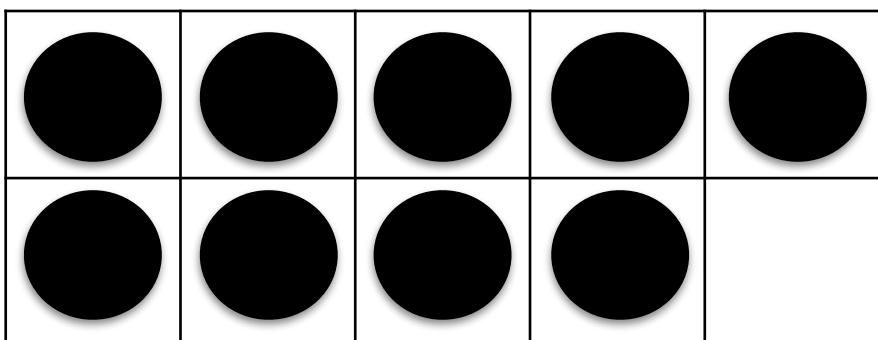
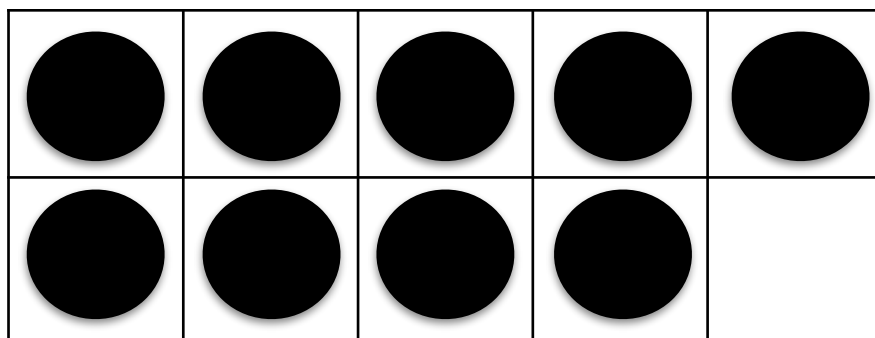
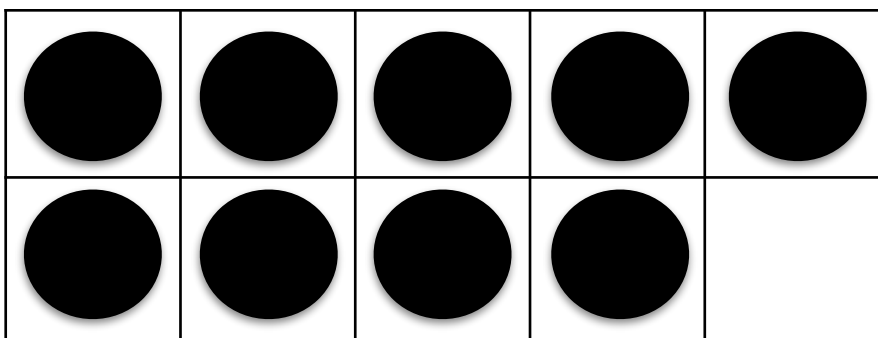
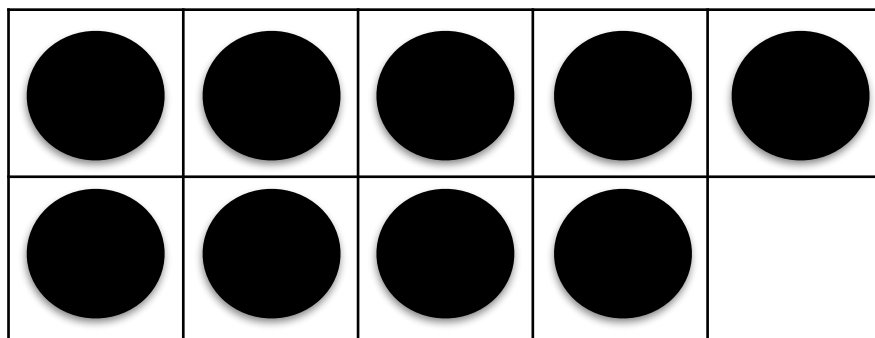
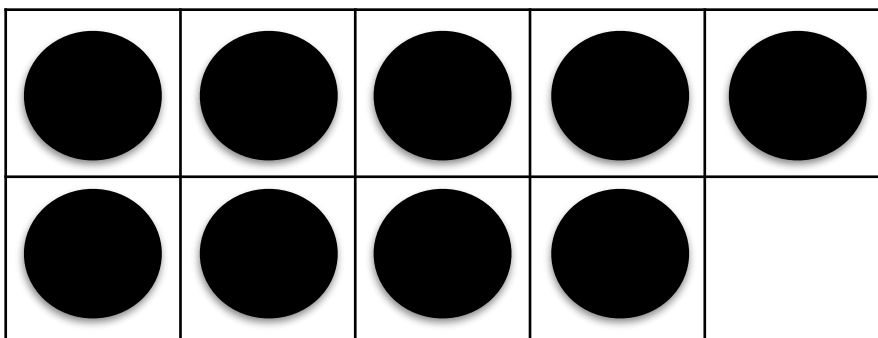
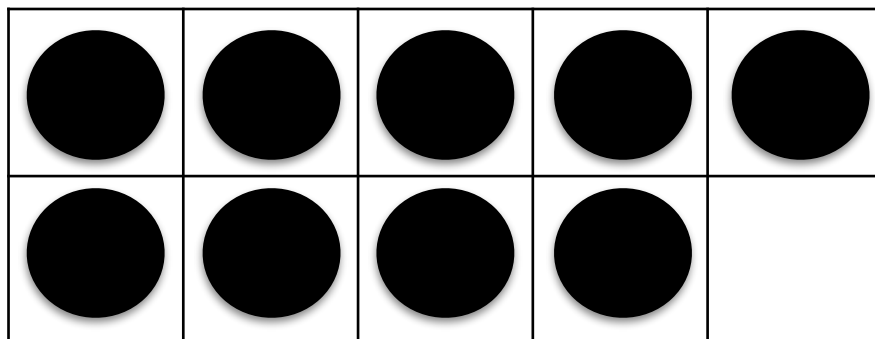
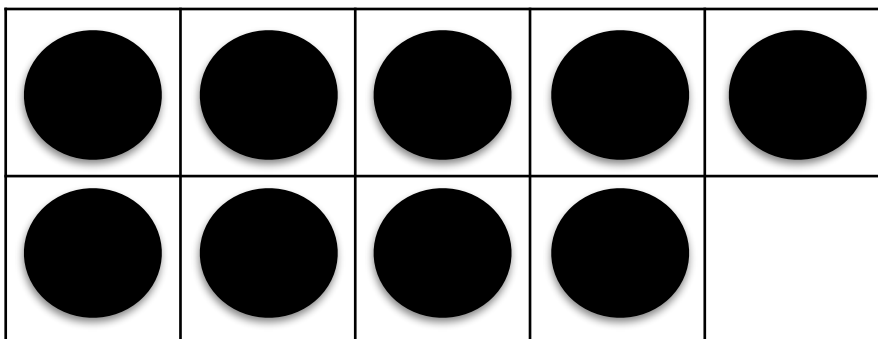
How did you see them?

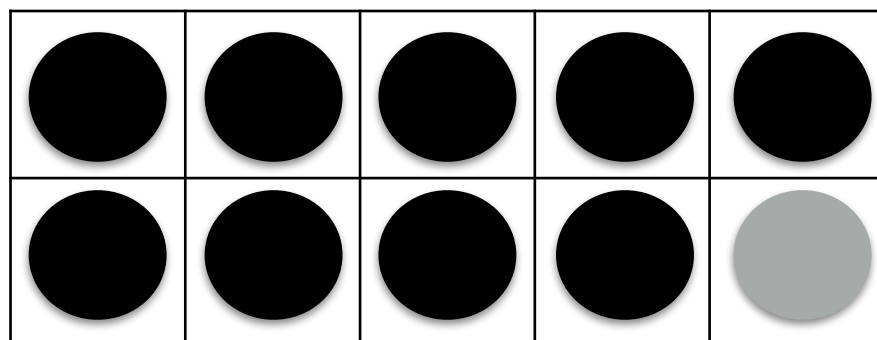
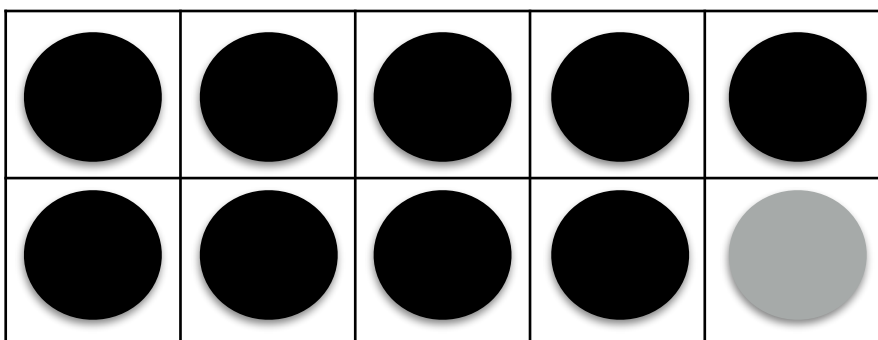
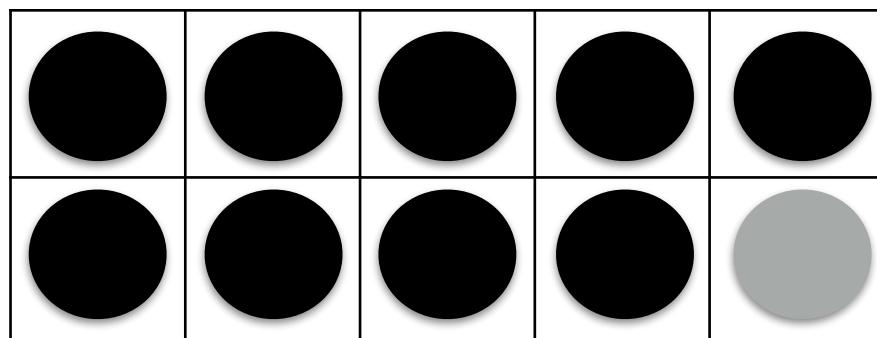
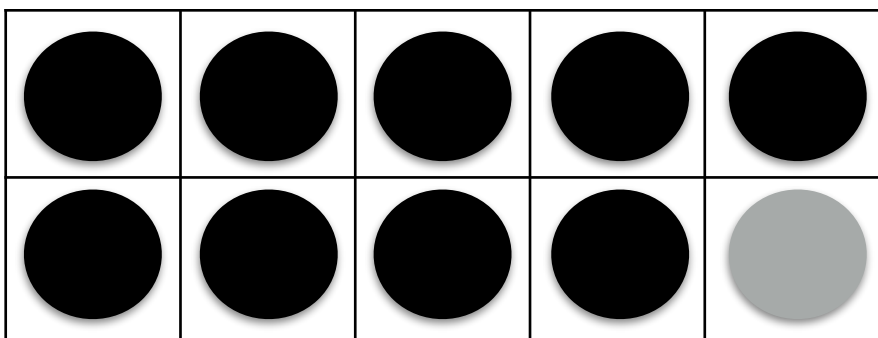
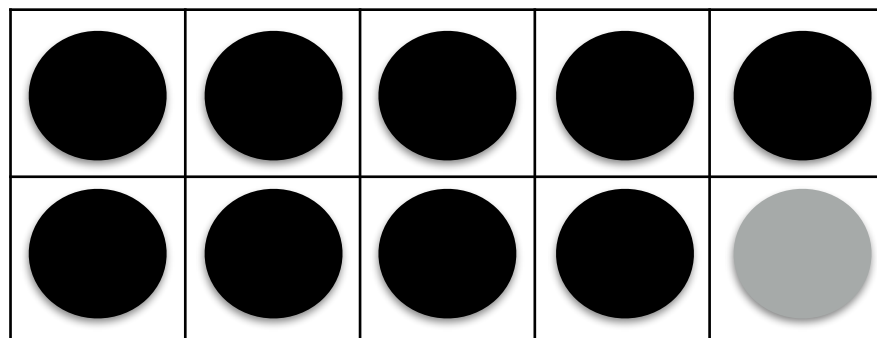
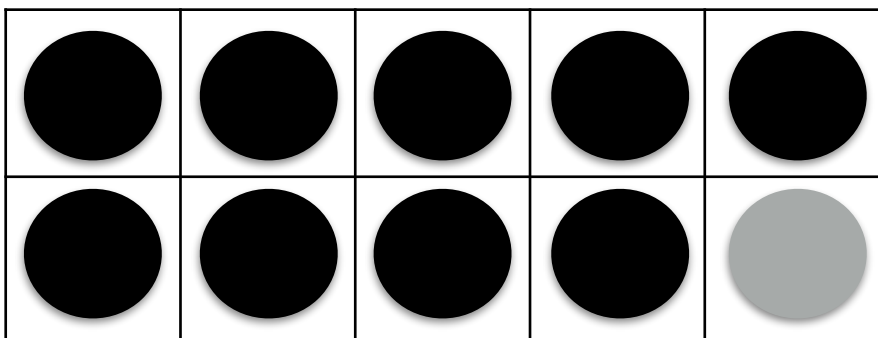
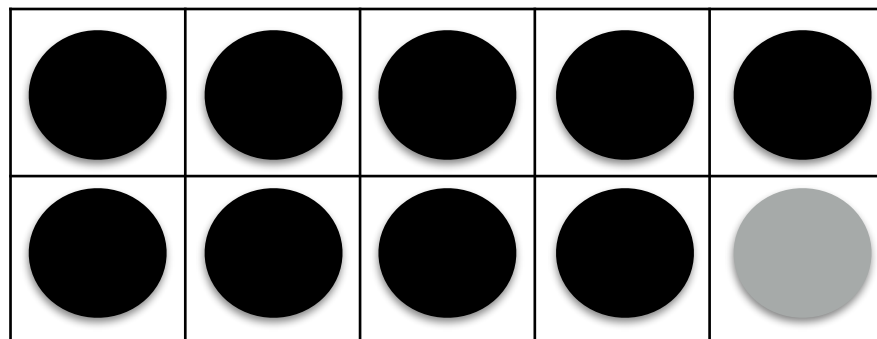
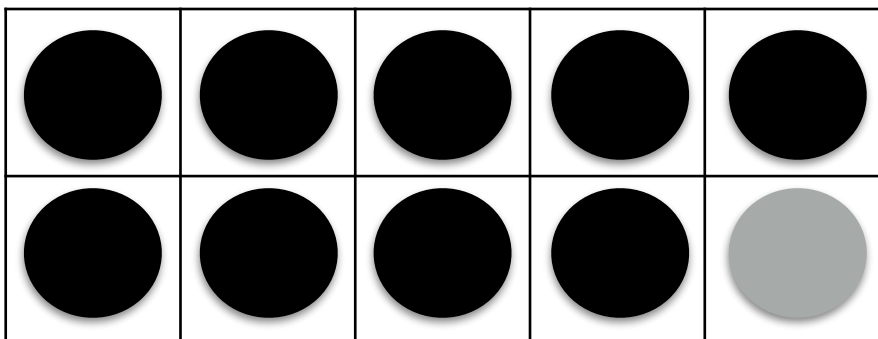


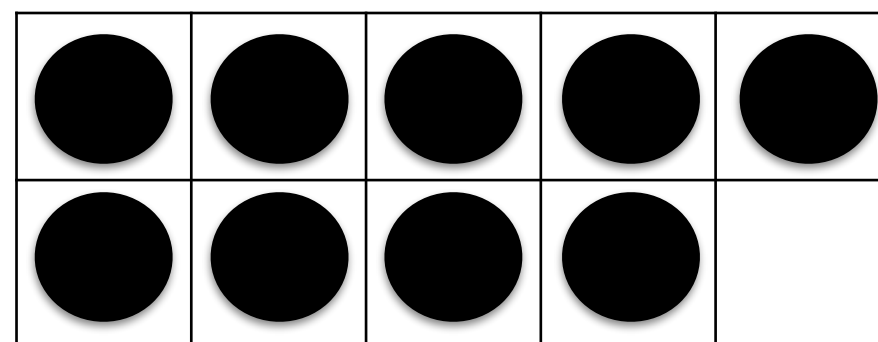
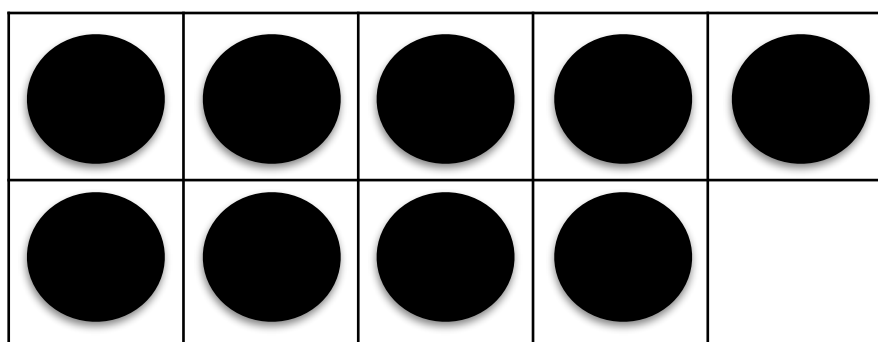
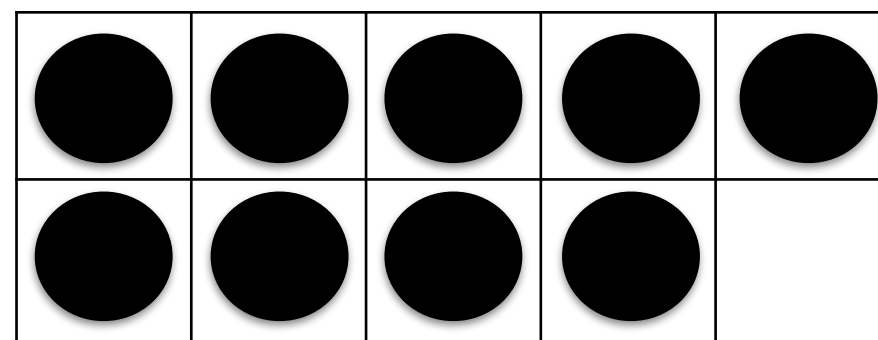
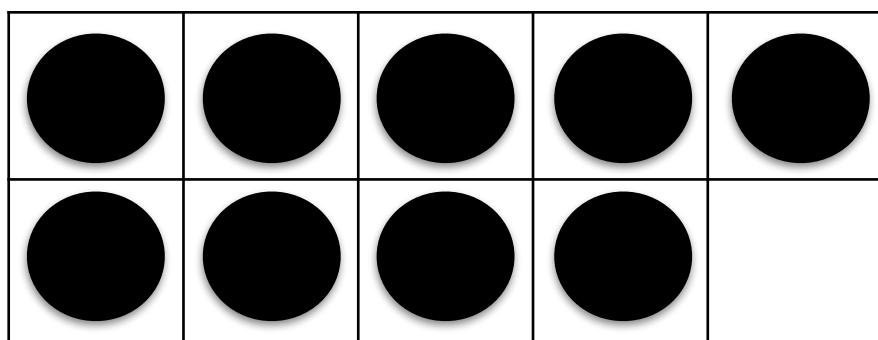
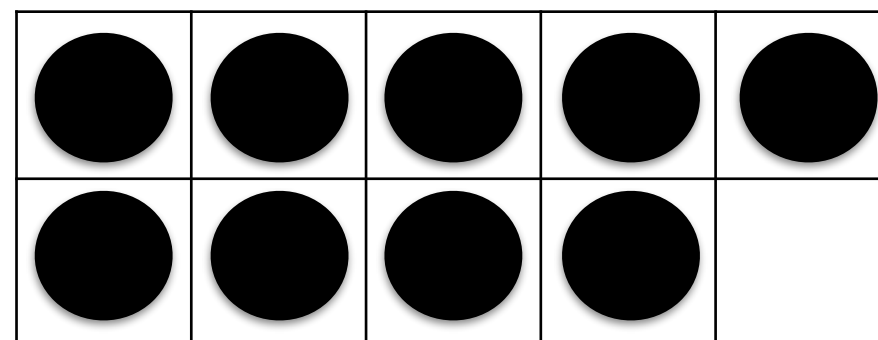
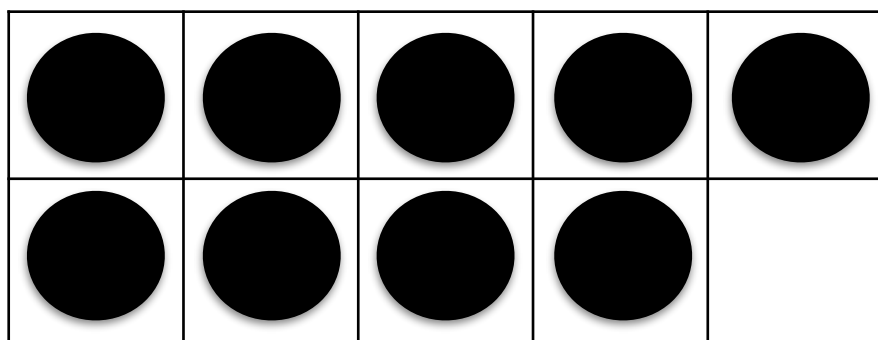
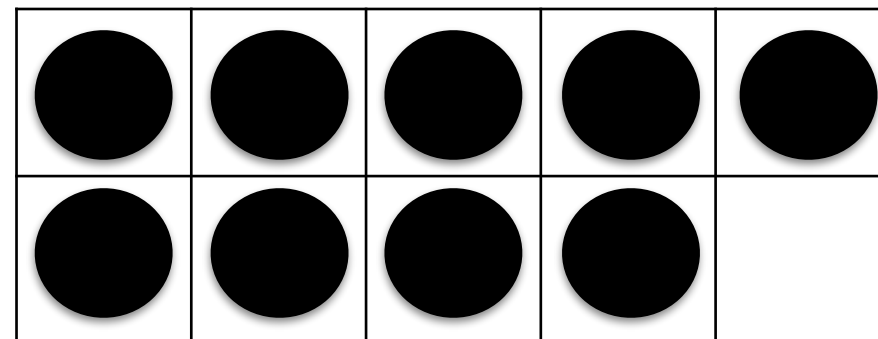
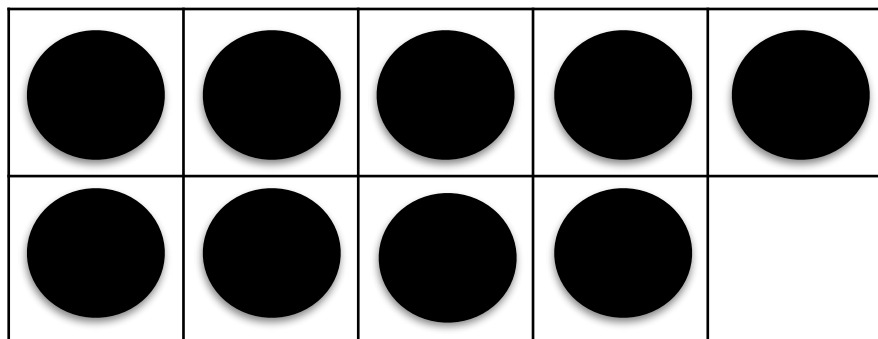
How many?

How did you see them?





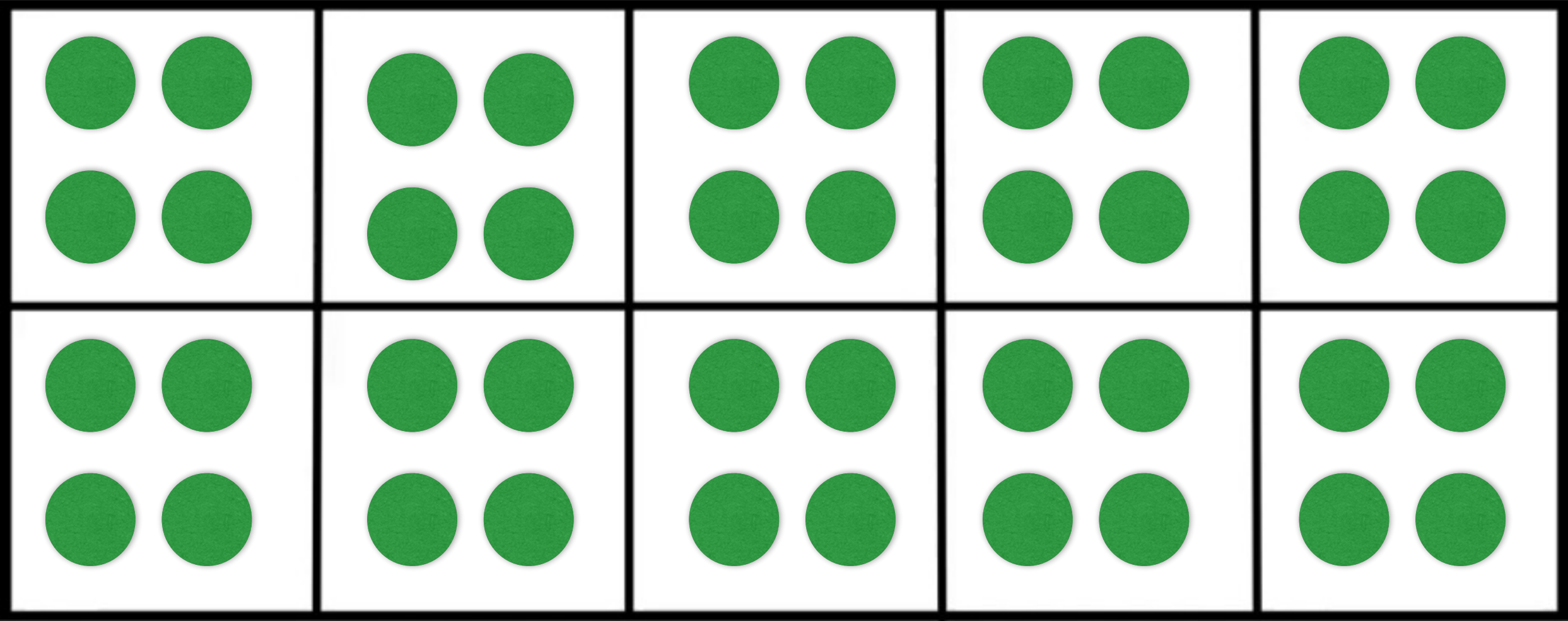




$$(8 \times 10) - 8 = 72$$

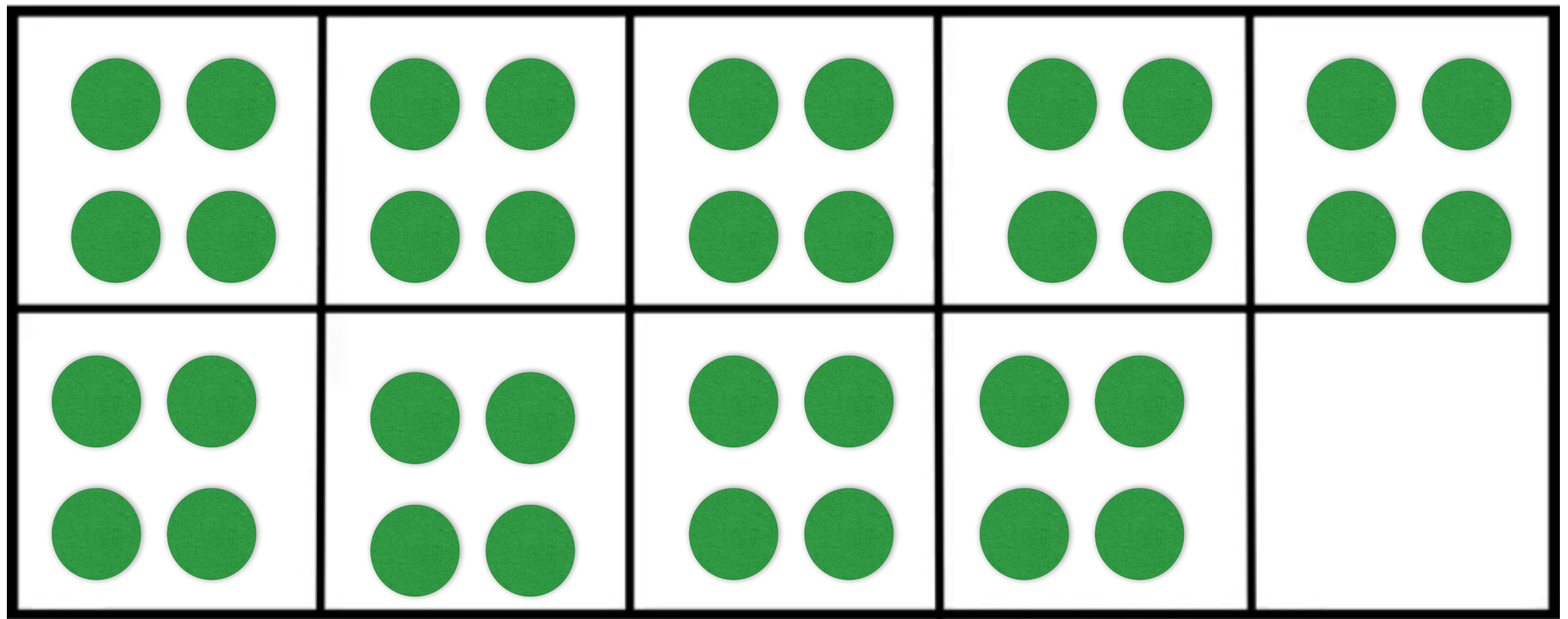






How many?

How did you see them?



How does thinking about the first image we saw help us with this new image?



# Number Talks

## Learning Intentions:

- develop multiple strategies for Decomposing (Mental Math)
- developing flexibility through use of multiple strategies
- Computational Fluency
- Place Value

10 - 15 minutes focussed on one question or a  
“string” of questions

$$\begin{array}{rcl} & & 6 \times 600 \\ 18 + 7 = & & 10 \times 600 \\ & & 16 \times 600 \\ & & 16 \times 599 \end{array}$$

# Two-digit x Two-digit example

- <https://www.teachingchannel.org/videos/4th-5th-grade-number-talks>

# SAME AND DIFFERENT

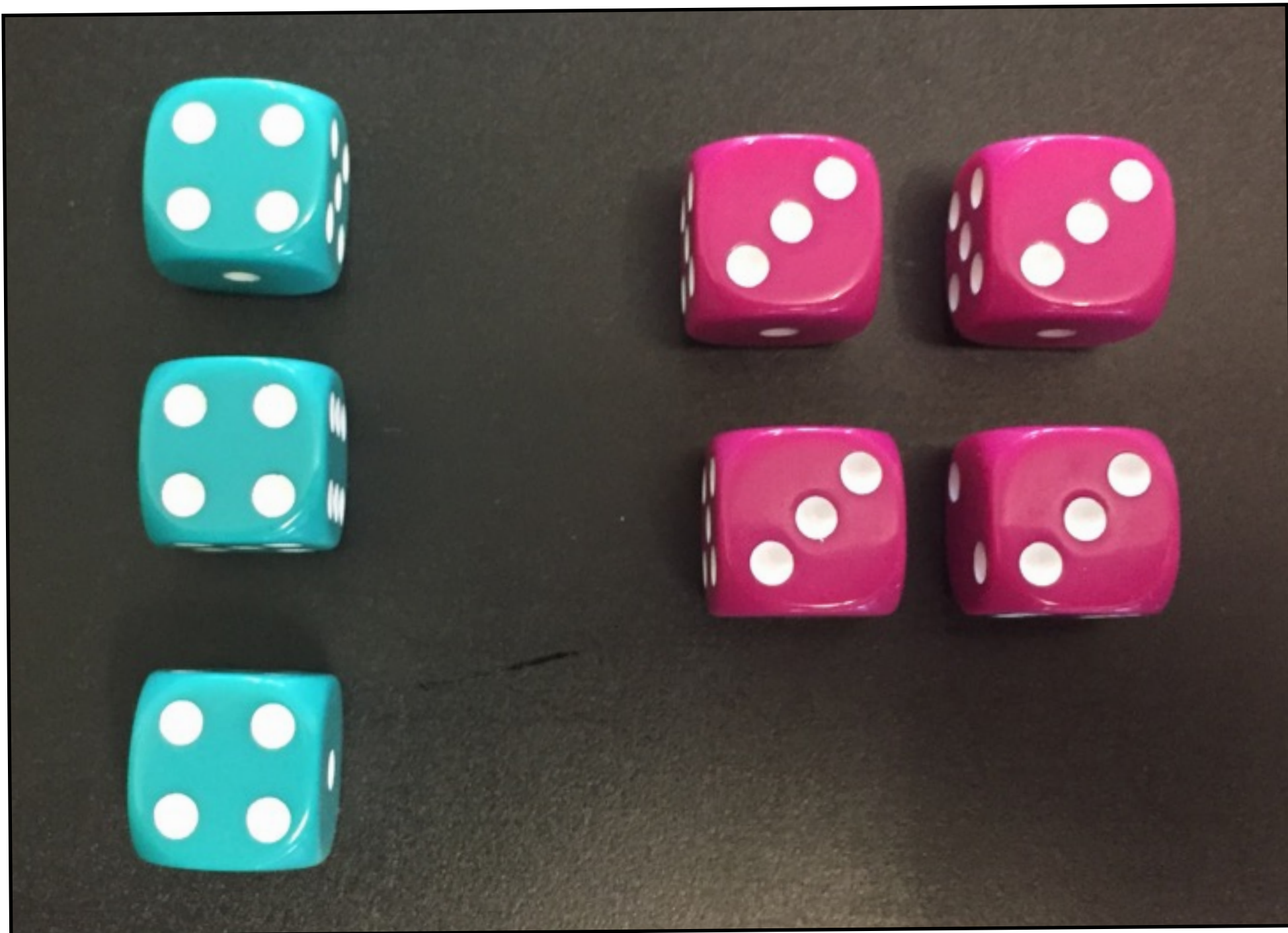
What's the learning?:

- identifying relationships between objects, shapes, and numbers
- using reasoning to construct arguments when comparing objects, shapes, and numbers
- develop their ability to communicate mathematical ideas





What is the same?  
What is different?



The image features a 4x4 grid of colored squares, likely representing a mathematical problem or a visual puzzle. The colors are red, yellow, and blue. The text 'SAME OR DIFFERENT?' is overlaid on the grid in a large, bold, white font with a slight shadow. The word 'SAME' is in a light blue color, 'OR' is in a light red color, 'DIFFERENT' is in a light blue color, and the question mark is in a light red color.

# SAME OR DIFFERENT?

*supporting mathematical argument in the elementary grades*

HOME

VIDEOS

CONTRIBUTORS

ABOUT



<https://samedifferentimages.wordpress.com/>

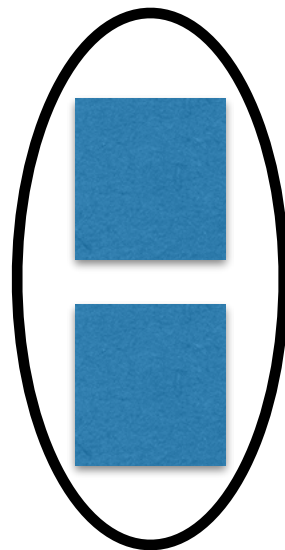
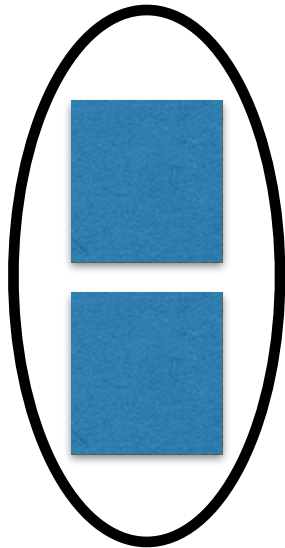
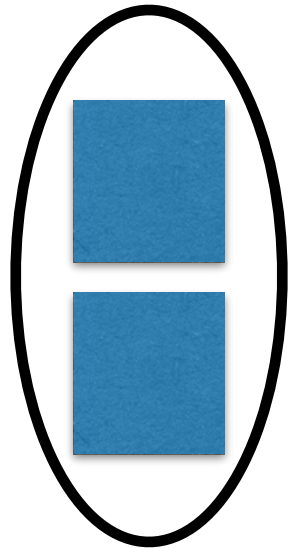
Website curated by Brian Bushart et al.

#samedifferent

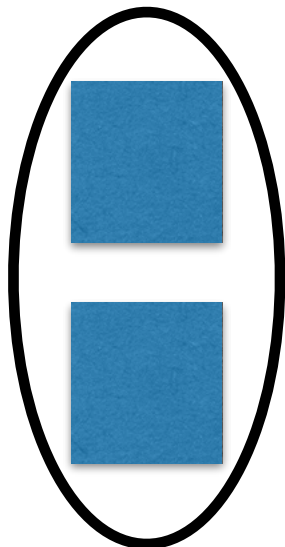
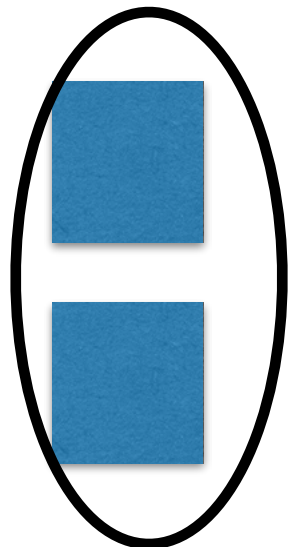
**TRUE**

**OR**

**FALSE**



$$= 5 \times 2$$





**TRUE OR FALSE**

$$3 + 3 + 3 = 4 \times 3$$

**TRUE OR FALSE**



$$= 4 \times 6$$

**TRUE OR FALSE**

$$2 \times 3 \times 4 = 3 \times 4 \times 2$$



**TRUE OR FALSE**

$$4 \times 4 = 2 \times 8$$

# TRUE OR FALSE

Inline Skating: 10:30

Does the order of factors matter?

$$2 \times 3 \times 4 = 3 \times 4 \times 2$$

6

24

$$(2 \times 3) \times 4$$

=

$$(4 \times 2) \times 3$$

24

8

factors

Commutative Property


$$\begin{array}{c} 3 \times 4 \\ \swarrow \searrow \\ 4 \times 3 \end{array}$$

Associative Property

# Multiplication Games

**Cover Up! A Doubles Game**

**How to Play**  
 Roll a 10-sided die. Multiply your number by 2.  
 Find it on the grid and cover it in your color.  
 Partner 2 gets a turn.  
 The first one to have 4 in a line wins!  
 Roll a 0 and lose a turn!



**You need**  
 ~ 10 sided dice  
 ~ Counters (2 different colors)

12	6	10	12	4	8
14	18	6	16	2	6
6	10	2	12	10	14
12	4	8	18	16	10
14	16	2	14	4	12
10	8	4	2	16	18



**Double or Double-Double**

**Factor Box**

Pick a factor from the Factor Box.  
 Double it (multiply by 2) or double-double it (multiply by 4).  
 Find the product below and cover it in your colour.  
 Four in a row wins!

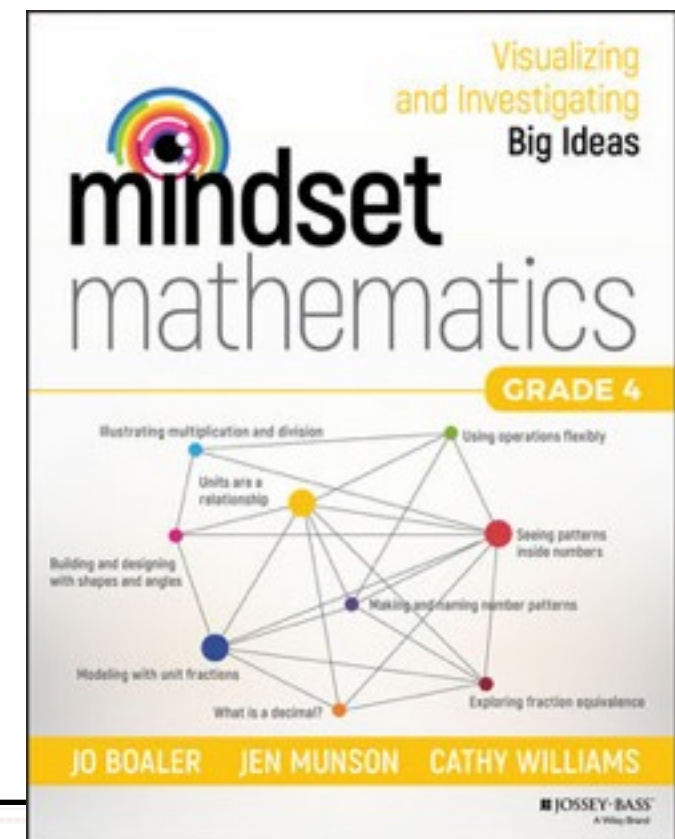
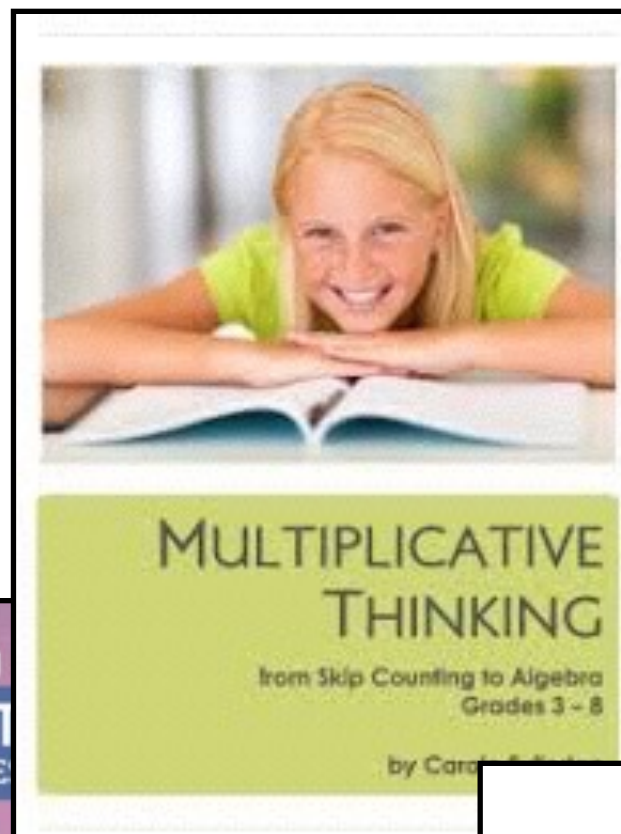
24	8	6	20	12	4
16	28	14	32	18	24
10	2	6	36	28	40
12	14	18	4	16	20
10	8	24	32	36	2
40	28	18	16	4	6



See handout for links to many different multiplication games!



# Key Resources:



Fair Shares: Teaching Division in Grades 4-7



TEACHERS  
who LOVE  
teaching,  
.....teach  
children  
TO love LEARNING.